

Momentum distribution and production cross section of projectile-like fragments at intermediate energies

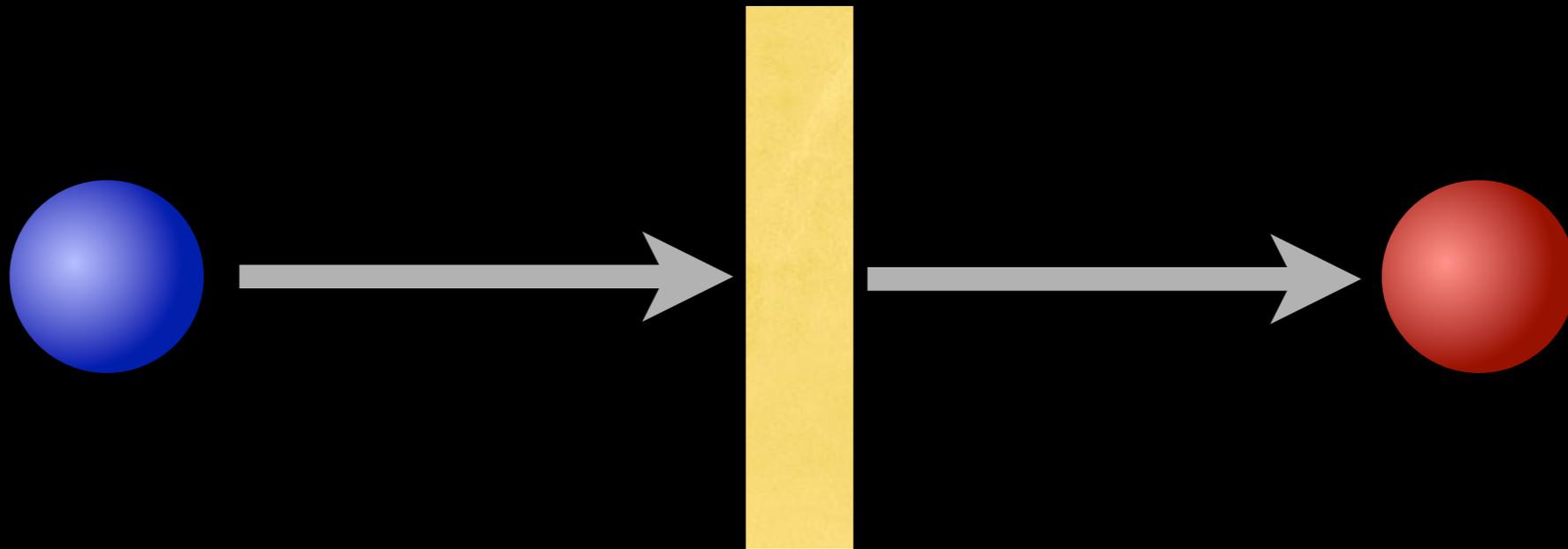
Sadao MOMOTA

Kochi University of Technology

Introduction

Fragmentation process

- as a means to produce RI beams

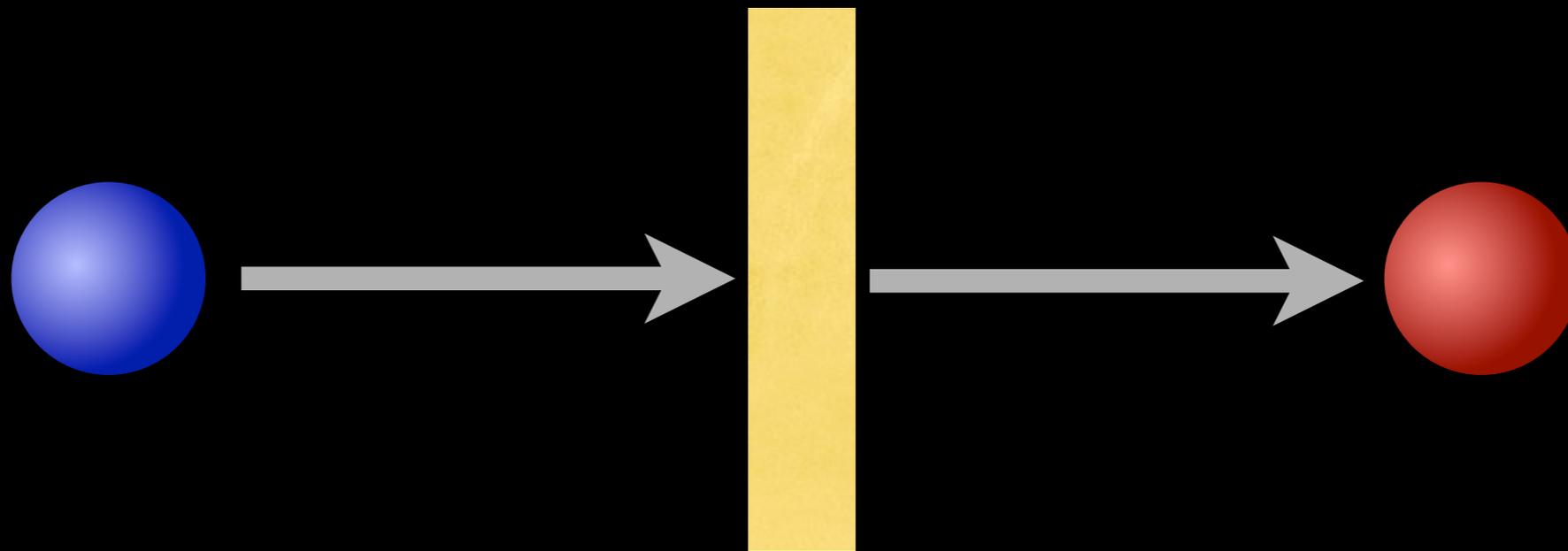


- $\sigma_{\text{Prod.}}$

- $\frac{d\sigma_{\text{Prod.}}}{dP_L}, \frac{d\sigma_{\text{Prod.}}}{dP_T}$

Fragmentation process

- as a means to produce RI beams



- $\sigma_{\text{Prod.}}$

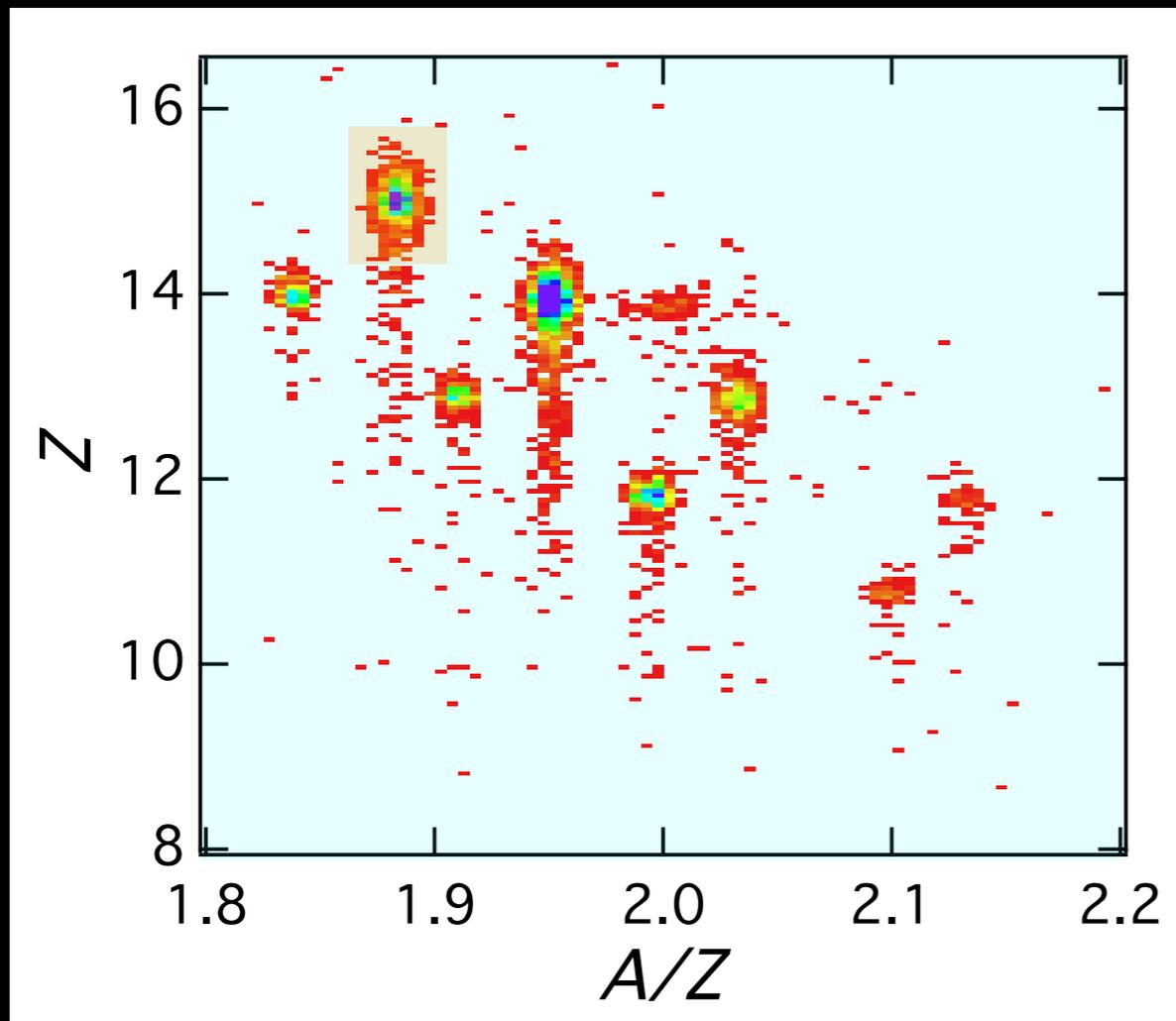
- $\frac{d\sigma_{\text{Prod.}}}{dP_L}, \frac{d\sigma_{\text{Prod.}}}{dP_T}$

1. Quality of RI beams

2. Reaction mechanism / nuclear structure

3. Nuclear database

Quality of RI beams



- Intensity/Purity

- Simulation code

INTENSITY, LISE, MOCADI

- Empirical systematics/
formulation

EPAX *etc.*

- $\sigma_{\text{Prod.}}$

- P_L, P_T distribution

Nuclear database

Transport of heavy ions in materials

- Radiation shield at RIB facility
- Space mission (Irr. effect of galactic cosmic ray)
- HI therapy

Nuclear database

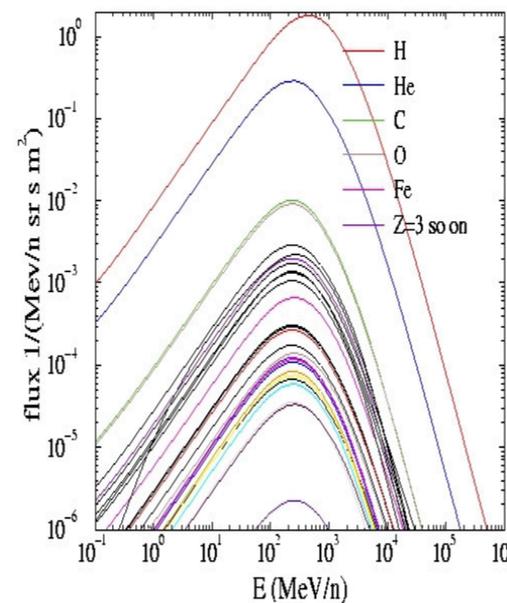
Transport of heavy ions in materials

- Radiation shield at RIB facility
- Space mission (Irr. effect of galactic cosmic ray)
- HI therapy

Heavy Ions:
small in number - but important in radiation effects

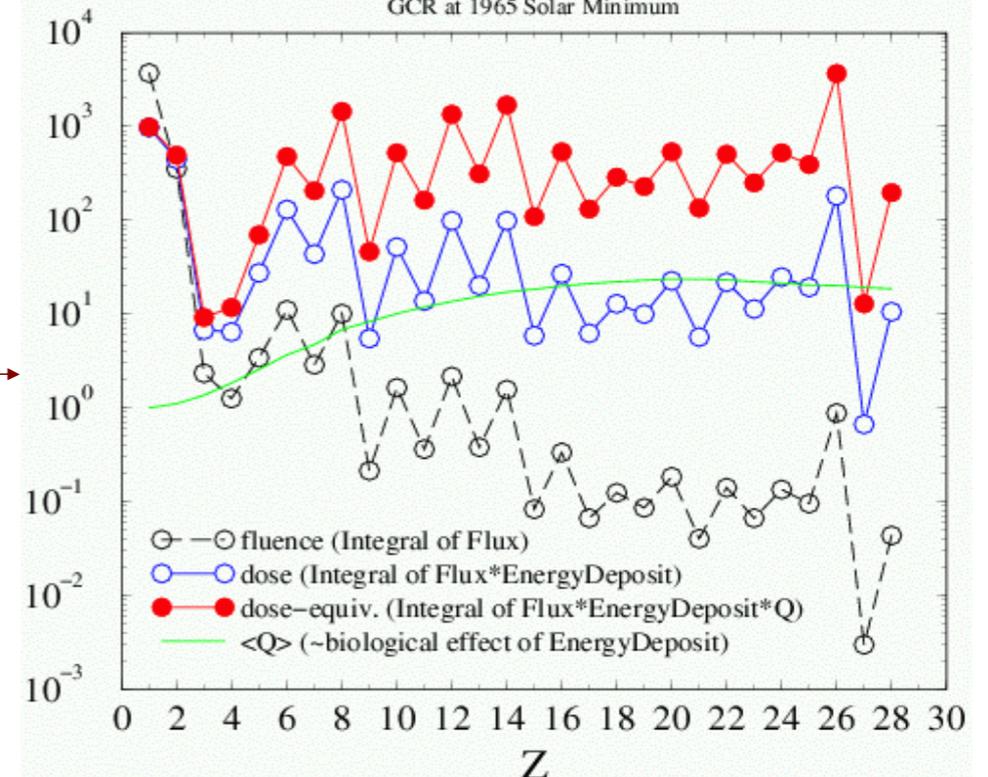
Galactic Cosmic Rays

HZETRN input iyear=2 (1965 solar min)



Fluence, dose, dose-equivalent of different elements

GCR at 1965 Solar Minimum



Momentum dist.
and $\sigma_{\text{Prod.}}$

Evaluation of prod. rate

- In case of LISE++

Formulation/Systematics ← Prod. process

Projectile fragmentation

Fragment velocity | Momentum distribution | Cross section, Excitation energy and etc

Final relation Vf/Vb been used in the program = 1.000 40Ar(140.0 MeV/u) + Be -> 32S

Fragment velocity

- Constant V fragment / V beam = 1
- Calculation - A [V.Borrel et al., Z.Pyhs.A314(1983)191]
- Calculation - B [F.Rami et al., NPA 444(1985)349]
- Calculation - C [O.Tarasov, NPA 734(2004)536]
- Calculation - D [from two-body reaction]
- Calculation - E [D.Morrissey, PRC 39(1989)460]
 - Vf / Vb = 0.989
 - dE/dA = 8 at Afrag = Aproj
 - 8 at Afrag = Aproj / 2

Options

- Velocity after reaction can not exceed fragment velocity from two-body reaction kinematics (at 0 degree). It is important for pick-up reactions!
- Assume symmetric velocity distribution around Aproj / 2. Important for light fragment production.
- Use velocity shift for pick-up reactions
R.Pffaf, D.Morrissey et al., PRC51(1995)1348
- Exclude this shift for (p,n) and (n,p) reactions

A - V.Borrel et al., Z.Pyhs. A314(1983)191

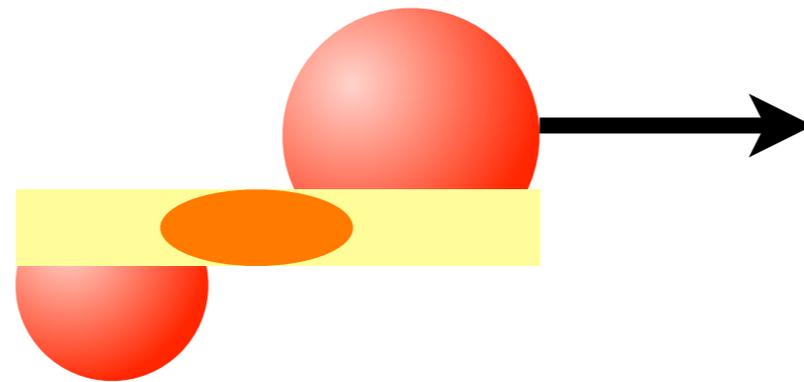
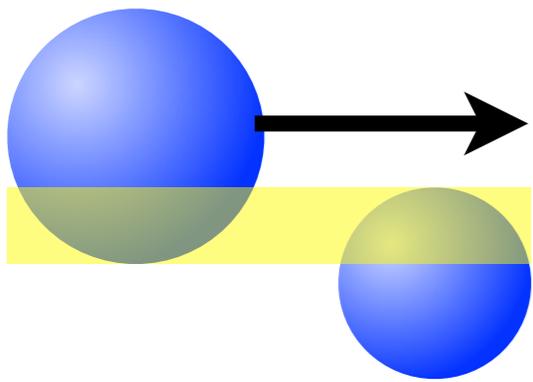
$$\frac{v_F}{v_p} = s + \sqrt{1 - \frac{B_n(A_p - A_F)}{A_F E_p}}$$

Shift of Vf/Vb relation velocity (s) 0 (default 0) Vf / Vb

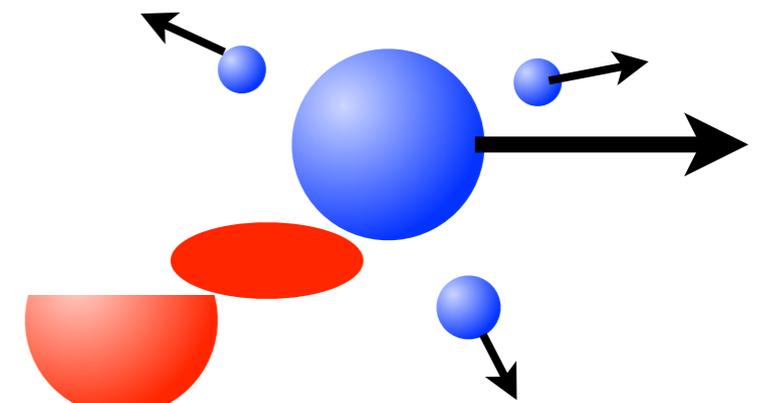
Energy necessary to ablate one nucleon (Be) 8 MeV (default 8) 0.993

Participant-Spectator

- Independent particle model



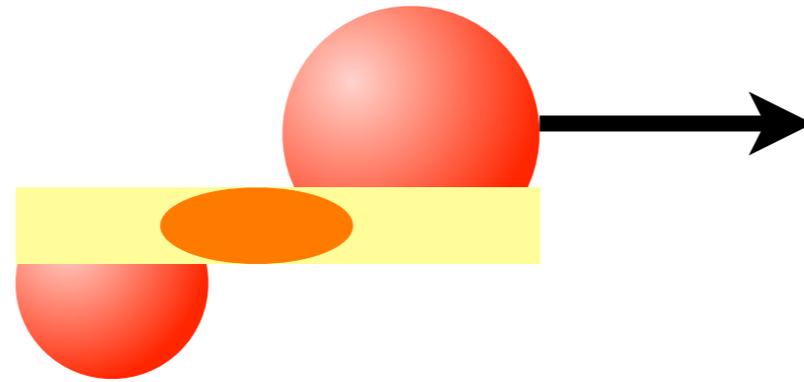
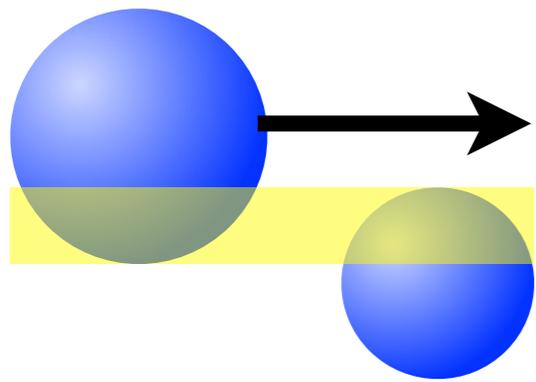
Abrasion-ablation



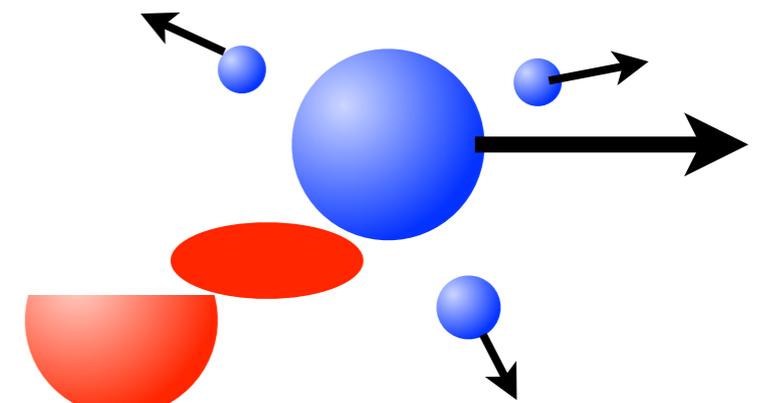
Statistical decay

Participant-Spectator

- Independent particle model



Abrasion-ablation



Statistical decay

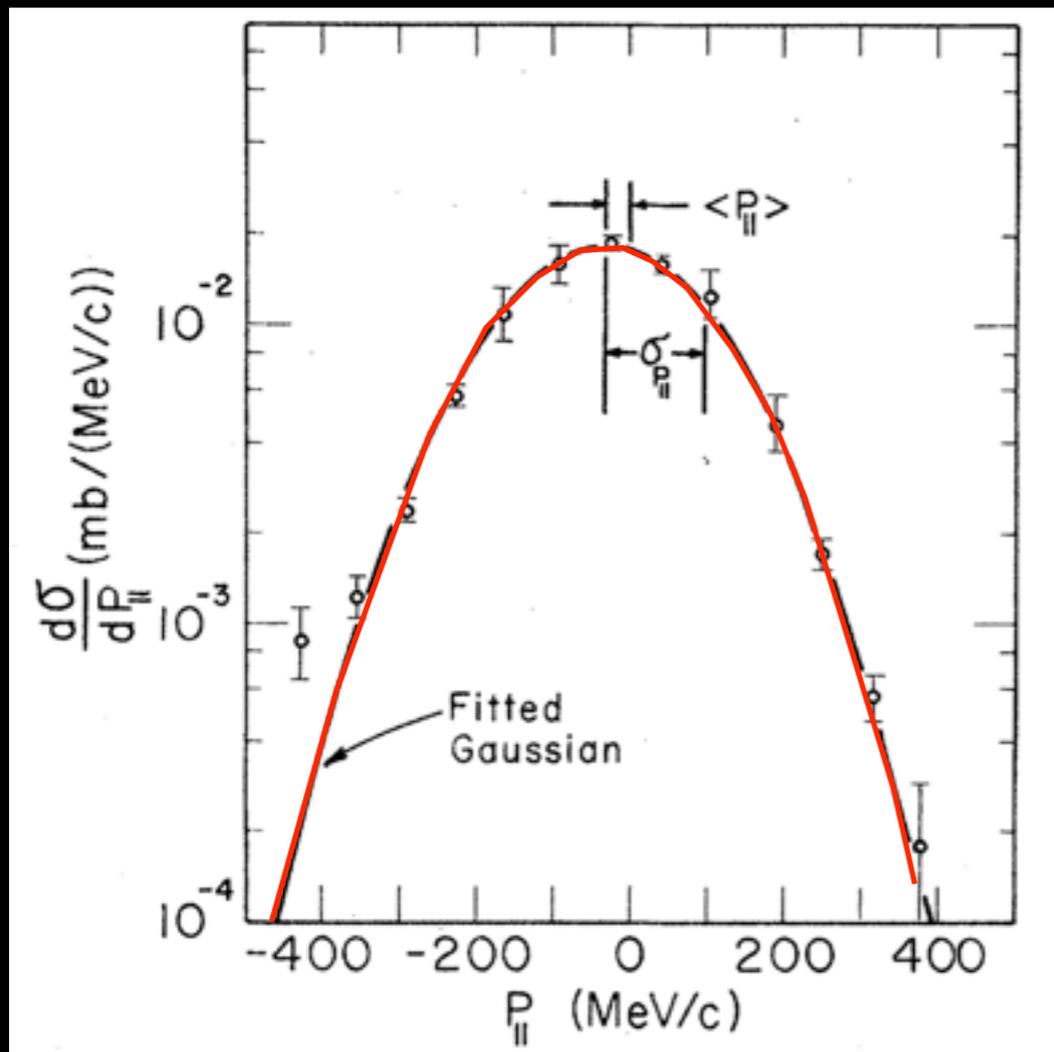
This model provides

- 1) Velocity shift : small
- 2) P dist. : P_{Fermi} of removed nucleons

P dist. at $E \cong 1$ GeV/u

- Isotropic distribution

^{12}C (2.1 GeV/u) + Be \rightarrow ^{10}Be

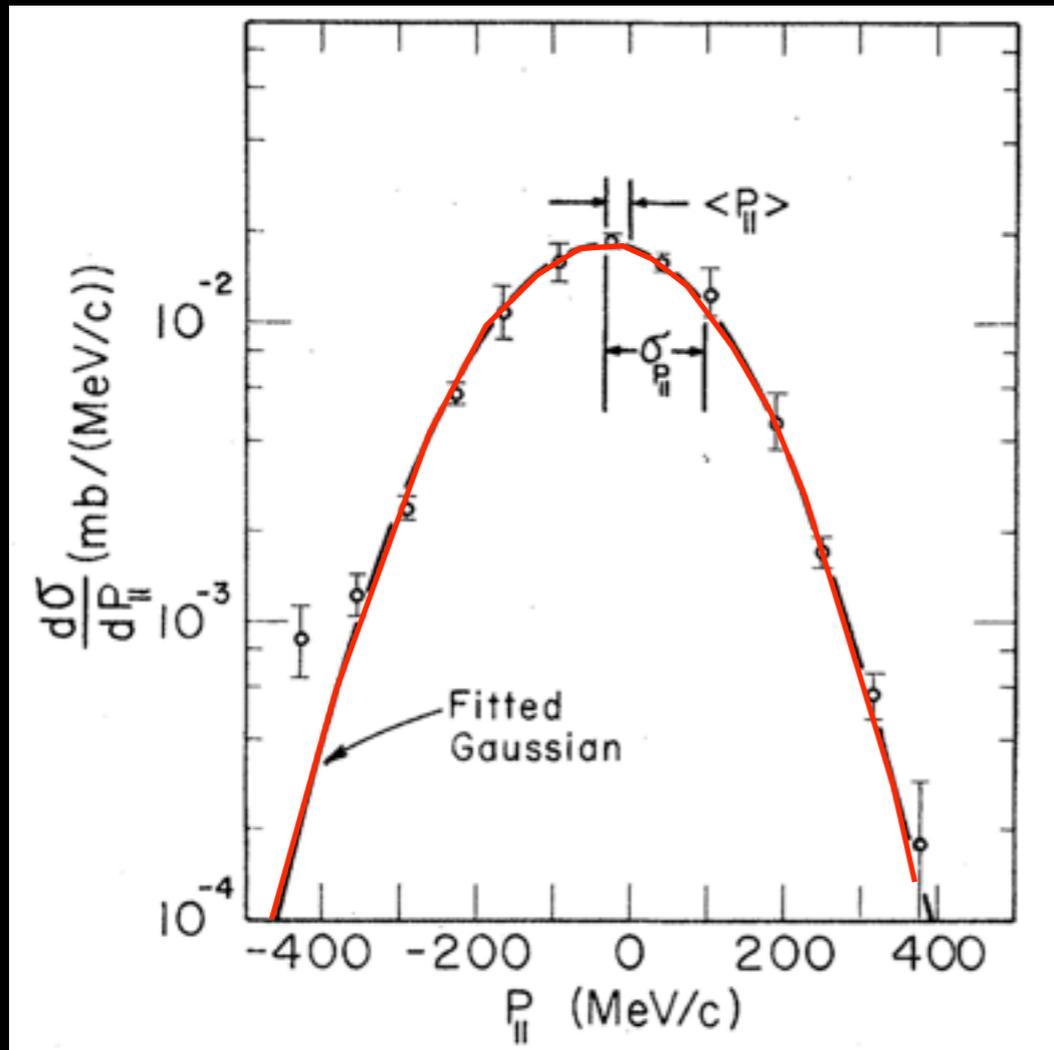


D.E. Greiner et al., PRL 35 (1975) 152.

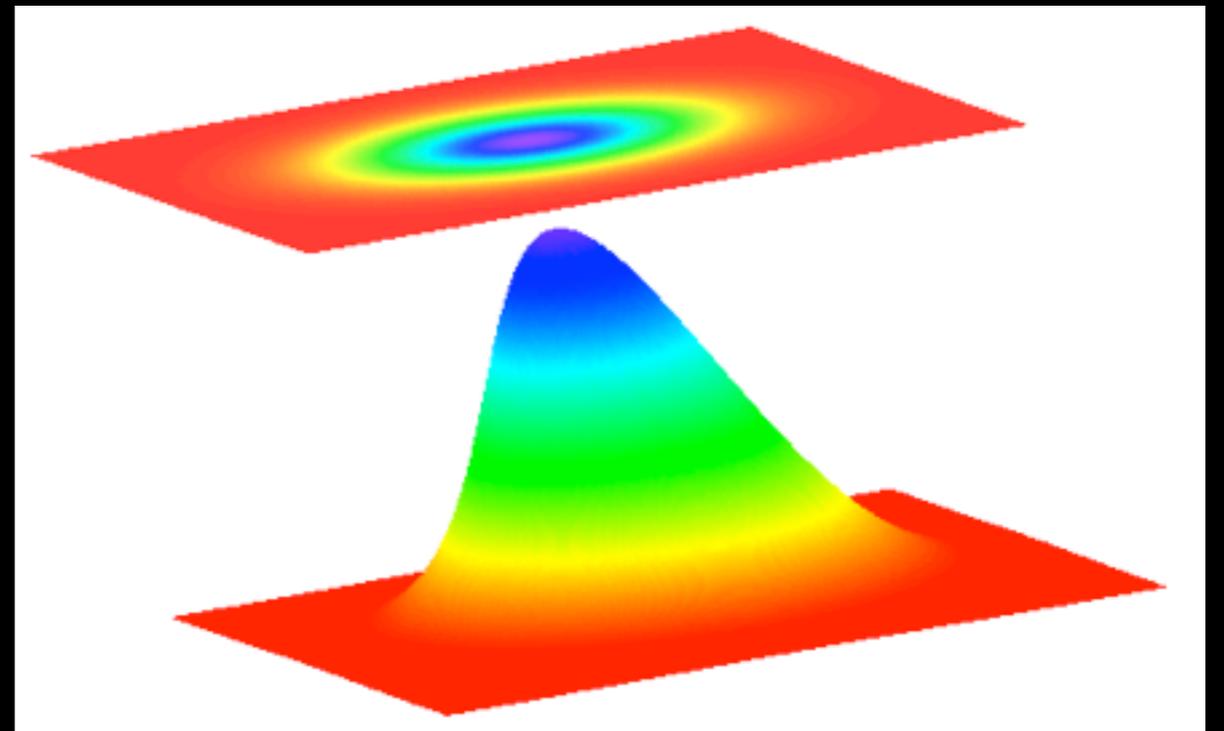
P dist. at $E \cong 1$ GeV/u

- Isotropic distribution

^{12}C (2.1 GeV/u) + Be \rightarrow ^{10}Be



D.E. Greiner et al., PRL 35 (1975) 152.



- **Isotropic** Gaussian dist.

$$\sigma(P_{\text{High}}) \sim \sigma(P_{\text{Low}})$$

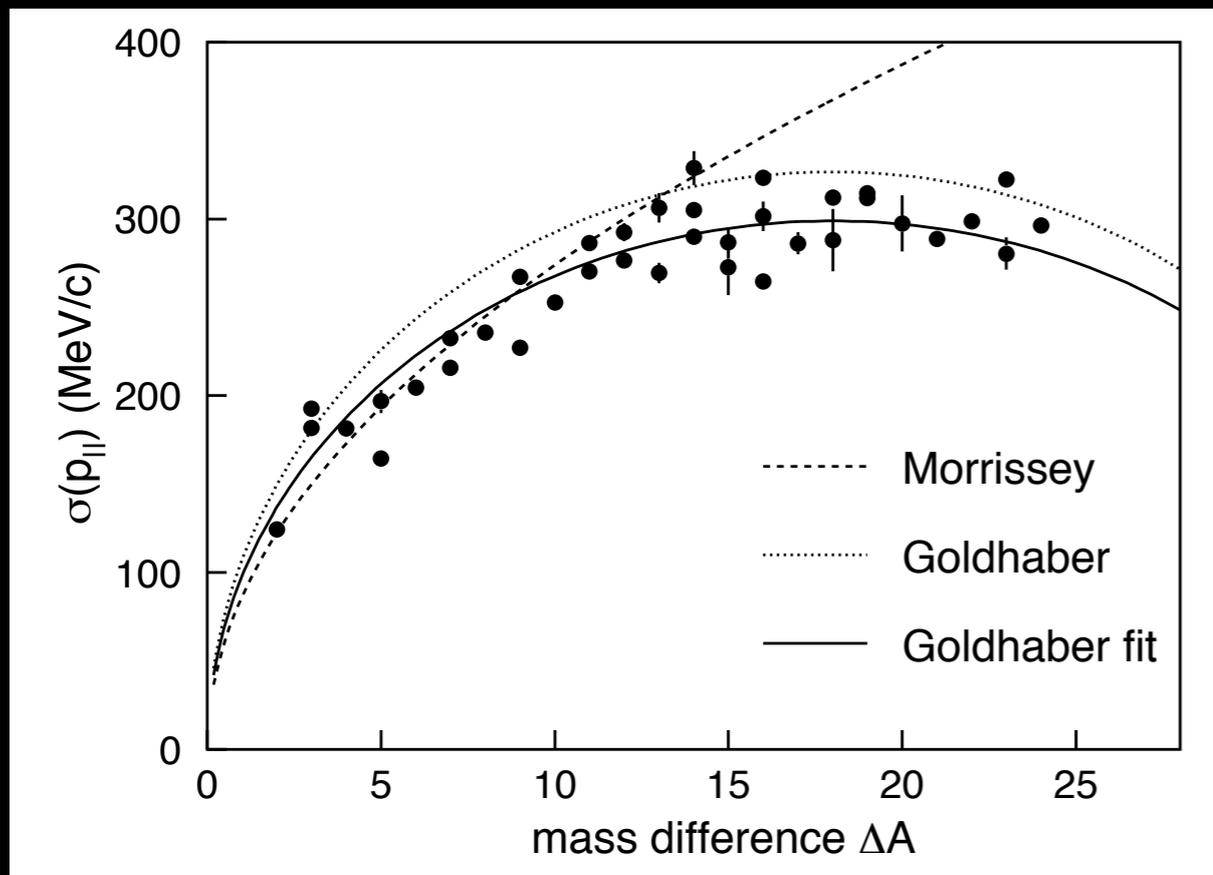
$$\sigma(P_{\text{T}}) \sim \sigma(P_{\text{L}})$$

- Small velocity shift

P dist. at $E \geq 1$ GeV/u

- Dispersion of distribution

$^{36}\text{Ar}(1.05 \text{ GeV/u}) + \text{Be}$

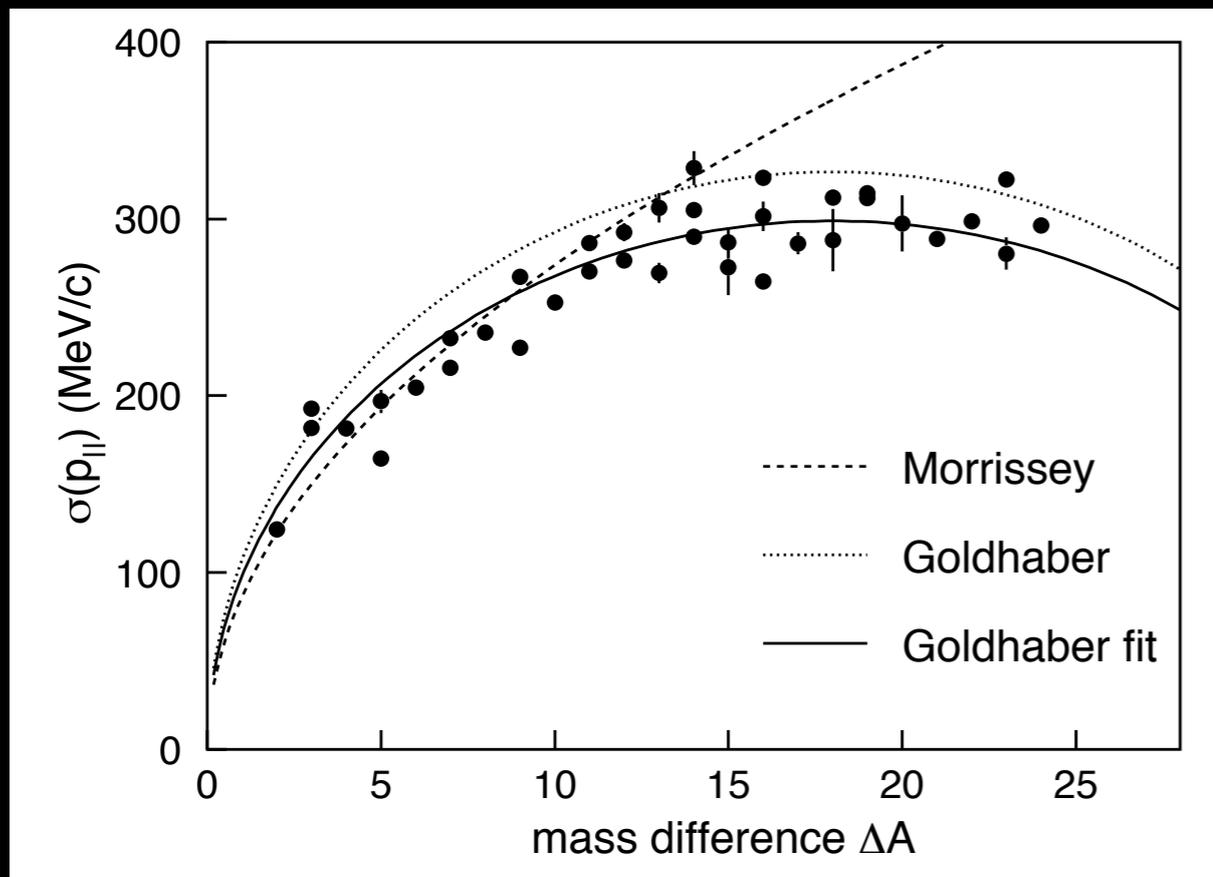


M. Caamano et al, Nucl. Phys. A 733 (2004) 187.

P dist. at $E \geq 1$ GeV/u

- Dispersion of distribution

$^{36}\text{Ar}(1.05 \text{ GeV/u}) + \text{Be}$



M. Caamano et al, Nucl. Phys. A 733 (2004) 187.

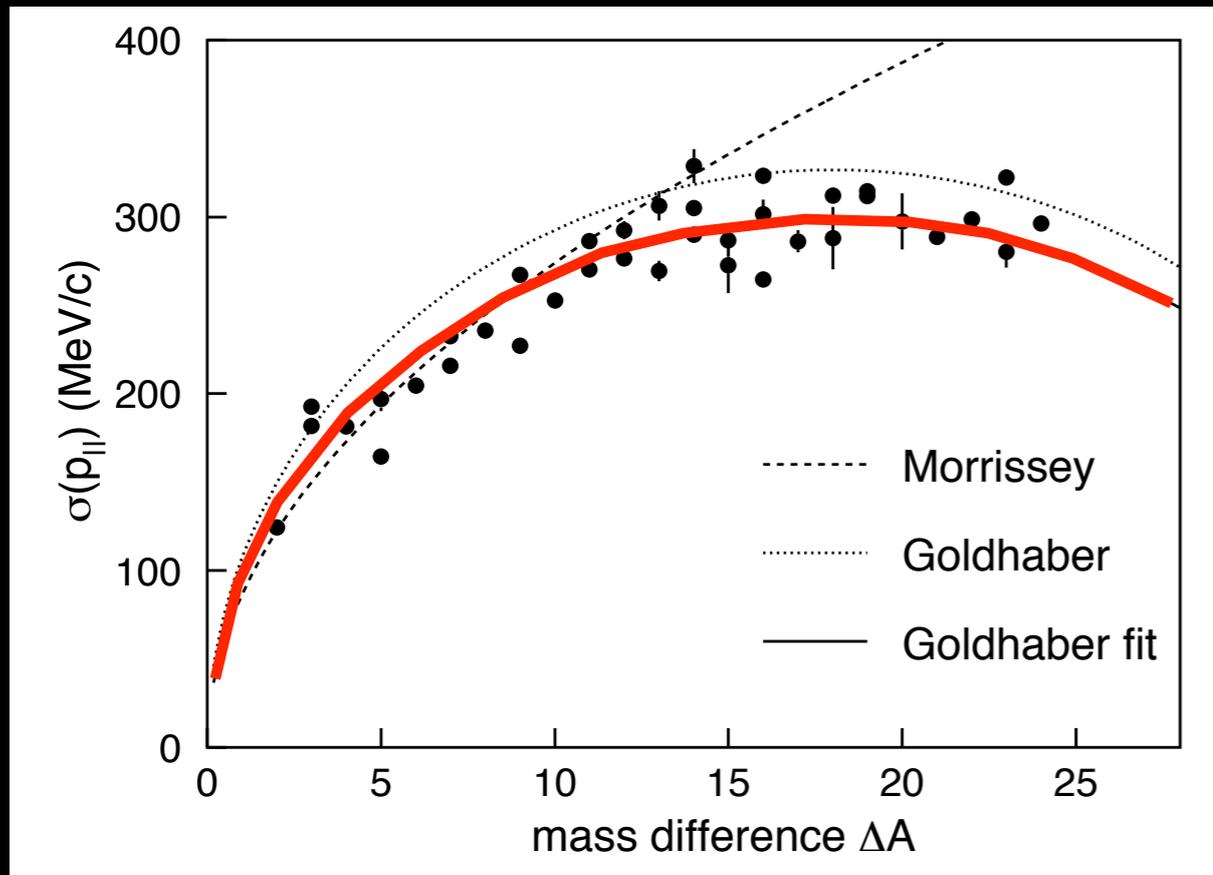
$\sigma(P_L) \leftarrow P_{\text{Fermi}}$ of removed nucleons
A.S. Goldhaber, Phys. Lett. B 53 (1974) 244.

$$\sigma_{\text{GH}} = \sigma_0 \sqrt{\frac{A_{\text{F}}(A_{\text{P}} - A_{\text{F}})}{A_{\text{P}} - 1}}$$
$$\sigma_0 \sim 100 \text{ (MeV/c)}$$

P dist. at $E \geq 1$ GeV/u

- Dispersion of distribution

$^{36}\text{Ar}(1.05 \text{ GeV/u}) + \text{Be}$



M. Caamano et al, Nucl. Phys. A 733 (2004) 187.

$$\sigma_0 = 98.2 \pm 0.2 \text{ MeV/c}$$

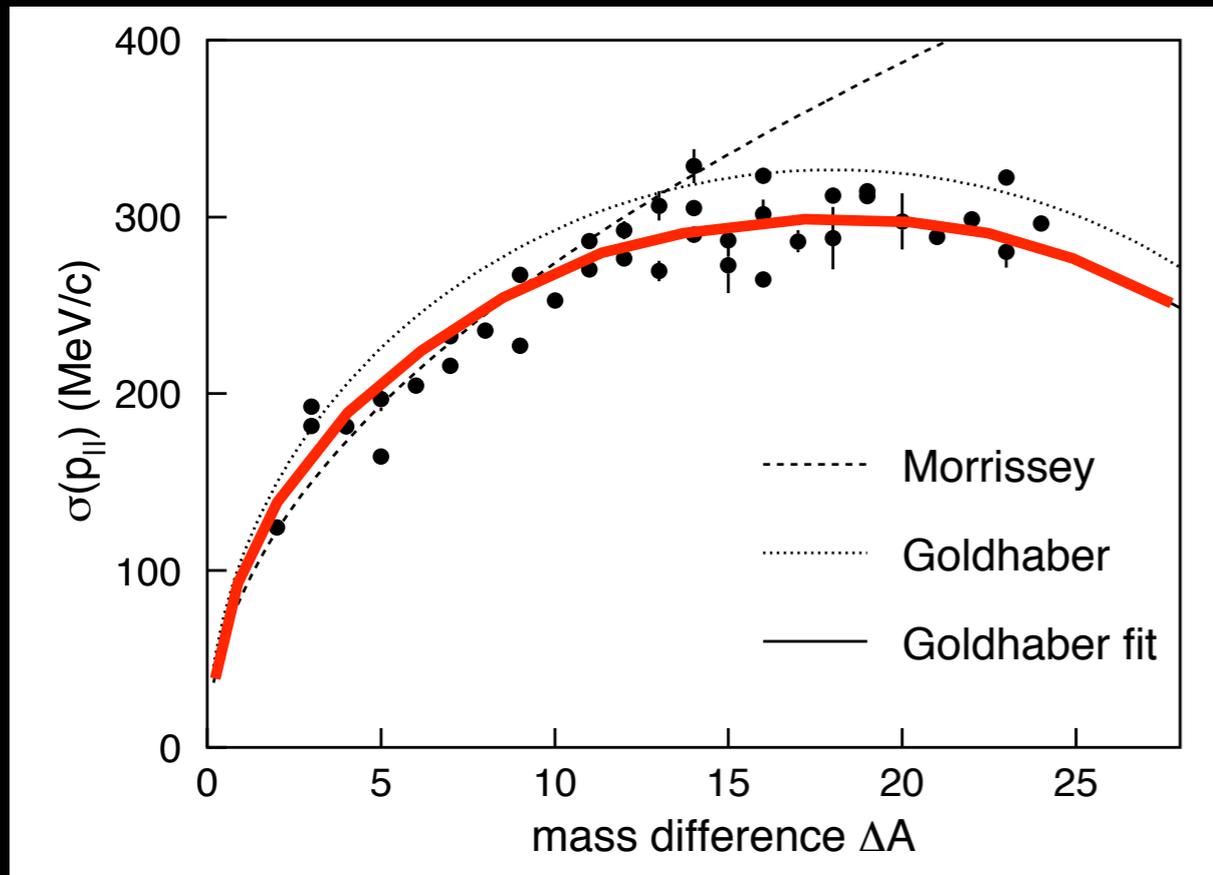
$\sigma(P_L) \leftarrow P_{\text{Fermi}}$ of removed nucleons
A.S. Goldhaber, Phys. Lett. B 53 (1974) 244.

$$\sigma_{\text{GH}} = \sigma_0 \sqrt{\frac{A_{\text{F}}(A_{\text{P}} - A_{\text{F}})}{A_{\text{P}} - 1}}$$
$$\sigma_0 \sim 100 \text{ (MeV/c)}$$

P dist. at $E \geq 1$ GeV/u

- Dispersion of distribution

$^{36}\text{Ar}(1.05 \text{ GeV/u}) + \text{Be}$



M. Caamano et al, Nucl. Phys. A 733 (2004) 187.

$$\sigma_0 = 98.2 \pm 0.2 \text{ MeV/c}$$

$\sigma(P_L) \leftarrow P_{\text{Fermi}}$ of removed nucleons
A.S. Goldhaber, Phys. Lett. B 53 (1974) 244.

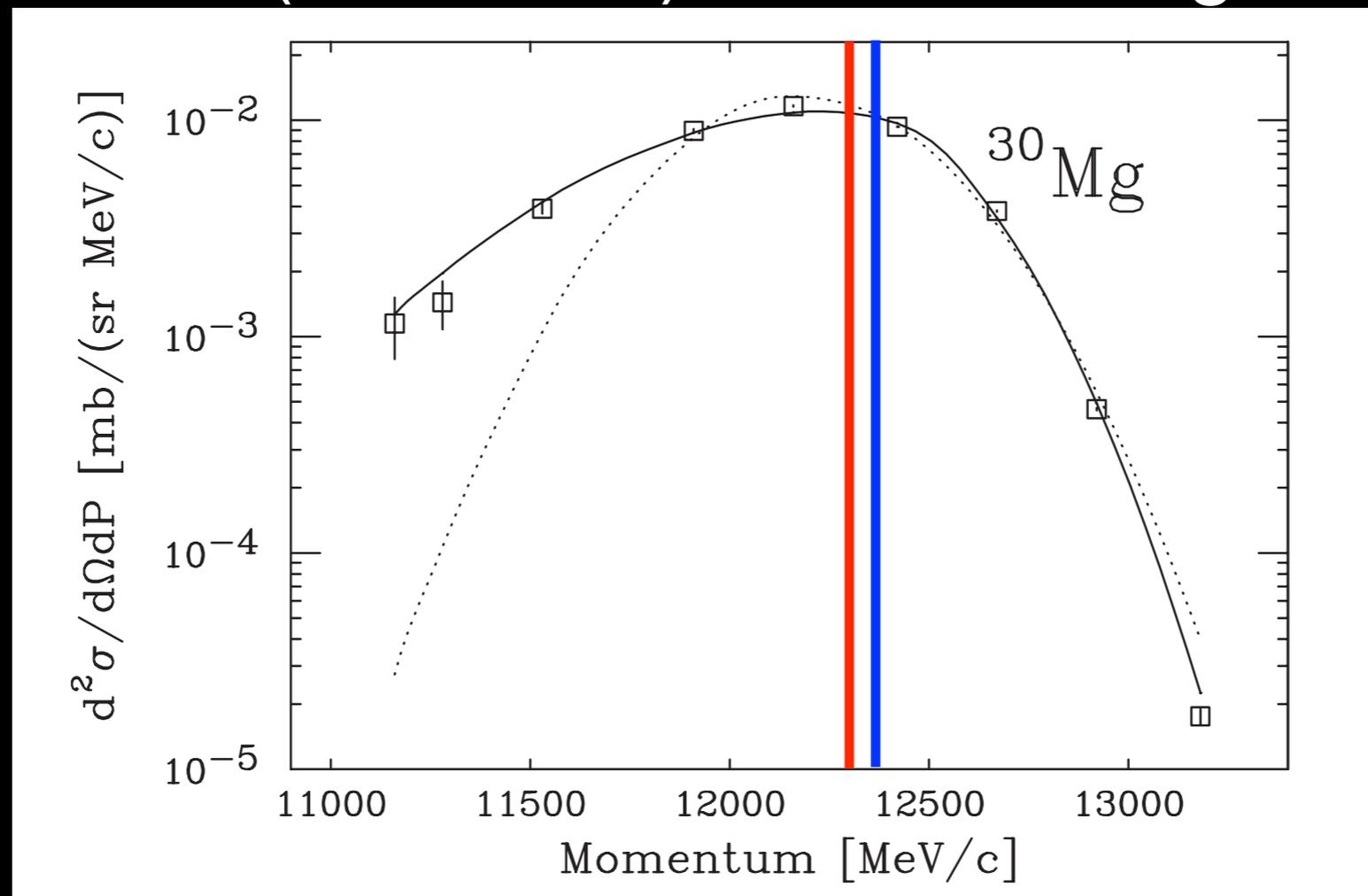
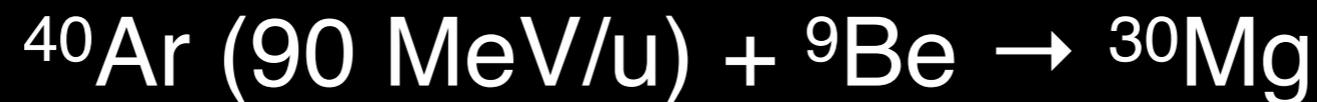
$$\sigma_{\text{GH}} = \sigma_0 \sqrt{\frac{A_F(A_P - A_F)}{A_P - 1}}$$

$$\sigma_0 \sim 100 \text{ (MeV/c)}$$

$$\sigma(P_L) \sim \sigma(P_T)$$

P_L dist. at $E \sim 100$ MeV/u

- Asymmetric longitudinal distribution

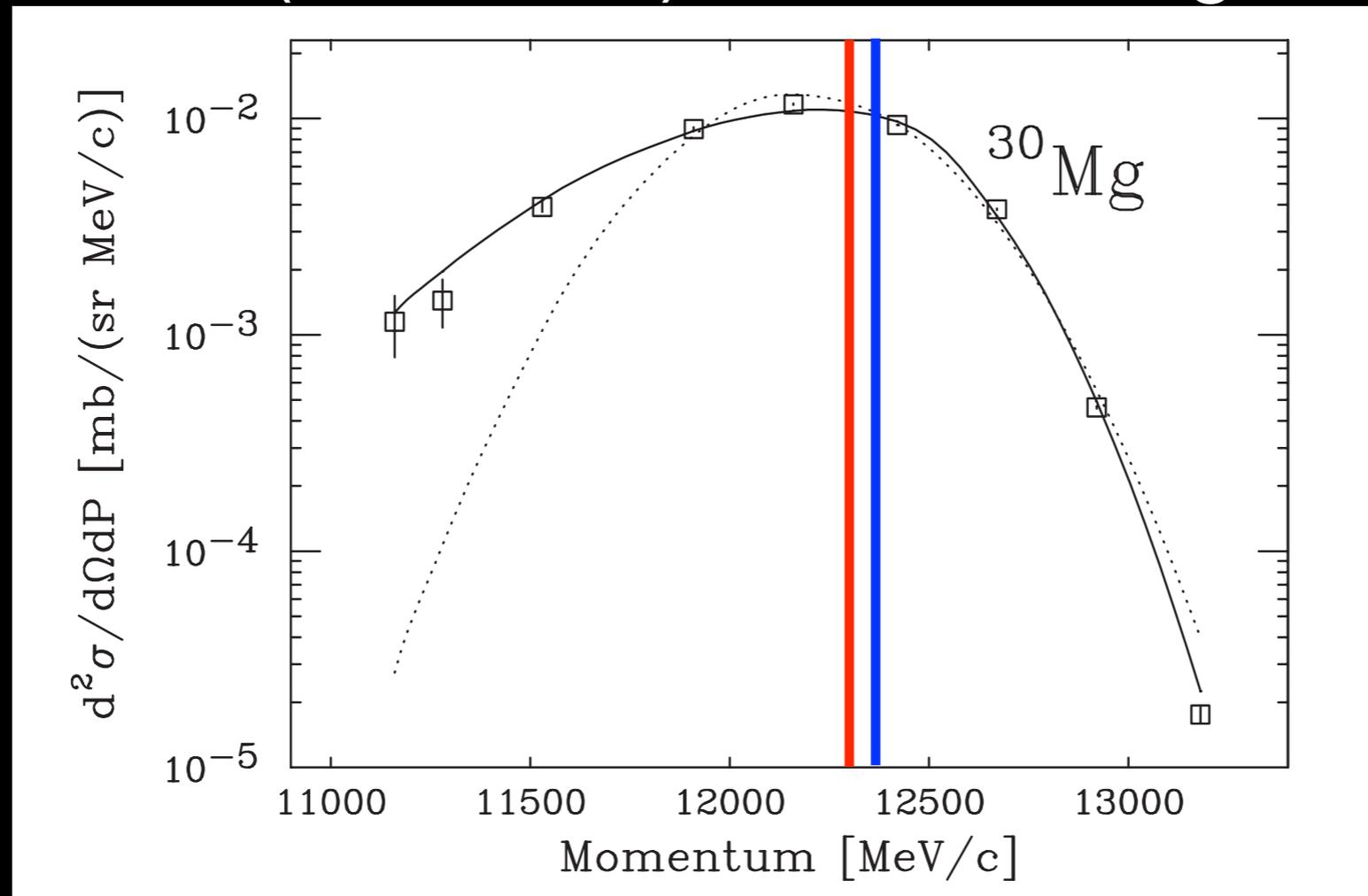
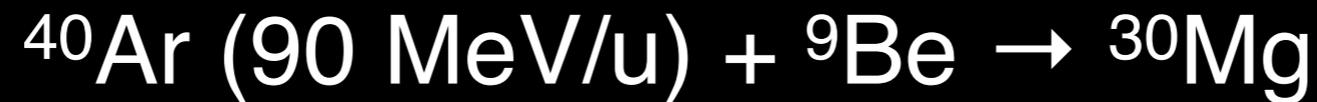


M. Notani et al., PRC 76 (2007) 044605.

$$\sigma(P_{\text{High}}) < \sigma(P_{\text{Low}})$$

P_L dist. at $E \sim 100$ MeV/u

- Asymmetric longitudinal distribution



M. Notani et al., PRC 76 (2007) 044605.

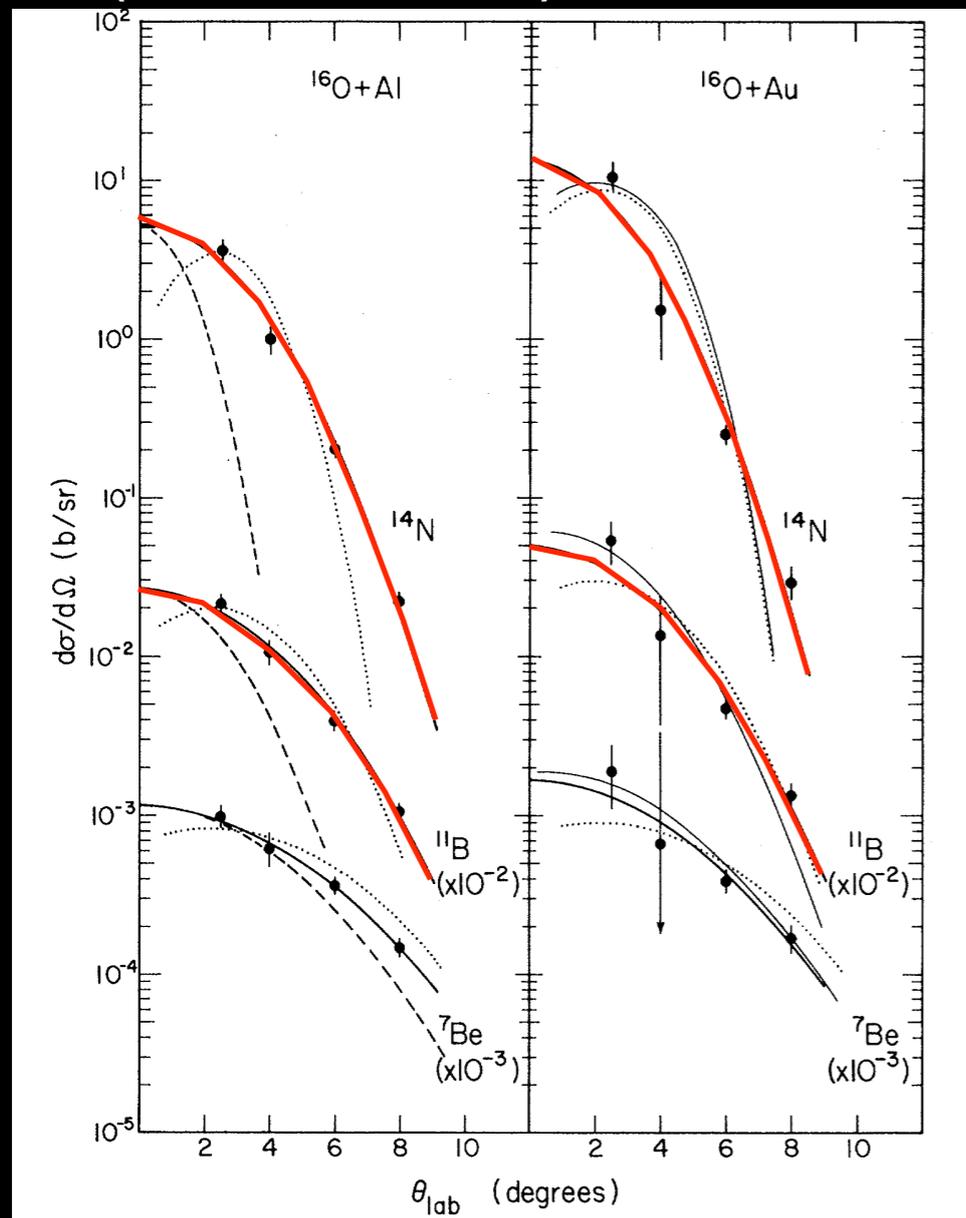
$$\sigma(P_{\text{High}}) < \sigma(P_{\text{Low}})$$

How about at $E \sim 300$ MeV/u?

P_T dist. at $E \sim 100$ MeV/u

- Additional dispersion found in P_T

^{16}O (92.5 MeV/u) + ^{27}Al , ^{197}Au



K. Van Bibber *et al.*, PRL 43 (1979) 840.

Anisotropy induced by orbital dispersion

$$\sigma(P_L) < \sigma(P_T)$$

Empirical formulation

K. Van Bibber *et al.*, Phys. Rev. Lett. 43 (1979) 840.

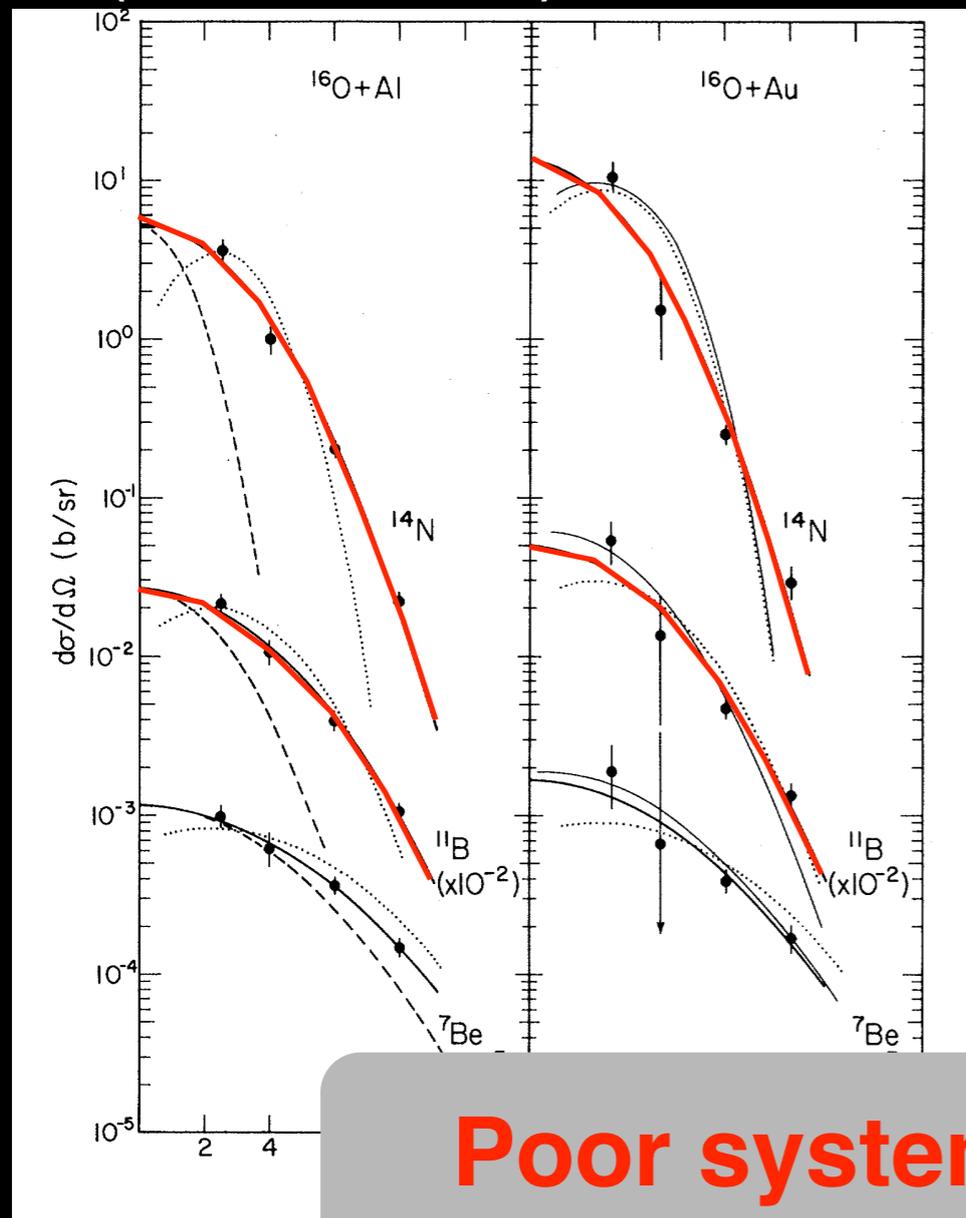
$$\sigma(P_{\perp}) = \sqrt{\sigma(P_{\parallel})^2 + \frac{A_F(A_F - 1)}{A_P(A_P - 1)} \sigma_{D0}^2}$$

$$\sigma_0 = 195 \text{ (MeV/c)}$$

P_T dist. at $E \sim 100$ MeV/u

- Additional dispersion found in P_T

^{16}O (92.5 MeV/u) + ^{27}Al , ^{197}Au



Anisotropy induced by orbital dispersion

$$\sigma(P_L) < \sigma(P_T)$$

Empirical formulation

K. Van Bibber et al., Phys. Rev. Lett. 43 (1979) 840.

$$\sigma(P_{\perp}) = \sqrt{\sigma(P_{\parallel})^2 + \frac{A_F(A_F - 1)}{A_P(A_P - 1)} \sigma_{D0}^2}$$

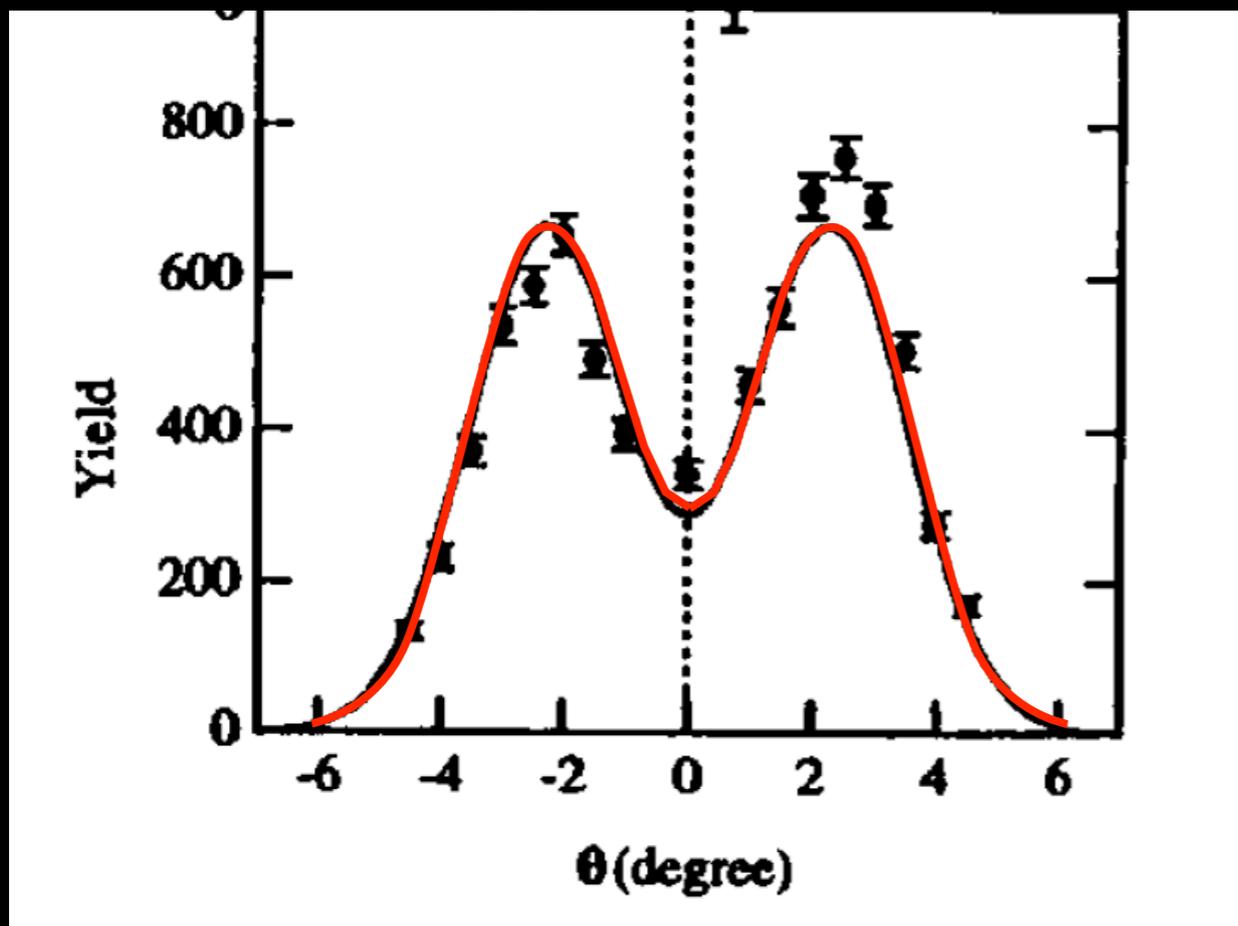
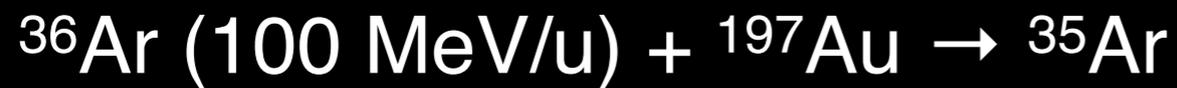
$$\sigma_0 = 195 \text{ (MeV/c)}$$

Poor systematic measurements

K. Van Bibber et al., PRL 43 (1979) 840.

P_T dist. at $E \sim 100$ MeV/u

- Orbital deflection in case of heavy target



Off-centered distribution

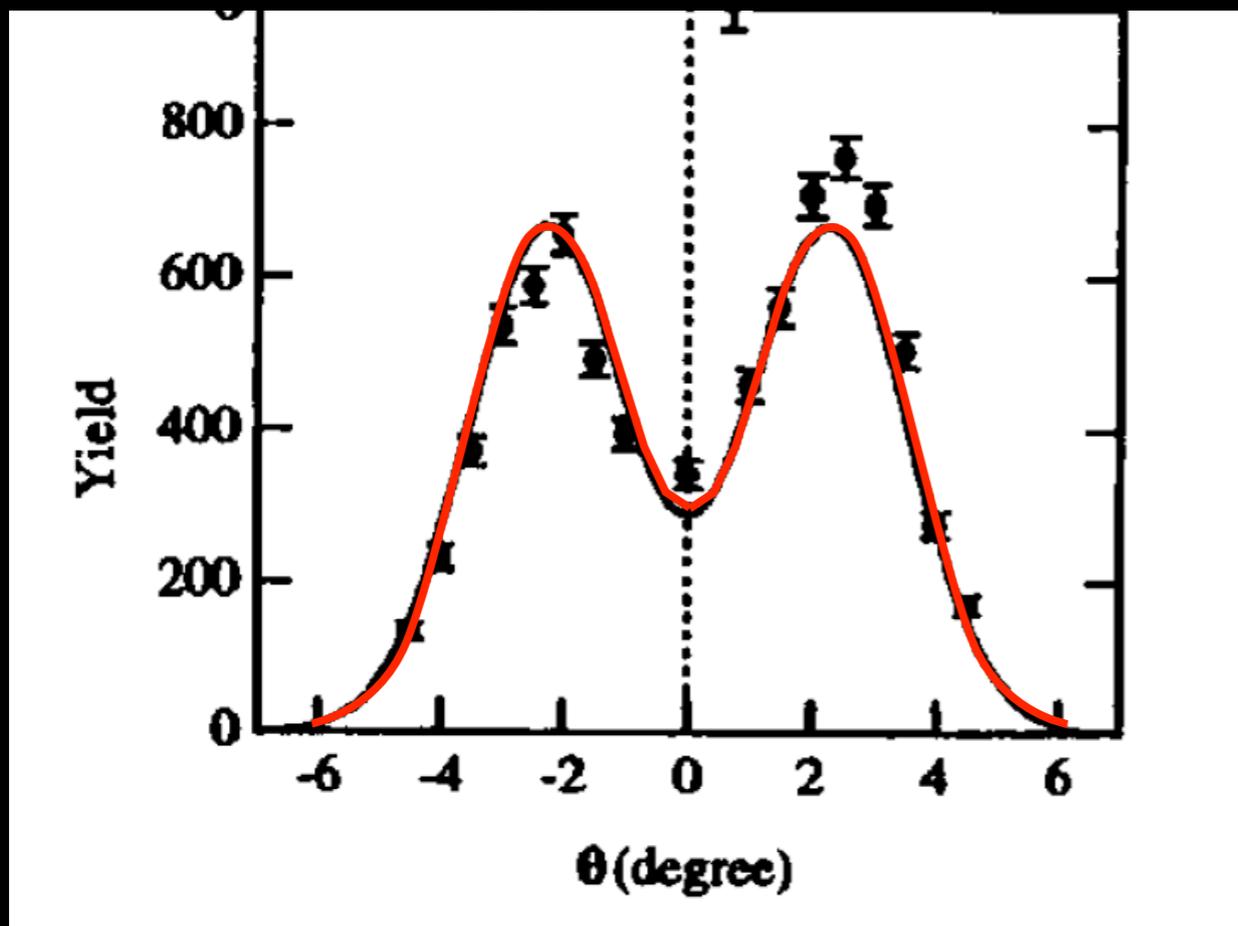
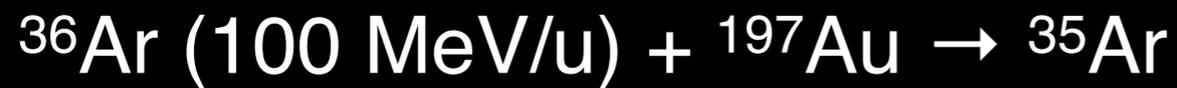


Orbital deflection caused
by Coulomb repulsion

K. Matsuta et al., NP A701 (2002) 383c.

P_T dist. at $E \sim 100$ MeV/u

- Orbital deflection in case of heavy target



K. Matsuta et al., NP A701 (2002) 383c.

Off-centered distribution



Orbital deflection caused
by Coulomb repulsion

Target, E dependence

Evaluation of $\sigma_{\text{Prod.}}$

- Theoretical calculation

ex. A) ABRABLA : abrasion-ablation model

J.J. Gaimard et al., Nucl. Phys. A 531 (1991) 709.

B) QMD, AMD

Time consuming, ambiguity of model

- Empirical formulation

ex. EPAX : Based on high-E spallation

K. Sümmerer et al., Phys. Rev. C 61 (2000) 034607.

Simple and good for rough estimation

Evaluation of $\sigma_{\text{Prod.}}$

- Theoretical calculation

ex. A) ABRABLA : abrasion-ablation model

J.J. Gaimard et al., Nucl. Phys. A 531 (1991) 709.

B) QMD, AMD

Time consuming, ambiguity of model

- Empirical formulation

ex. EPAX : Based on high-E spallation

K. Sümmerer et al., Phys. Rev. C 61 (2000) 034607.

Simple and good for rough estimation

E, target dependence

Contribution of nucl. structure

Experimental setup

- **HIMAC@NIRS** 290 MeV/u
- RRC@RIKEN 90, 95 MeV/u

Experiments

- RIKEN & NIRS

- RRC+RIPS

S. Momota et al., Nucl. Phys. A746, 407c (2004).

M. Notani et al., Phys. Rev. C 76, 044605 (2007).

P_L dist. (Machine study)

Beam : ^{40}Ar @90 MeV/u

Target : ^9Be

P_T dist. (r280n)

Beam : ^{40}Ar @95 MeV/u

Target : ^9Be

- HIMAC+SB2

S. Momota et al., Eur. Phys. J. Special Topics 150, 315–316 (2007).

S. Momota et al., to be published in J. of Korean Phys. Soc.

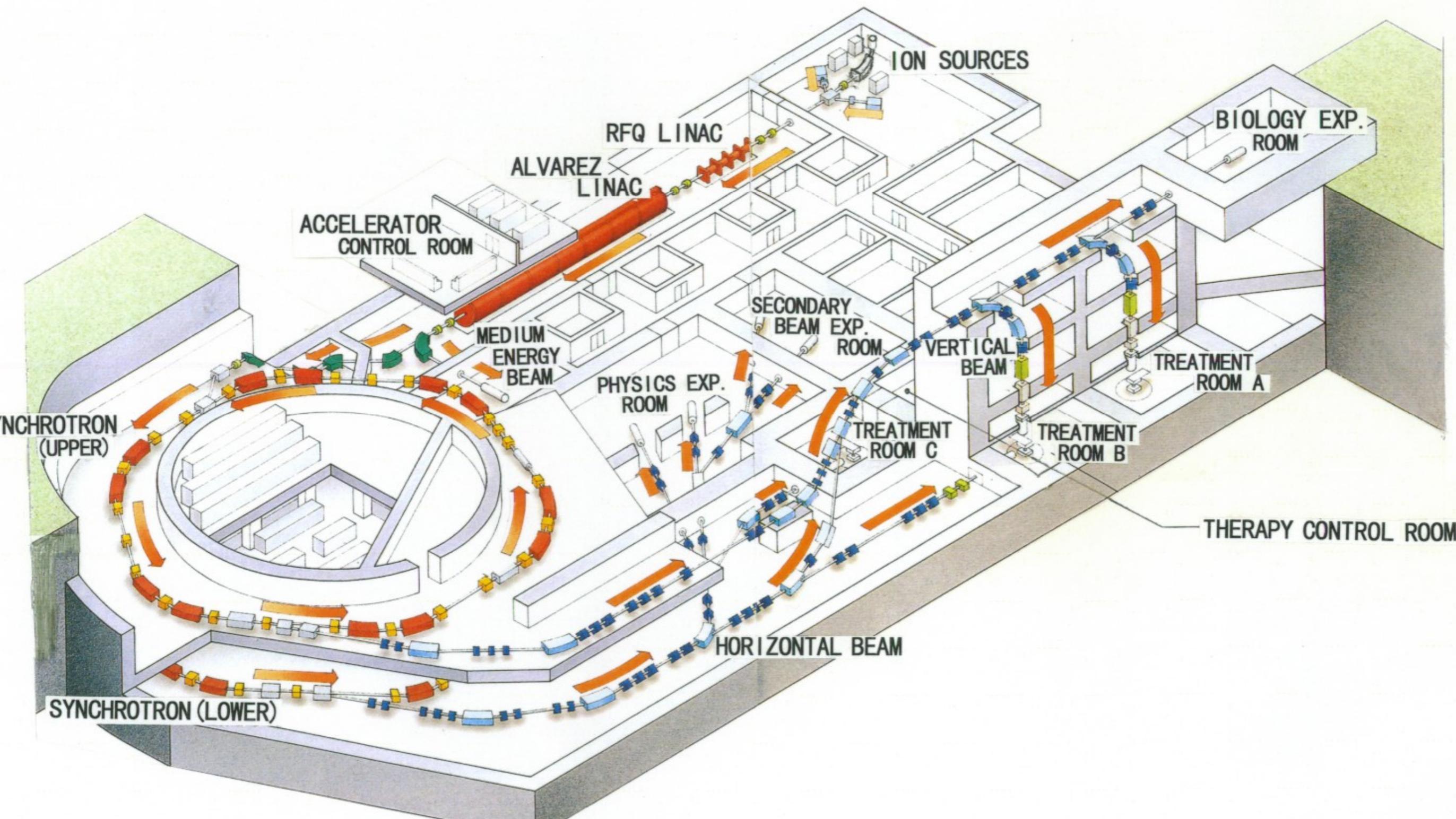
P_L dist., P_L dist. (P078, P178)

Beam : ^{40}Ar , ^{84}Kr @290 MeV/u

Target : ^{12}C , ^{27}Al , ^{93}Nb , ^{159}Tb , ^{197}Au

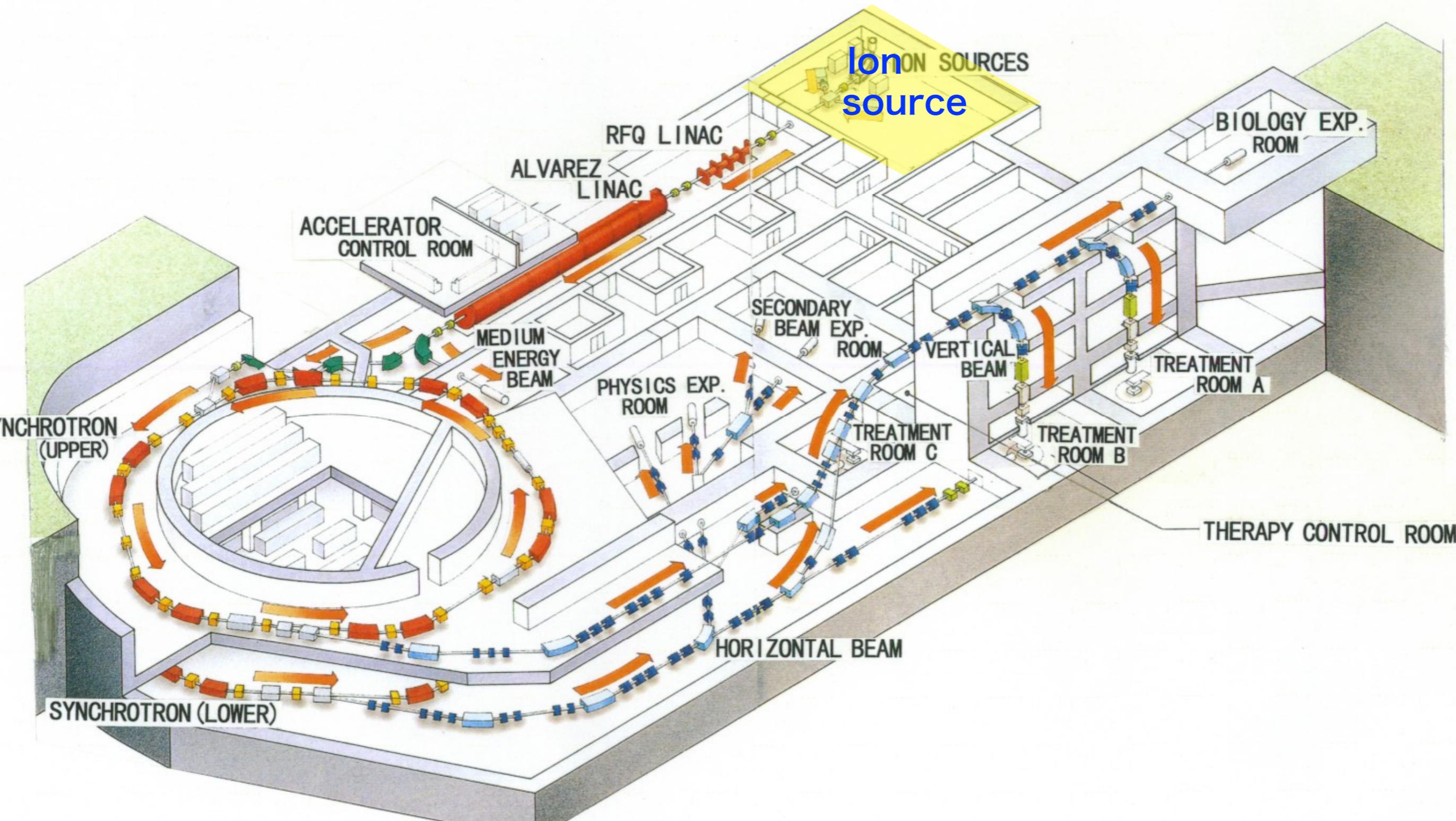
HIMAC facility at NIRS

- dedicated for cancer therapy



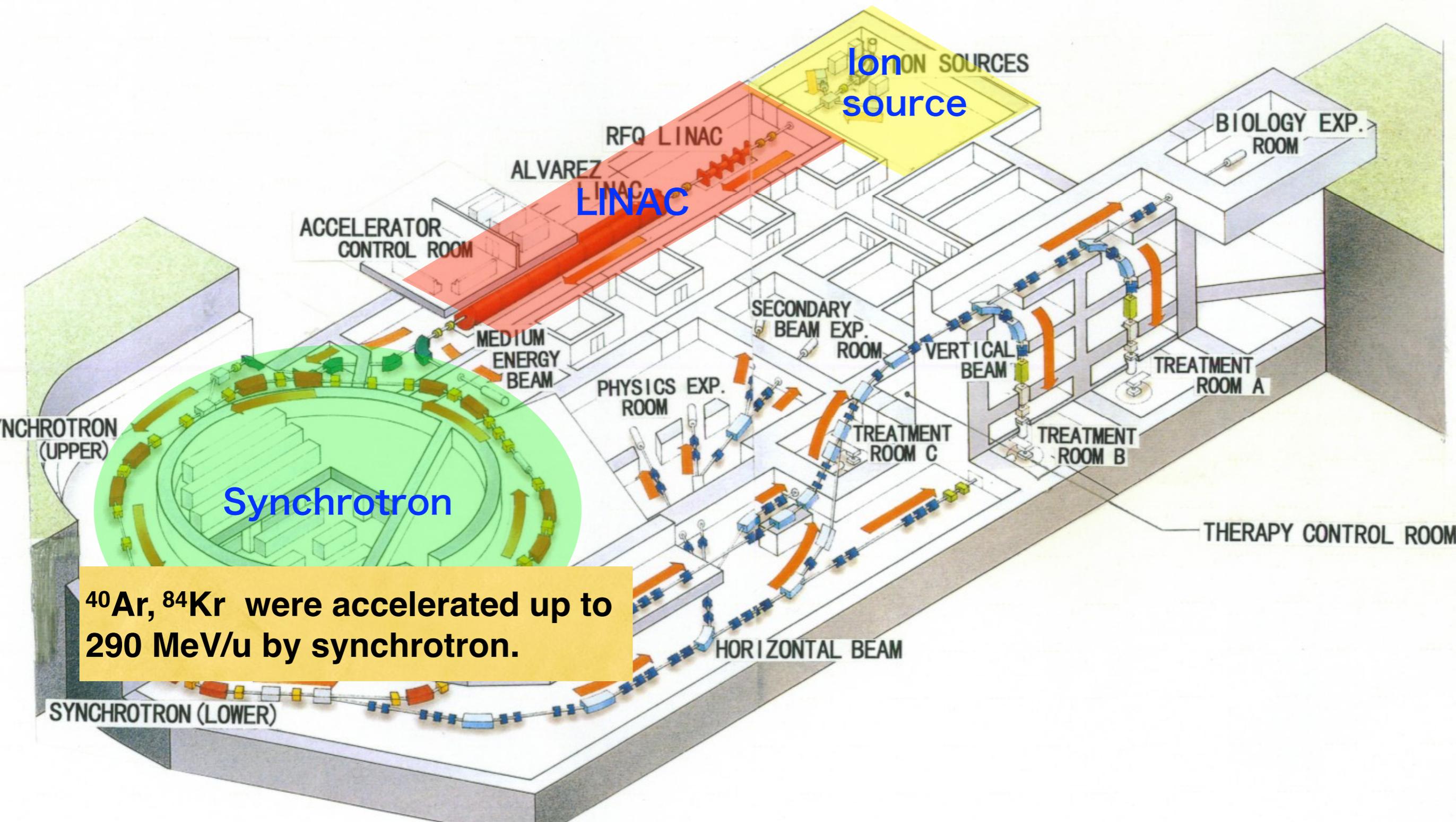
HIMAC facility at NIRS

- dedicated for cancer therapy



HIMAC facility at NIRS

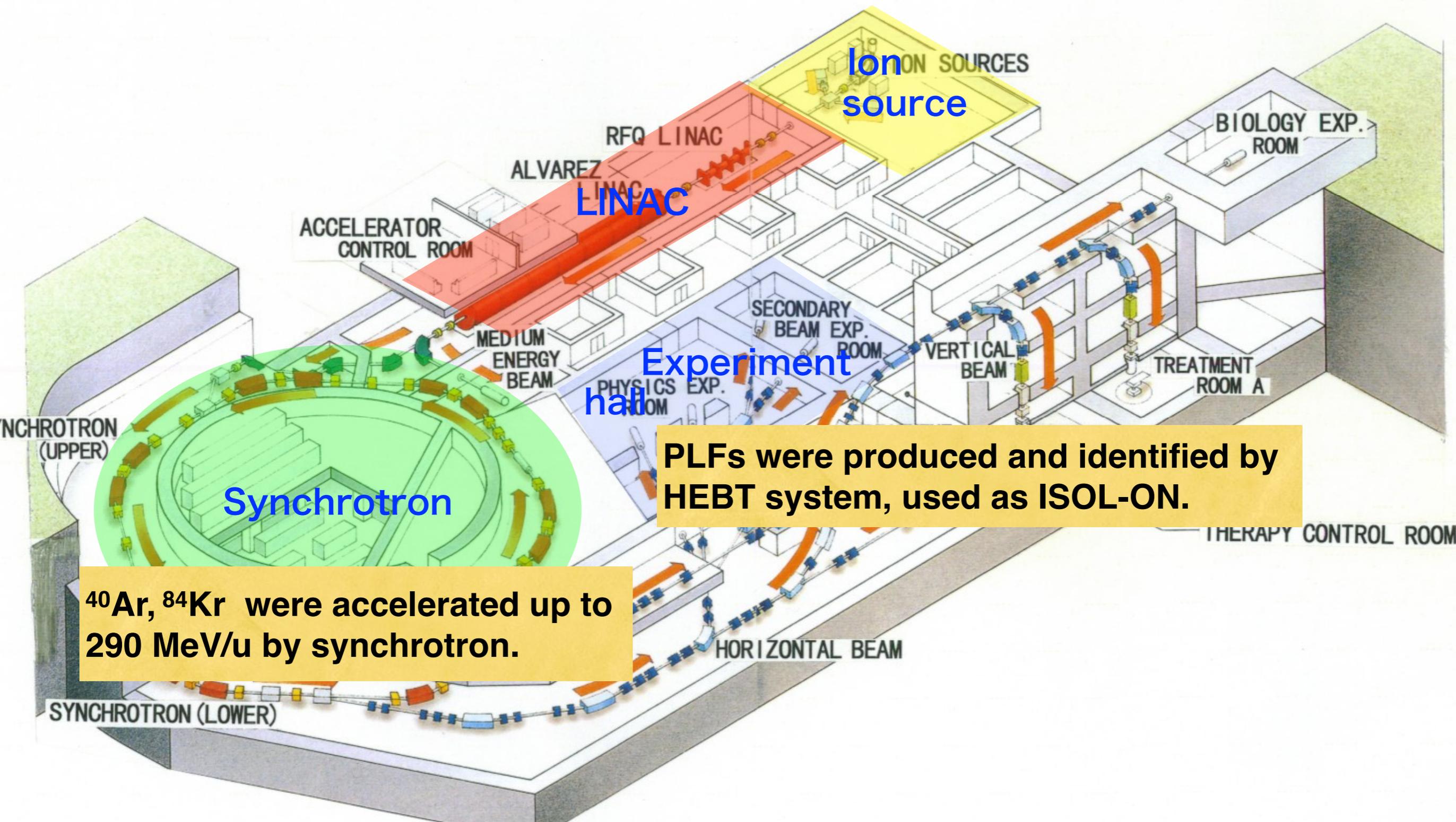
- dedicated for cancer therapy



^{40}Ar , ^{84}Kr were accelerated up to 290 MeV/u by synchrotron.

HIMAC facility at NIRS

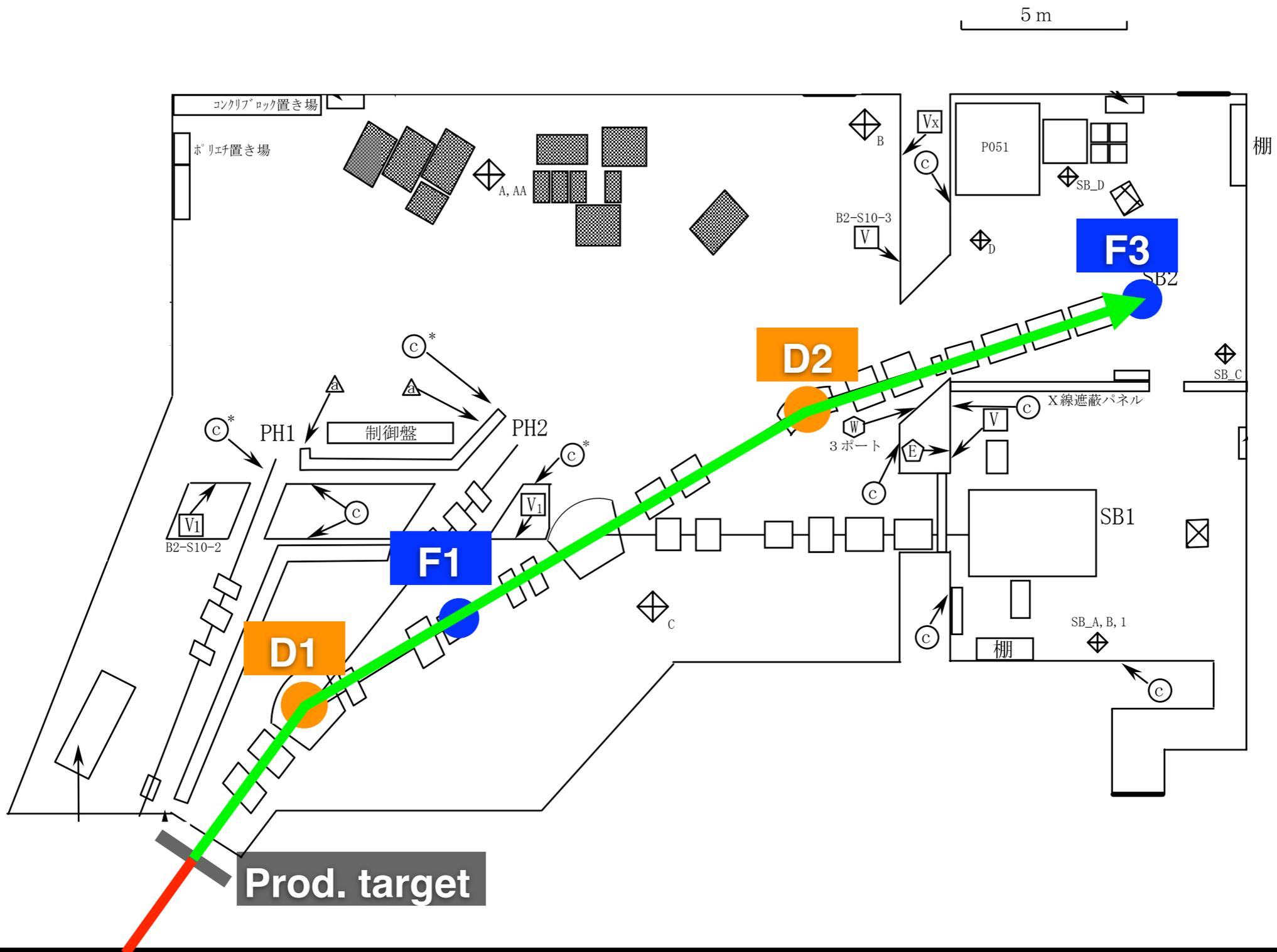
- dedicated for cancer therapy



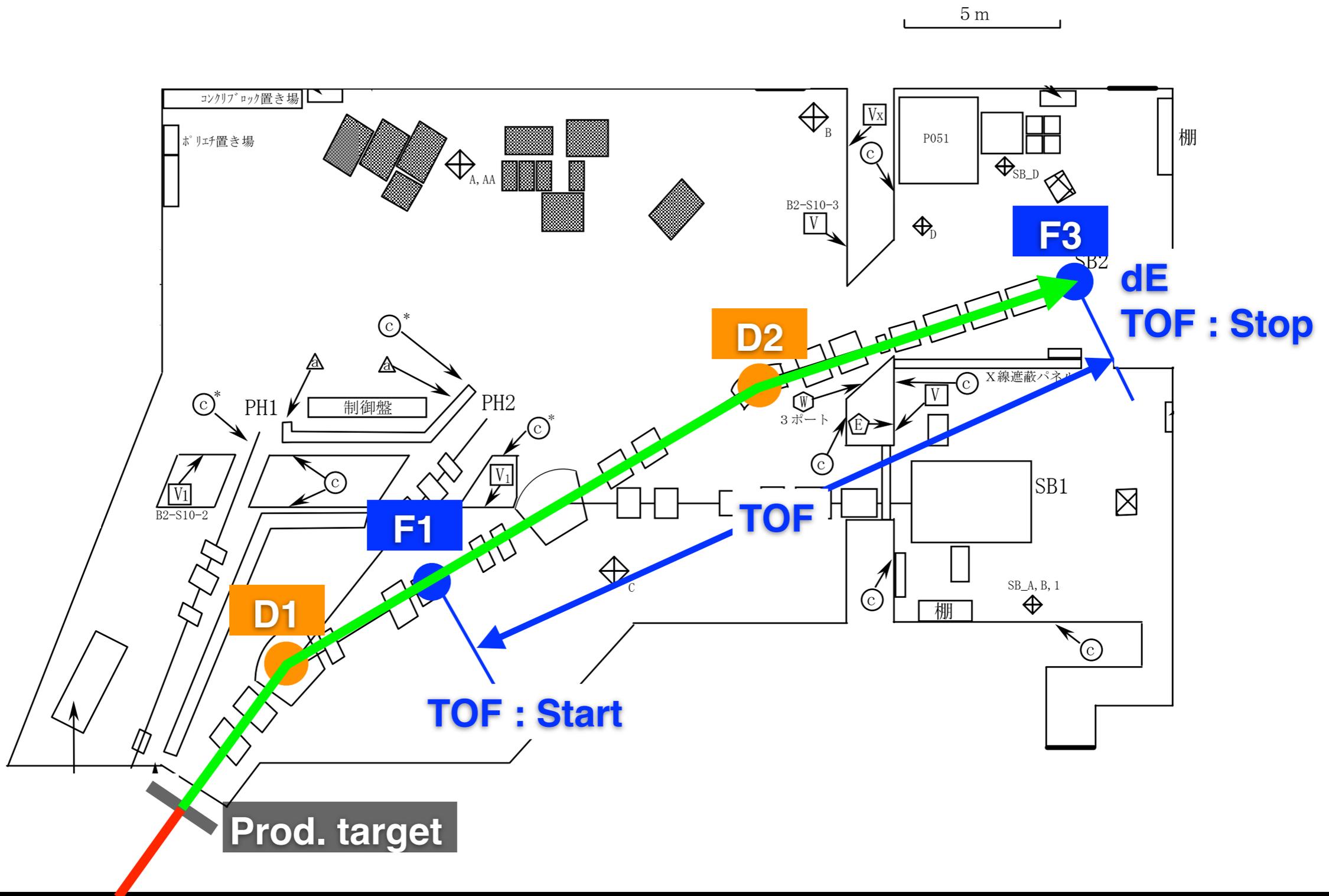
PLFs were produced and identified by HEBT system, used as ISOL-ON.

^{40}Ar , ^{84}Kr were accelerated up to 290 MeV/u by synchrotron.

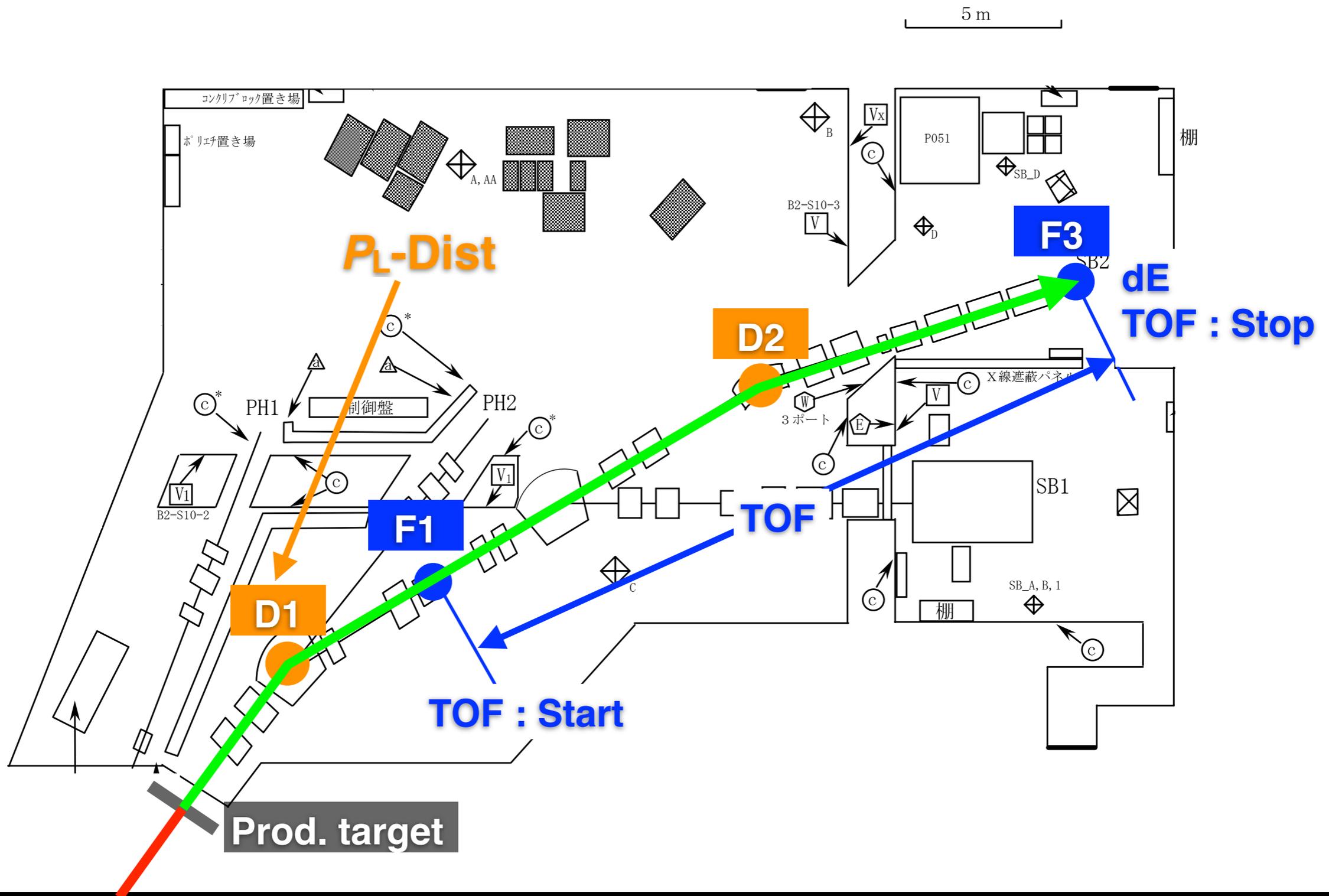
Fragment separator



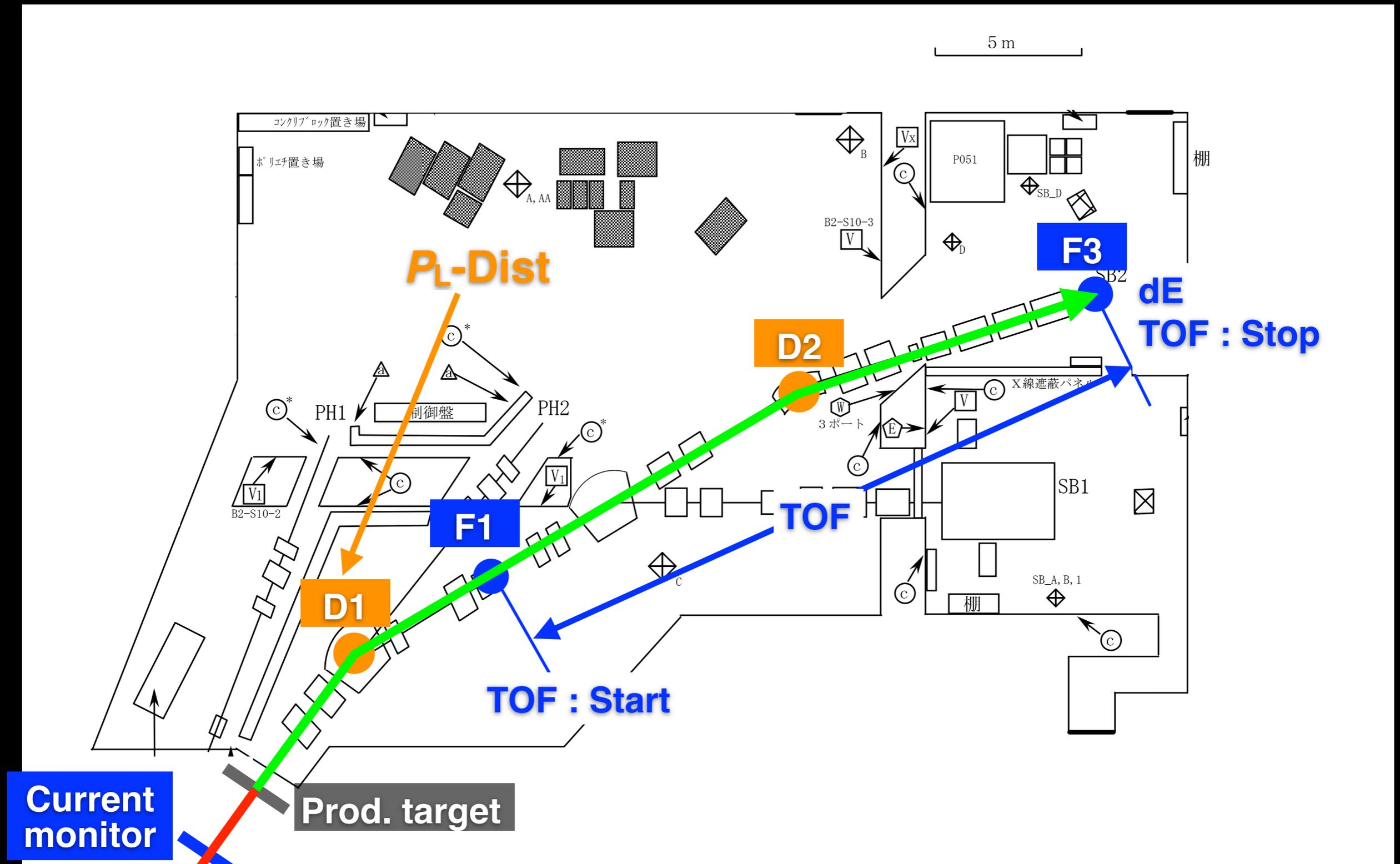
Fragment separator



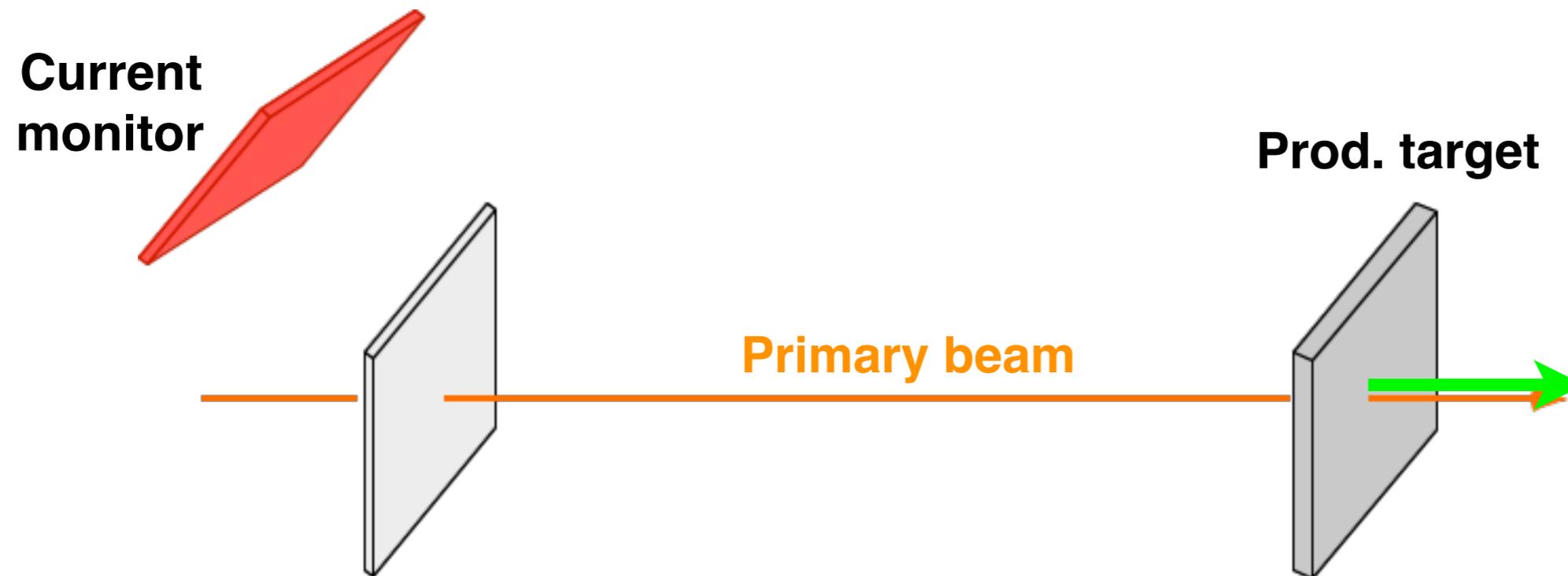
Fragment separator



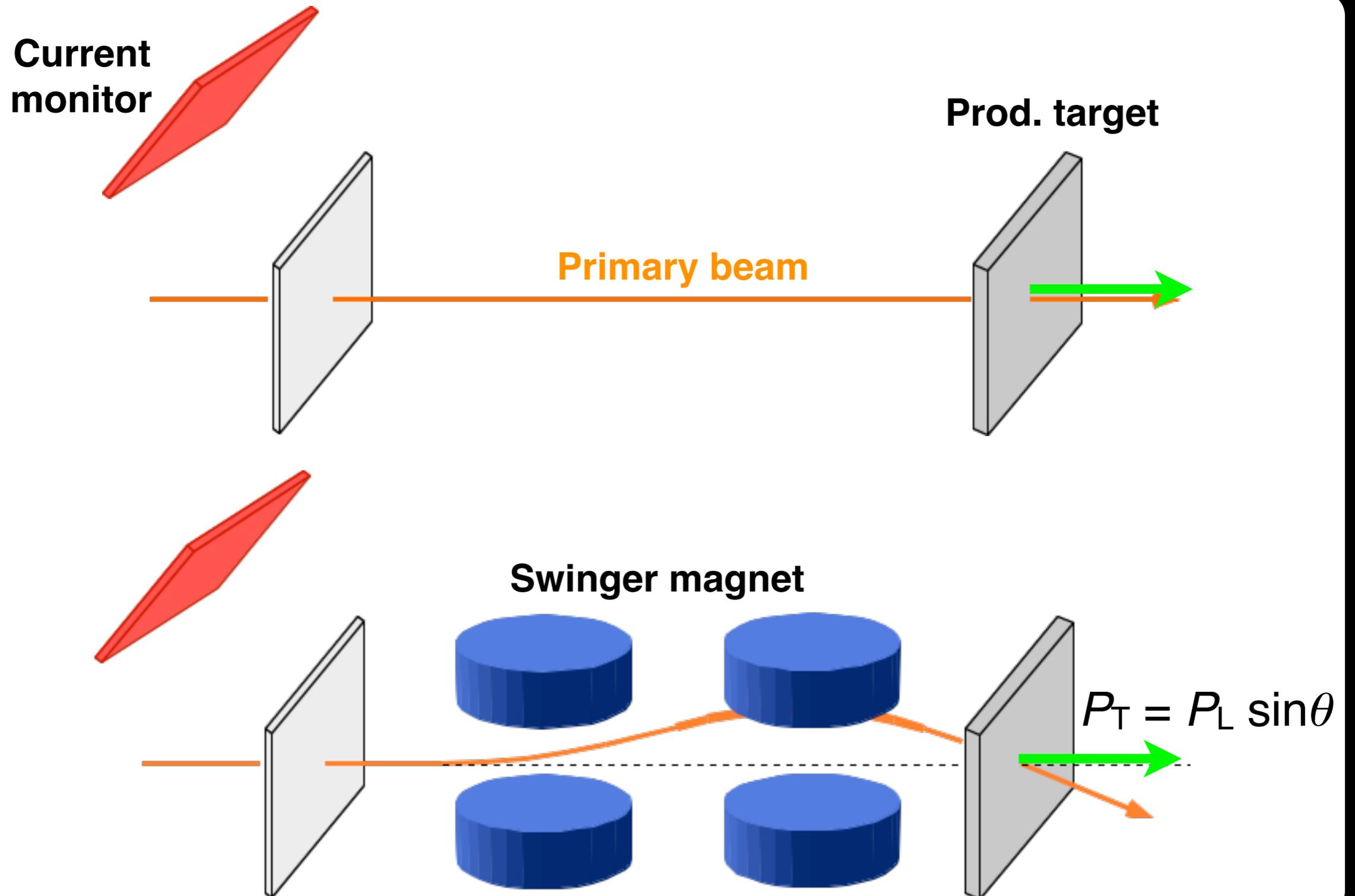
Fragment separator



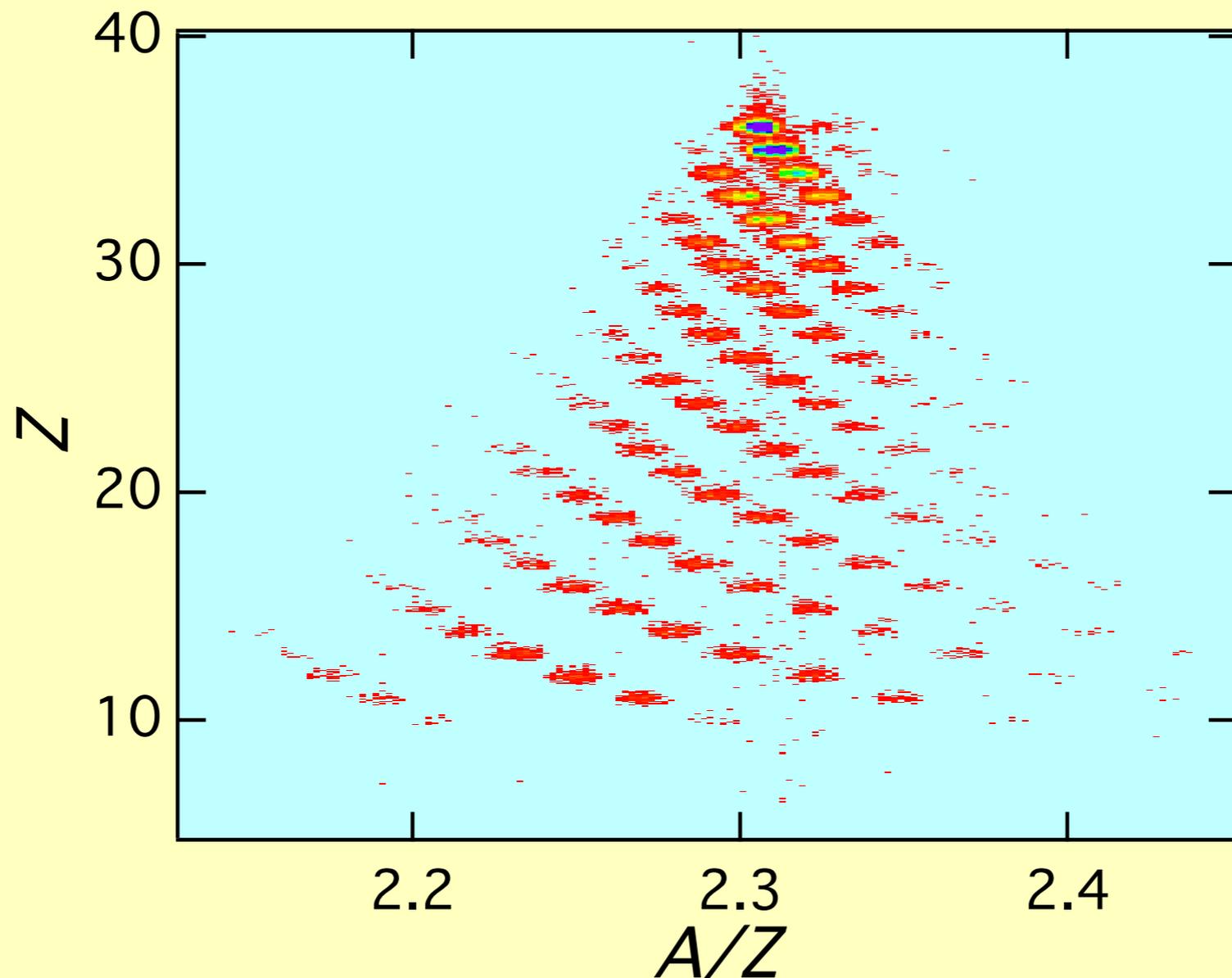
Angular (P_T) distribution



Angular (P_T) distribution



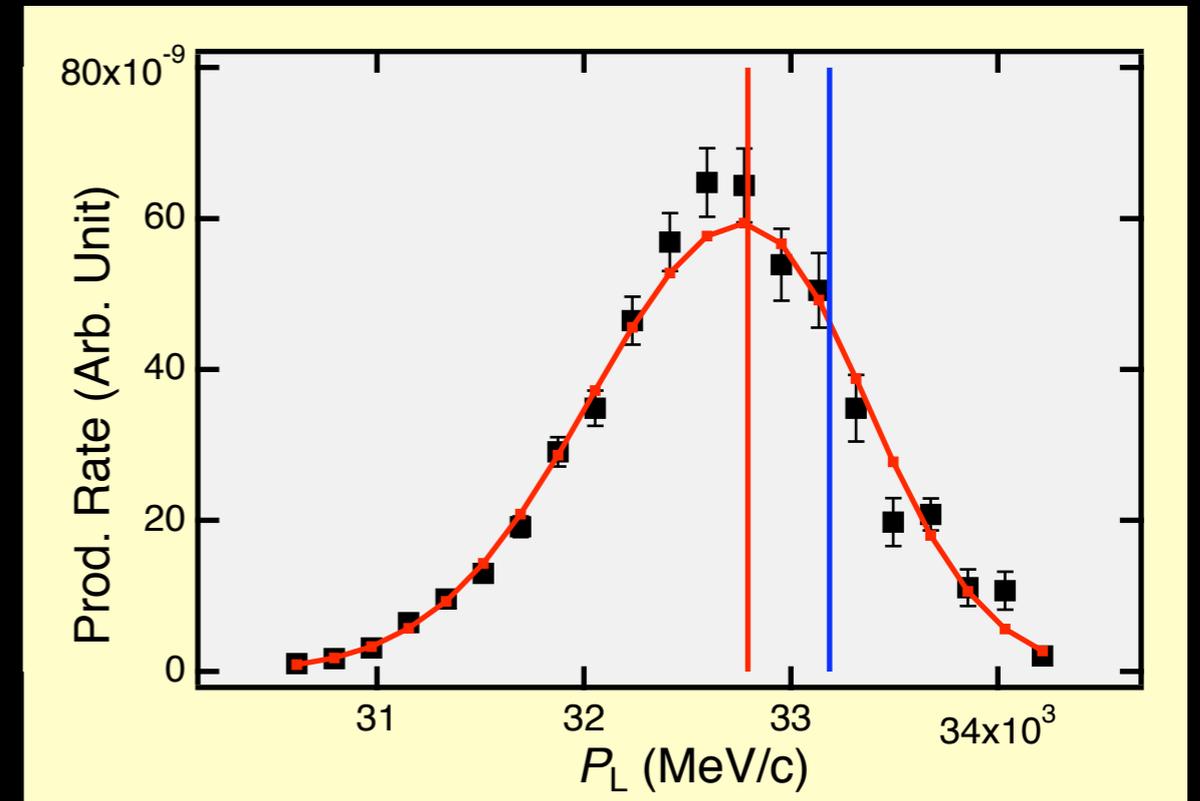
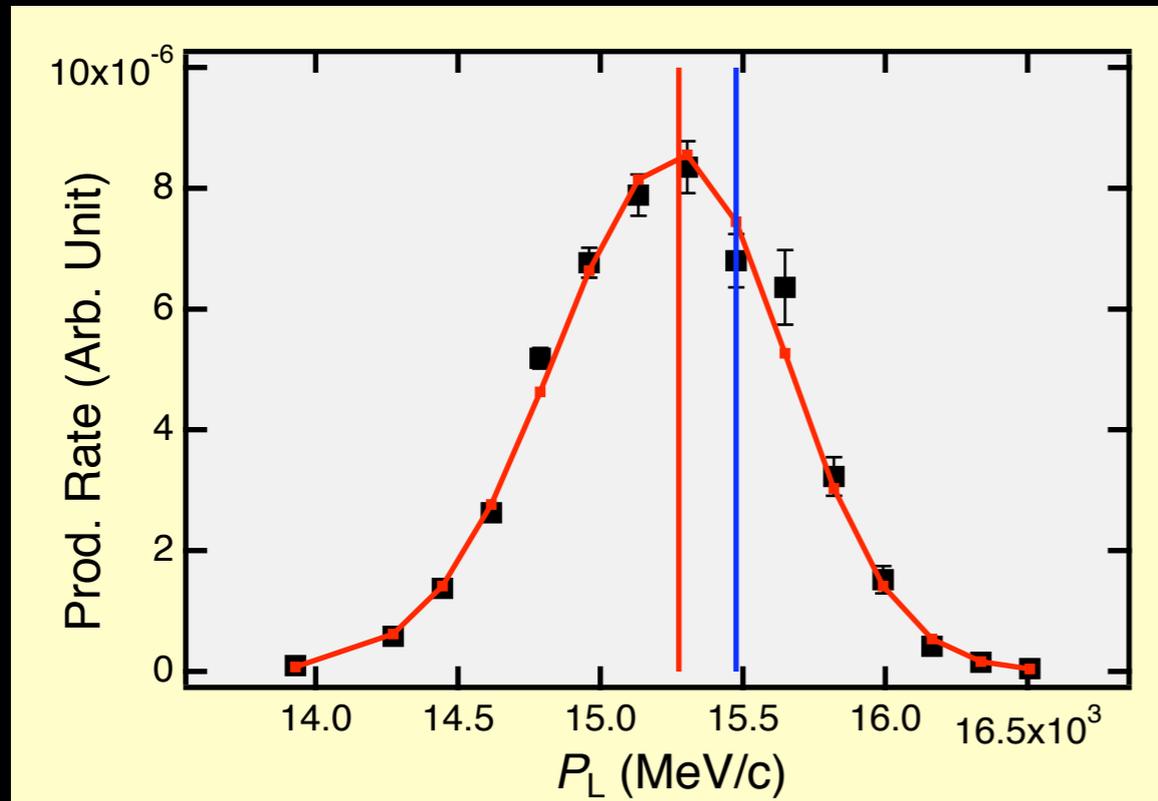
Particle identification



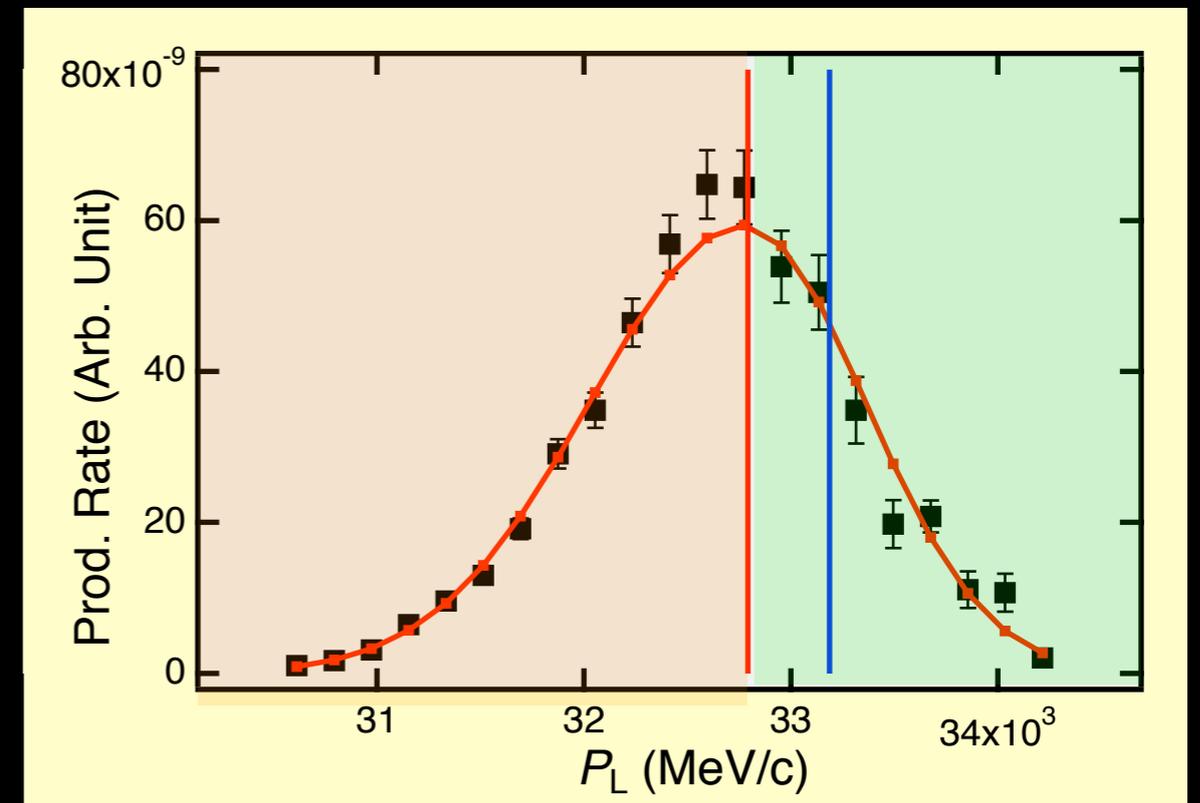
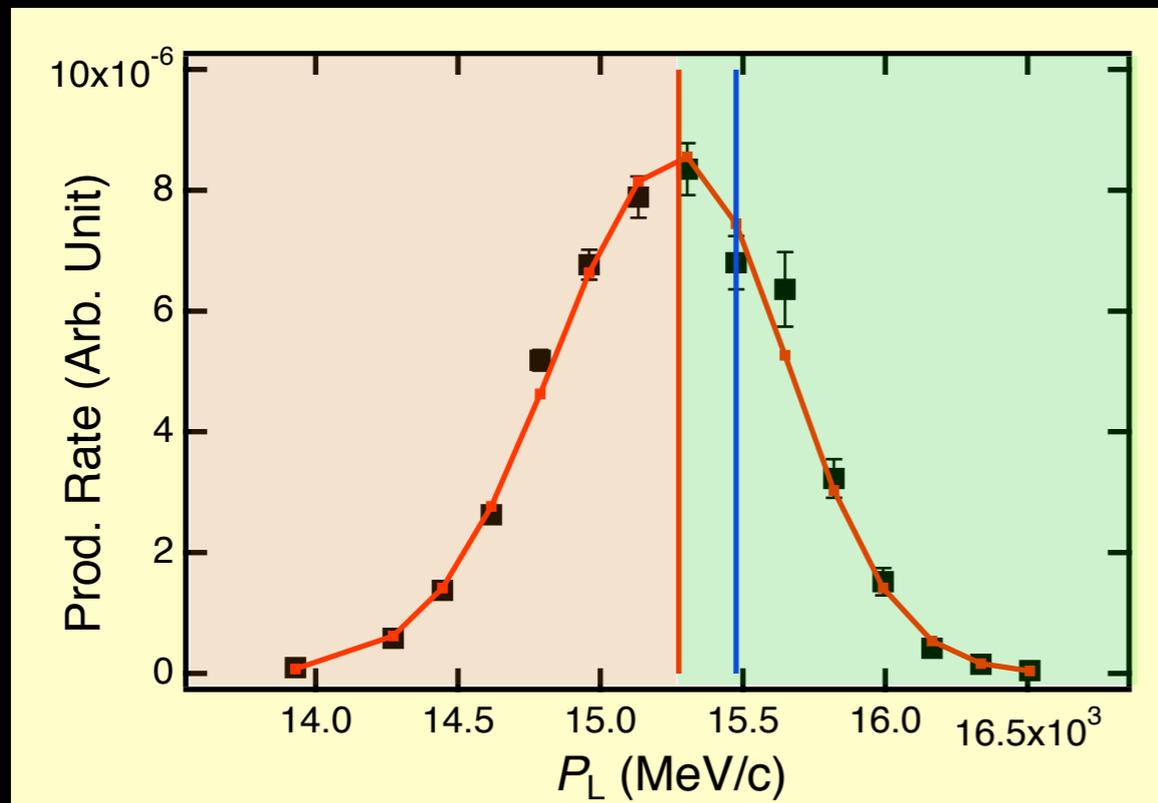
$B\rho=99.0 \pm 0.25\%$, $\theta = 16 \pm 4$ mrad

P_L distribution

Analysis of P_L distributions

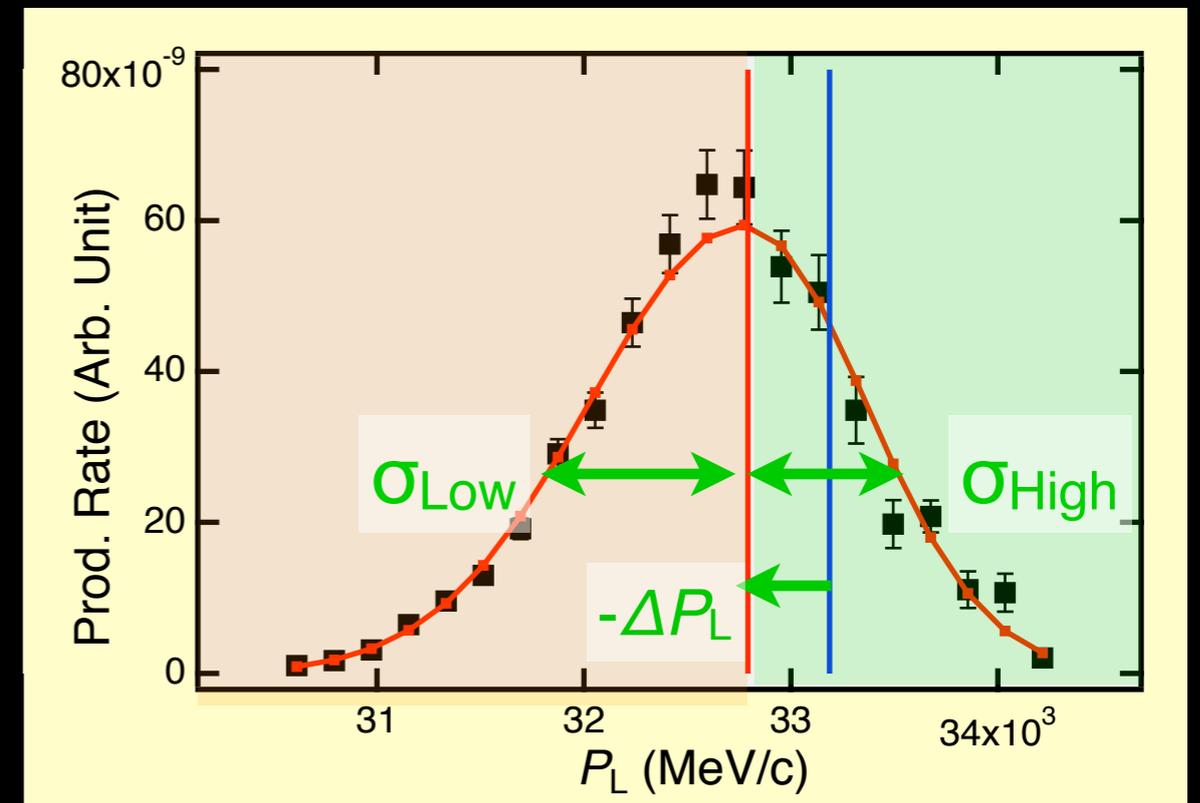
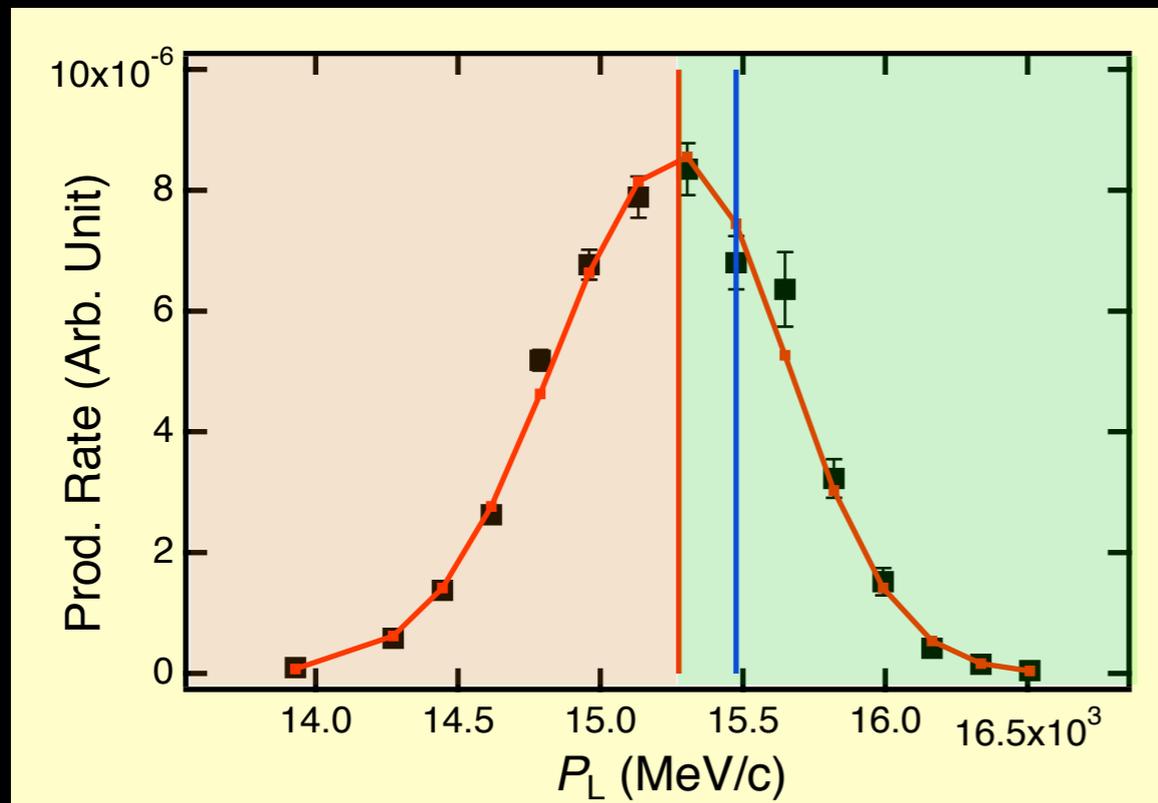


Analysis of P_L distributions



$$Y(P_L) = A \exp\left(-\frac{(P_L - P_0)^2}{2\sigma(P_L)^2}\right) \begin{cases} \sigma(P_L) = \sigma_{\text{Low}} & \text{if } P_L < P_0 \\ \sigma(P_L) = \sigma_{\text{High}} & \text{if } P_L > P_0 \end{cases}$$

Analysis of P_L distributions

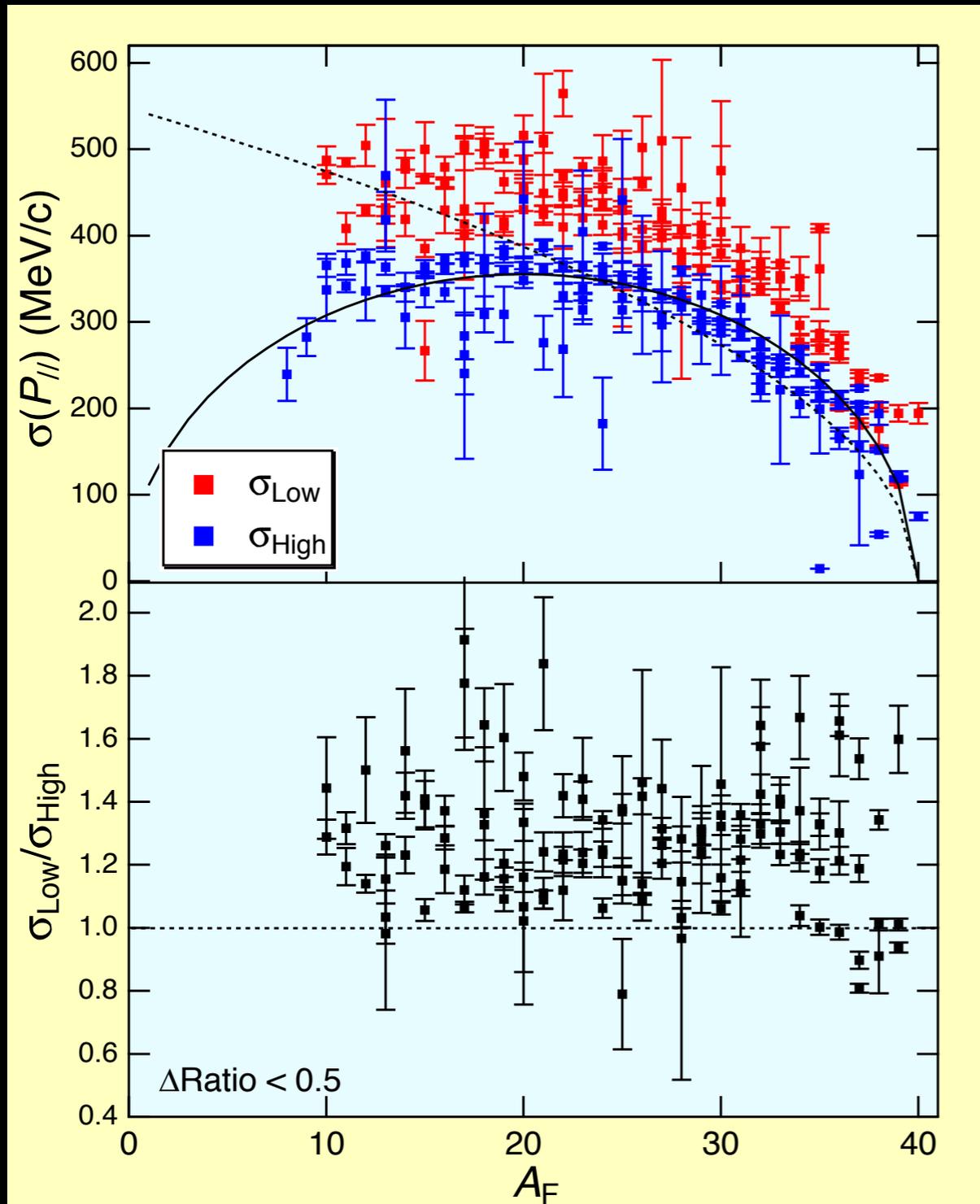


$$Y(P_L) = A \exp\left(-\frac{(P_L - P_0)^2}{2\sigma(P_L)^2}\right) \begin{cases} \sigma(P_L) = \sigma_{\text{Low}} & \text{if } P_L < P_0 \\ \sigma(P_L) = \sigma_{\text{High}} & \text{if } P_L > P_0 \end{cases}$$

Fitting results \rightarrow width and velocity shift
 σ_{Low} , σ_{High} $-\Delta P_L$

Asymmetry in P_L distributions

• $^{40}\text{Ar} + ^{93}\text{Nb} \rightarrow \text{AZ}$



- GH model is valid for σ_{High} .
- $\sigma_{\text{Low}}/\sigma_{\text{High}} = 120 \sim 130 \%$.

Asymmetric P_L distributions

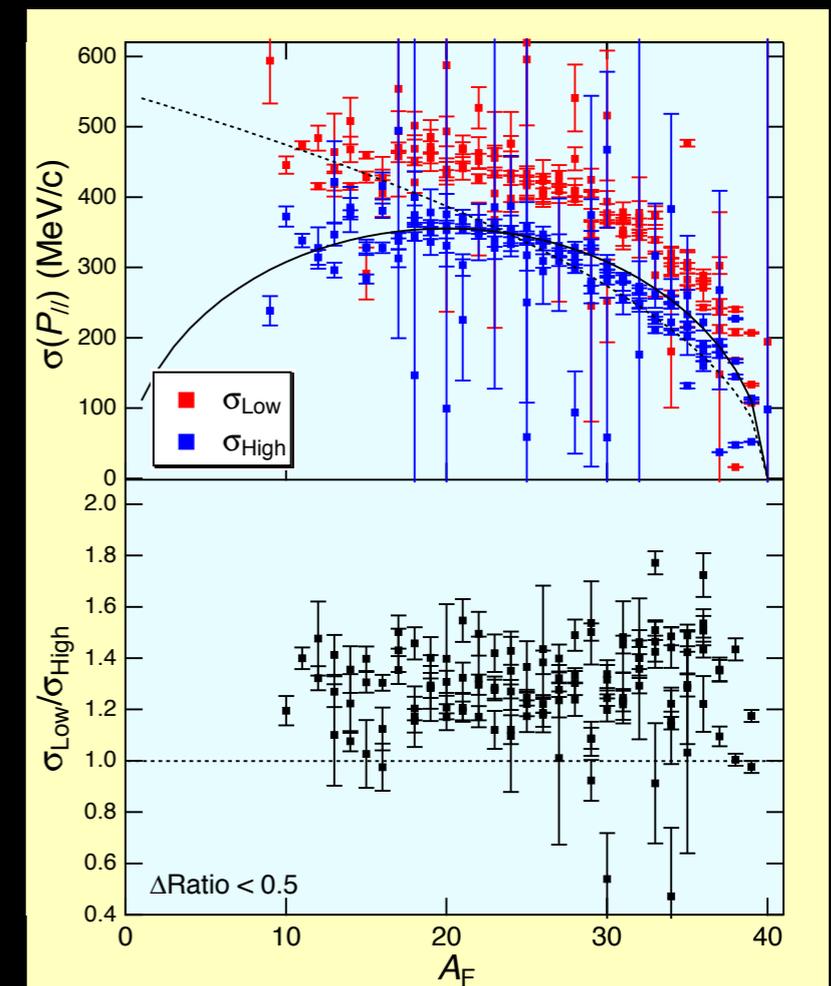
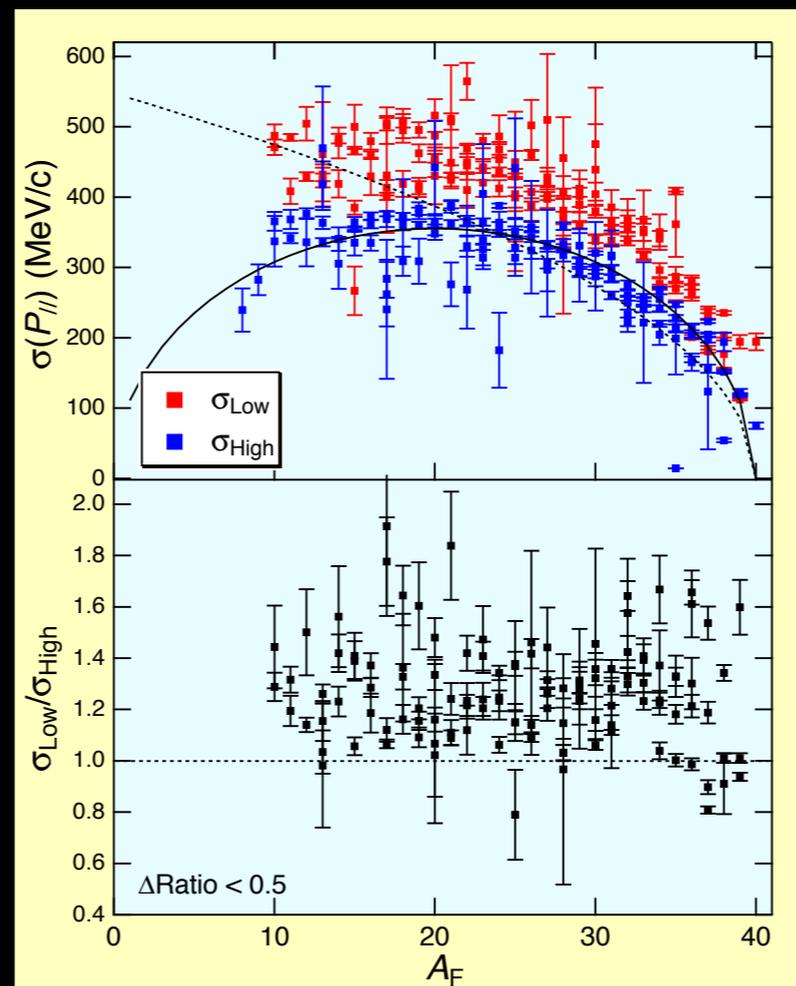
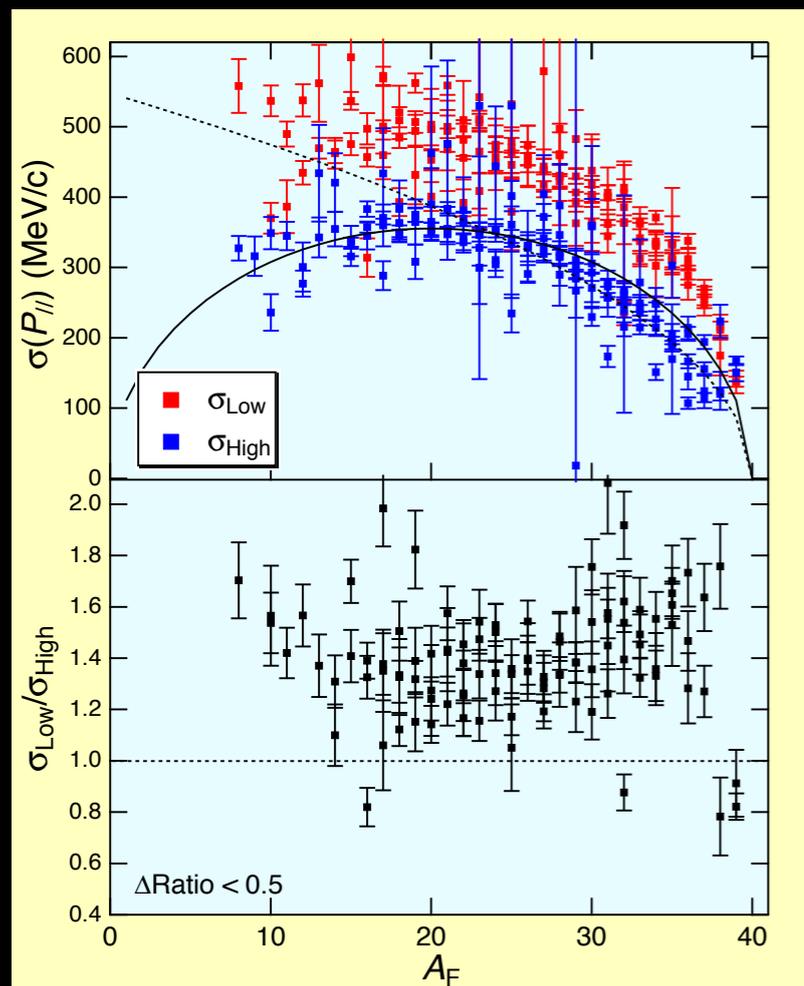
- Target dependence

$^{40}\text{Ar} +$

• ^{12}C

• ^{93}Nb

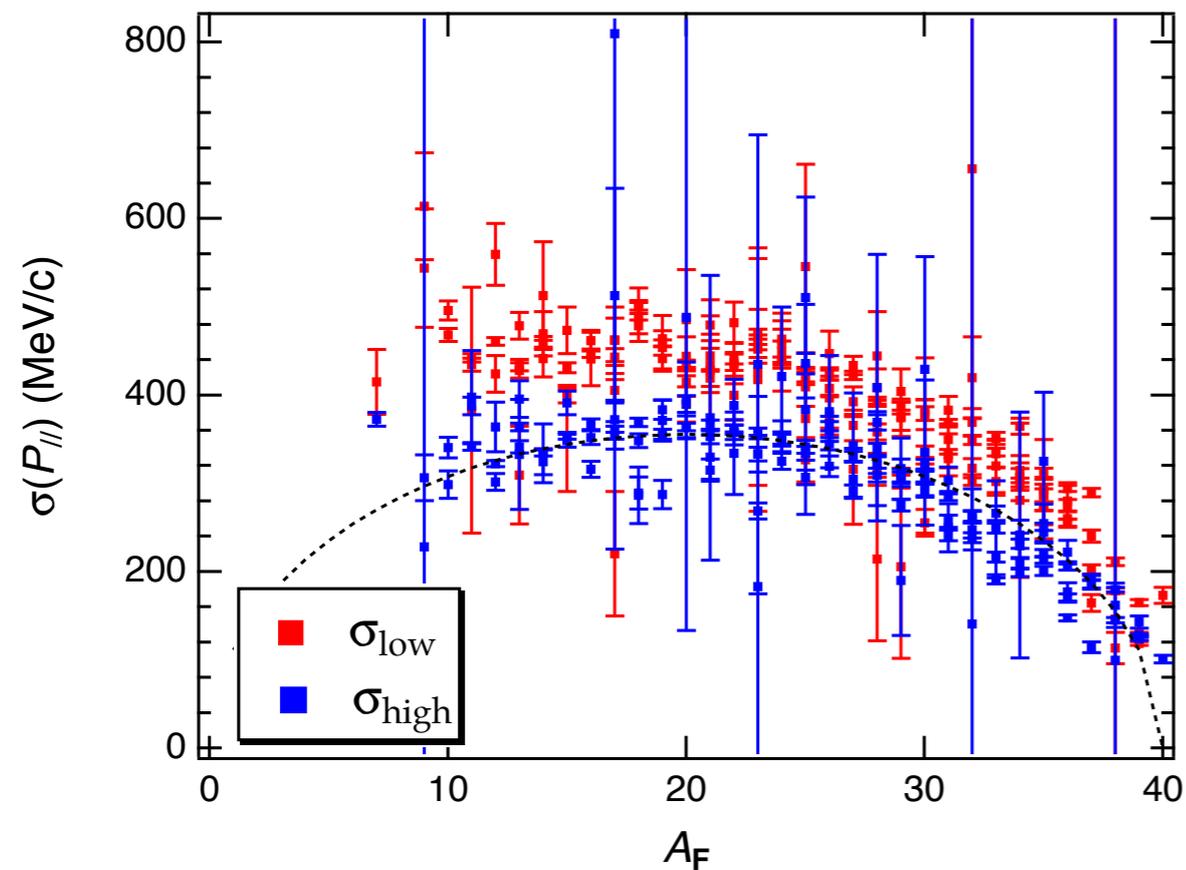
• ^{197}Au



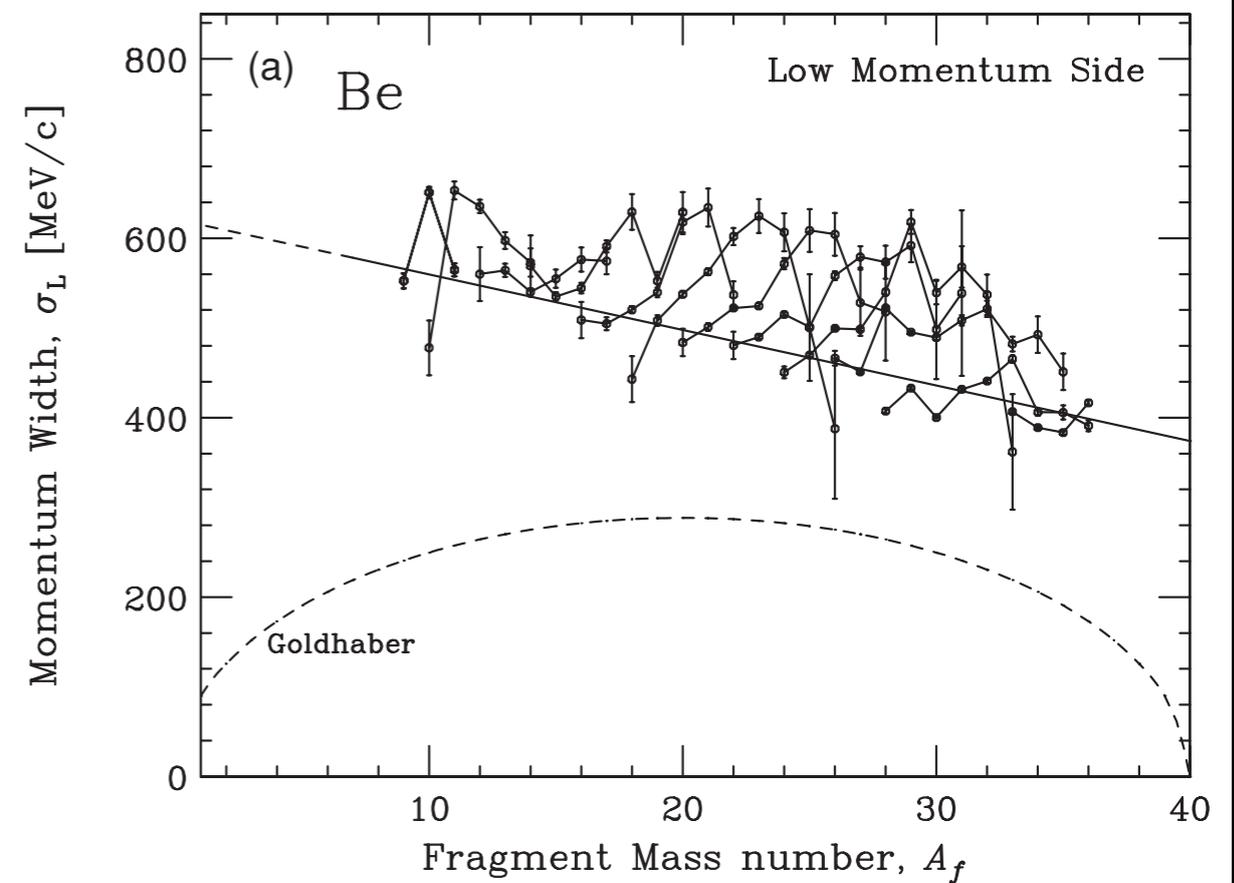
Asymmetric P_L distributions

- E dependence

• $^{40}\text{Ar}+^{12}\text{C}$ (290 MeV/u)



• $^{40}\text{Ar}+^9\text{Be}$ (90 MeV/u)



• Broadening effect is suppressed compared with lower energy reaction.

• $^{40}\text{Ar}+^9\text{Be}$ @95 MeV/u Notani et al.
M. Notani et al., PRC 76 (2007) 044605.

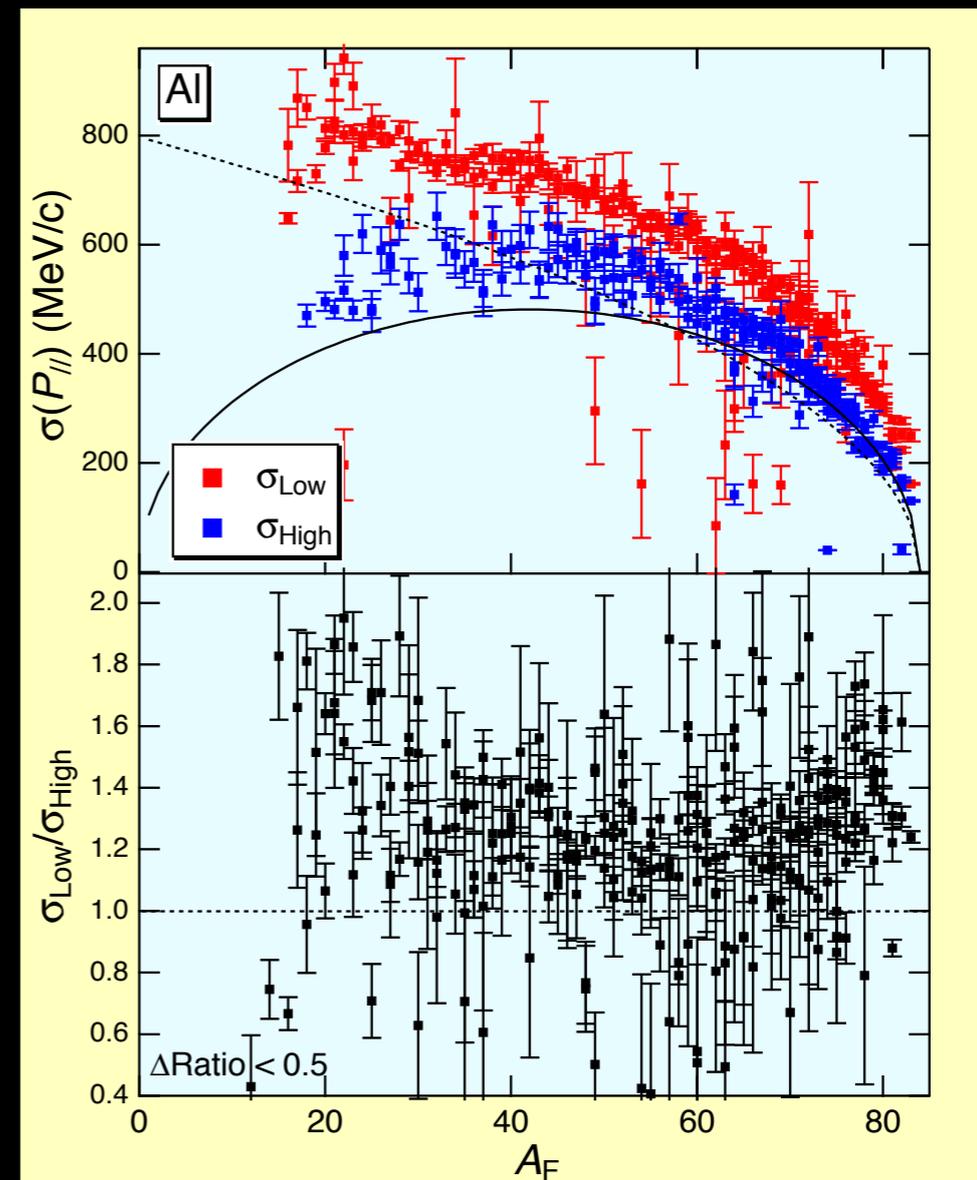
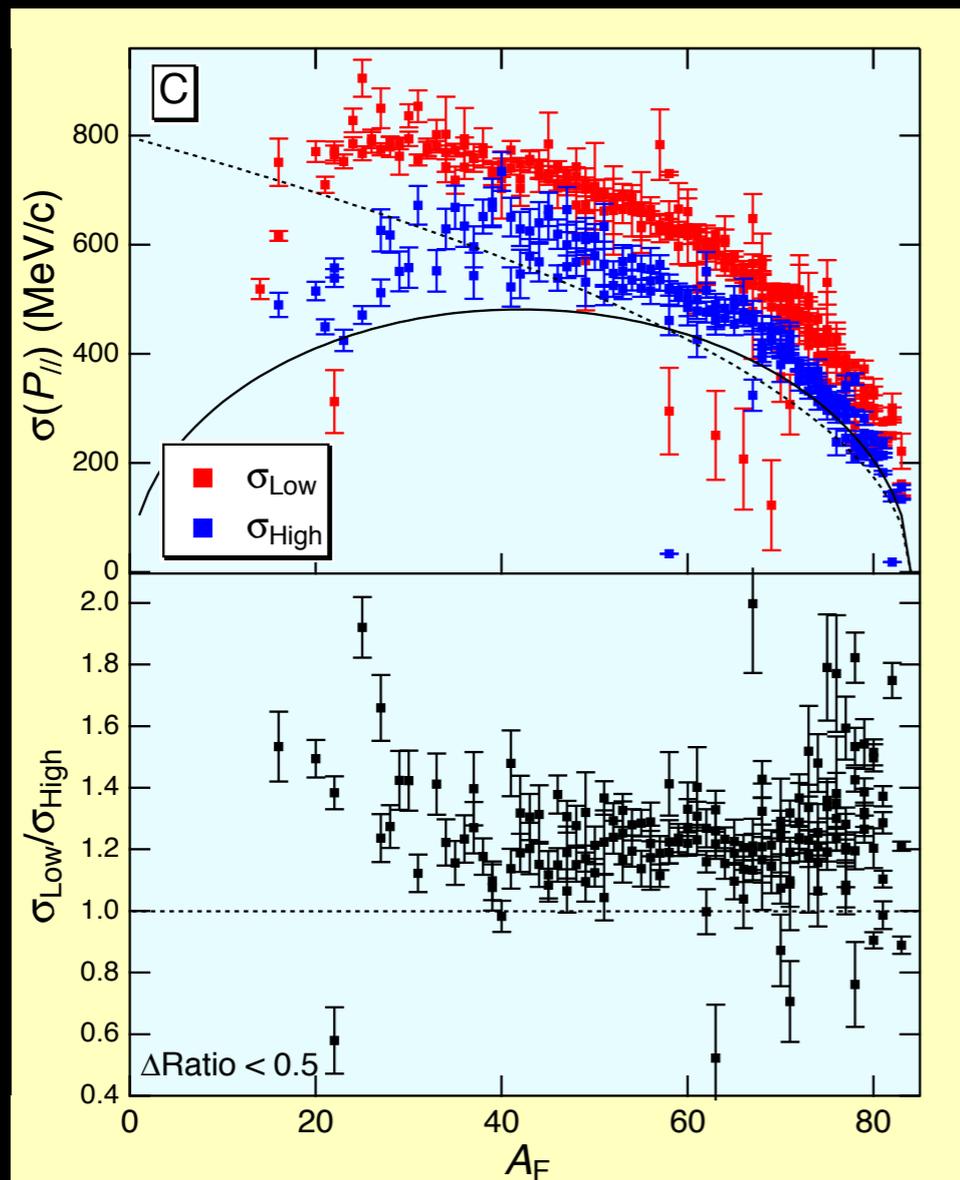
Asymmetric P_L distributions

- Target dependence

$^{84}\text{Kr} +$

• ^{12}C

• ^{27}Al

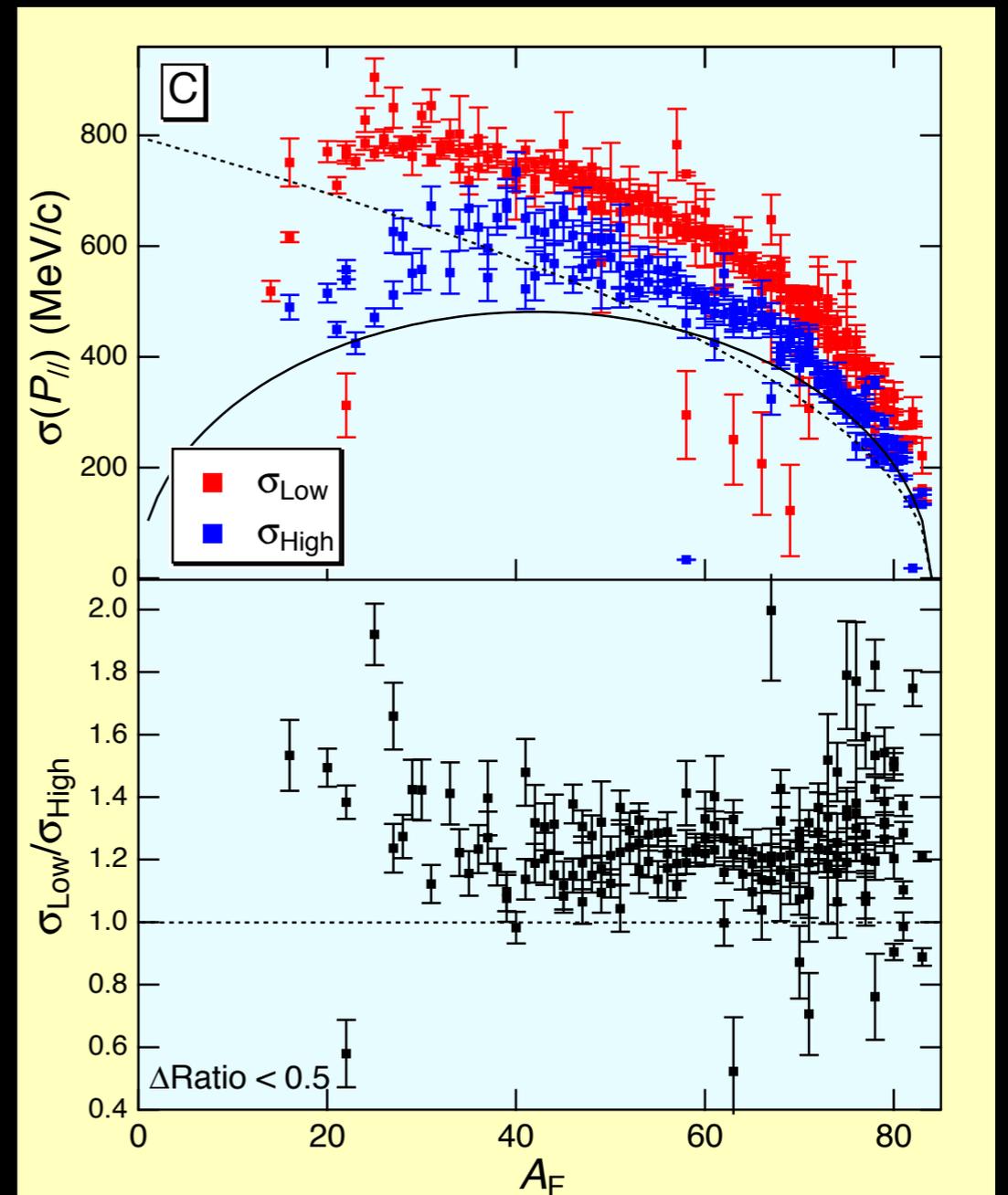
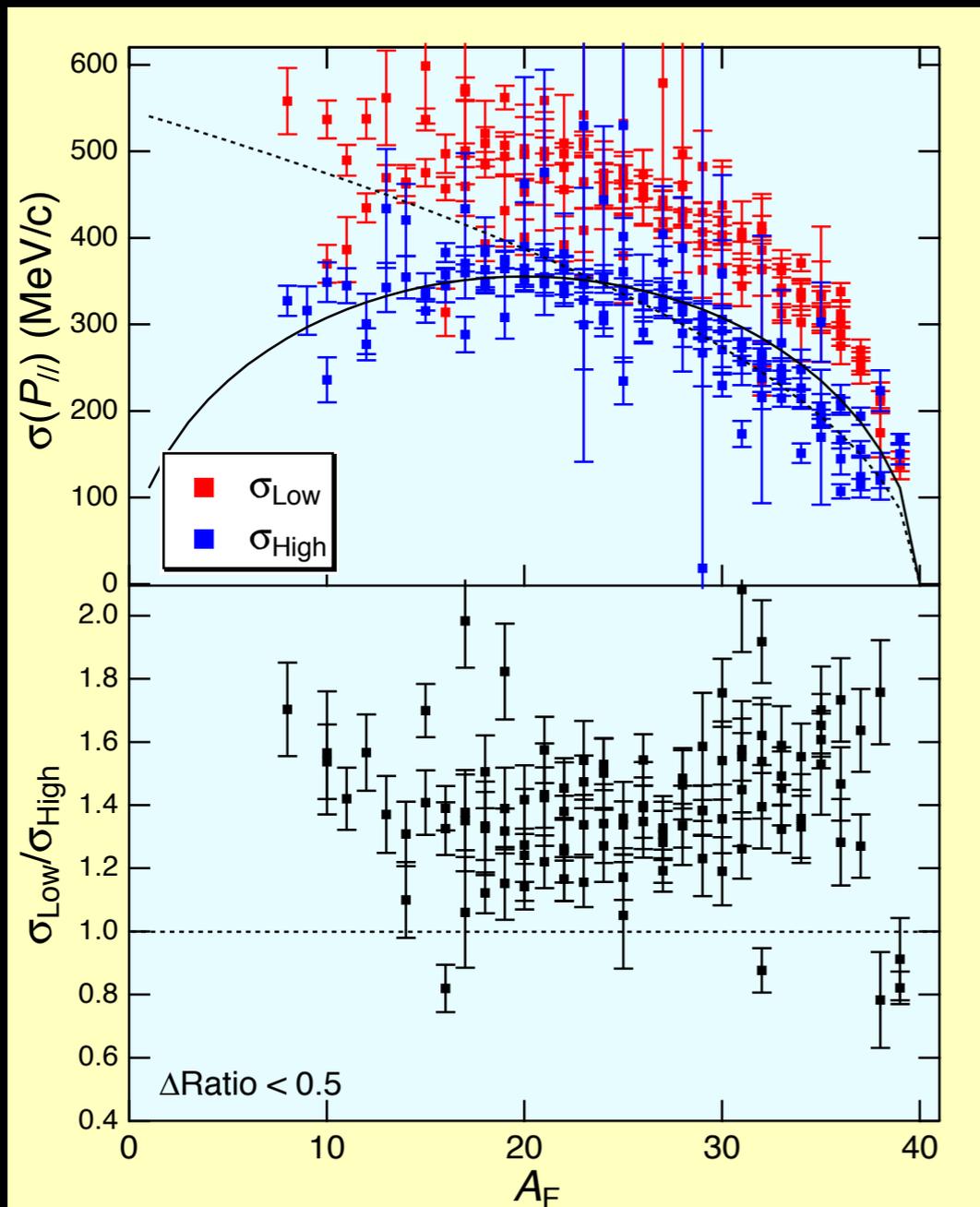


Asymmetry in P_L distributions

- Ar and Kr beam

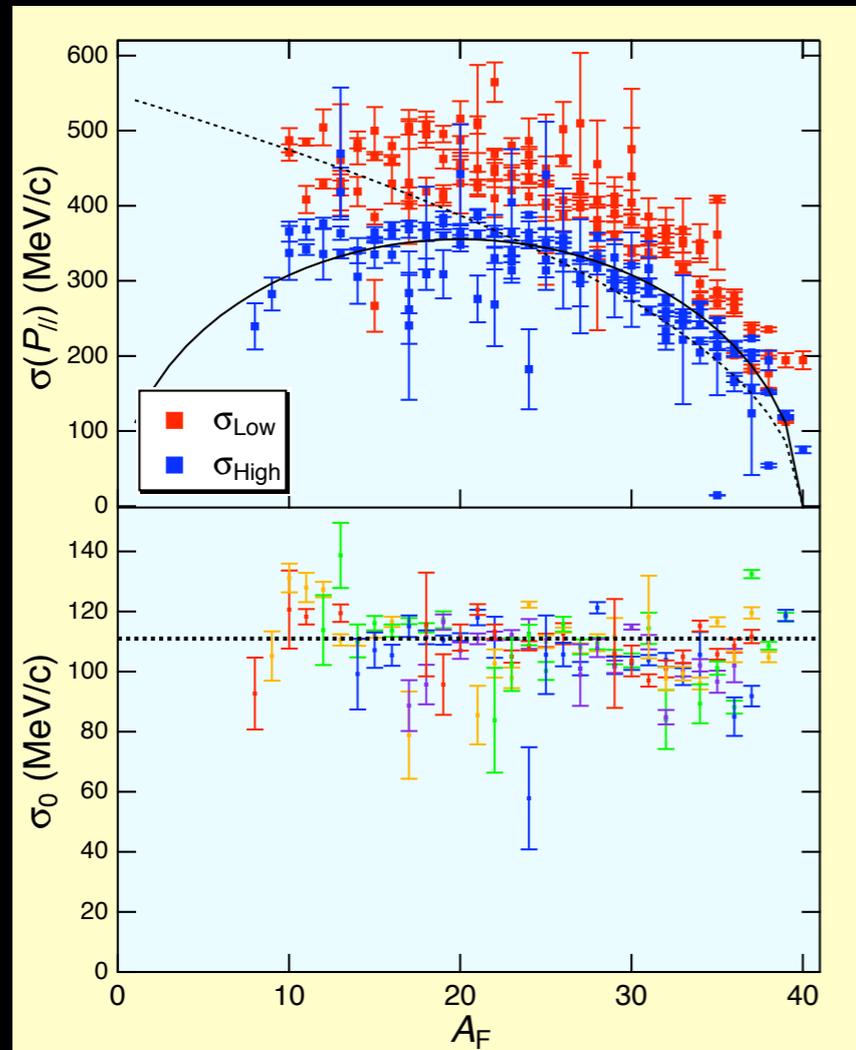
• $^{40}\text{Ar} + ^{12}\text{C}$

• $^{84}\text{Kr} + ^{12}\text{C}$



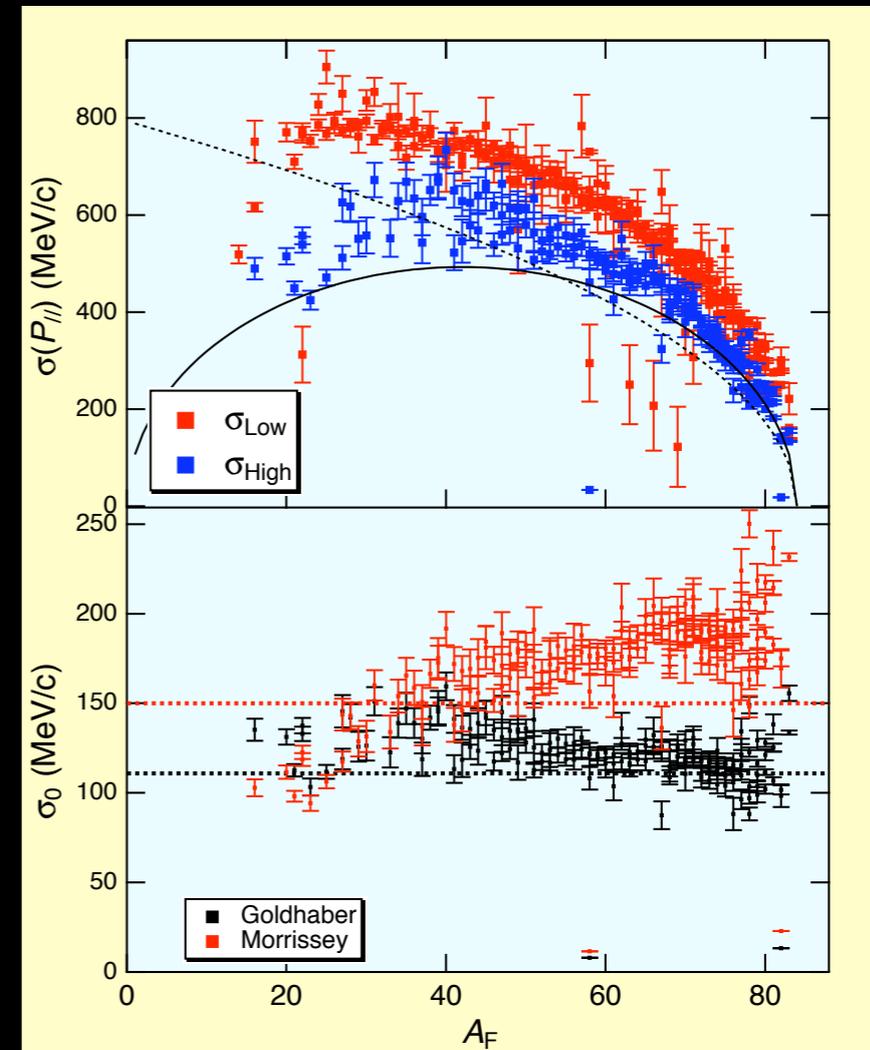
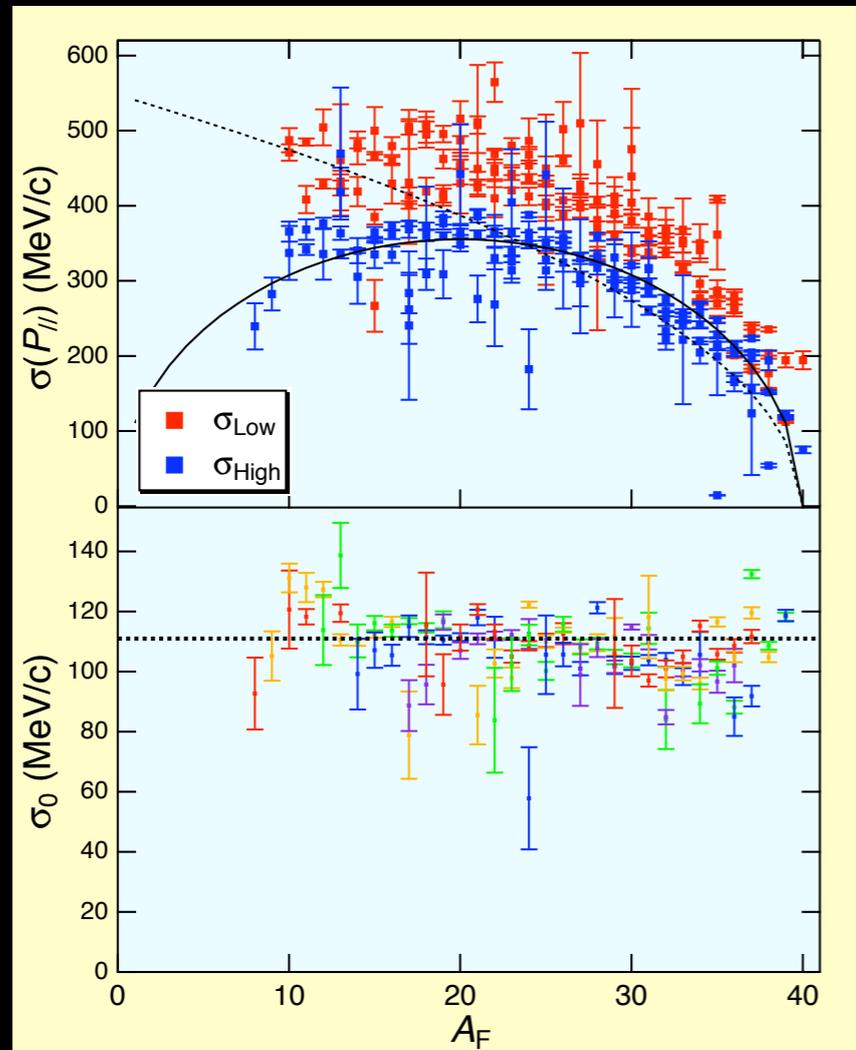
Reduced width : σ_0

- $^{40}\text{Ar} + ^{93}\text{Nb} \rightarrow \text{AZ}$



- GH formulation is valid for σ_{High} .
- σ_0 obtained from σ_{High} is ~ 110 MeV/c.

Reduced width : σ_0

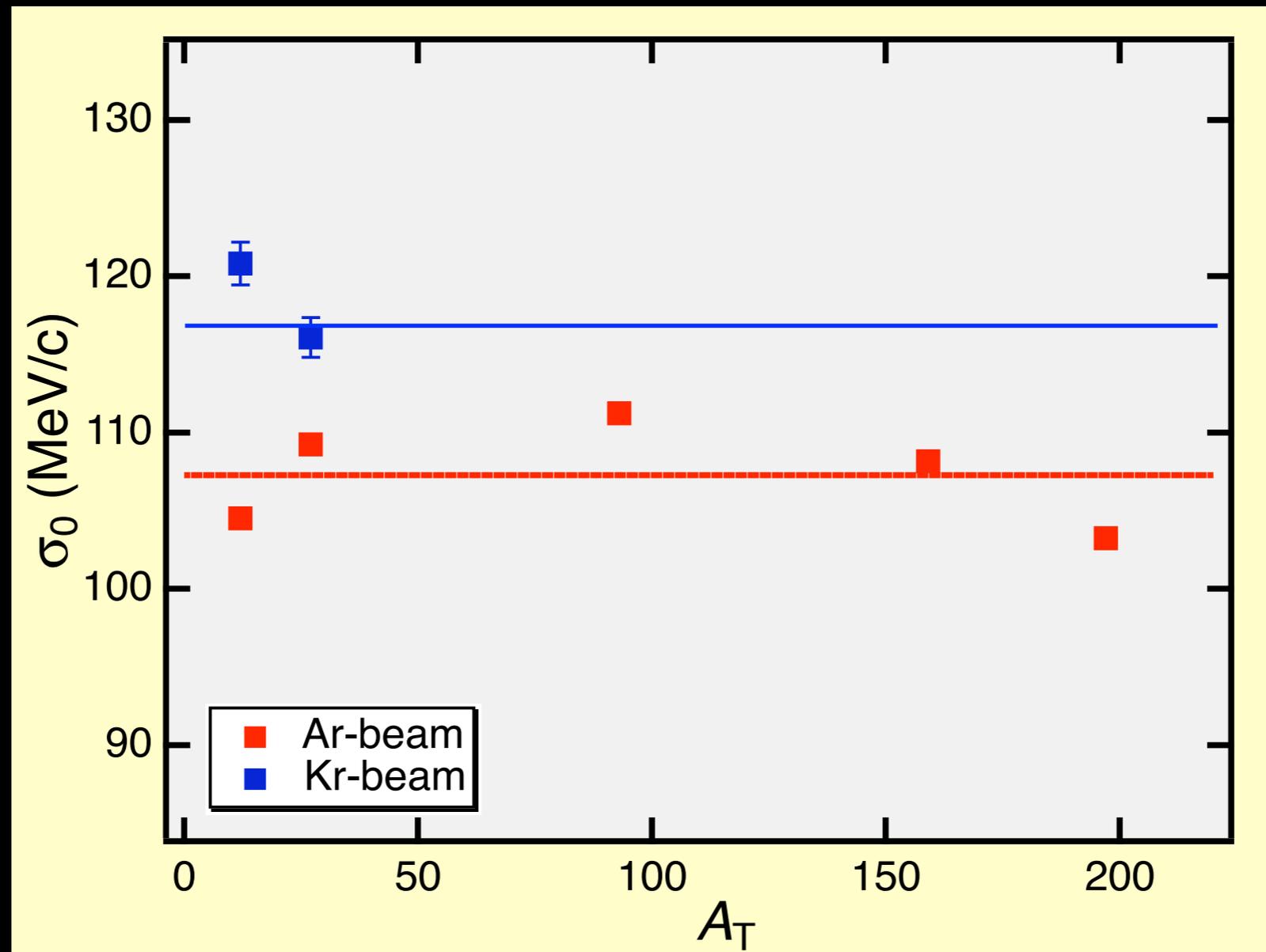


- GH formulation is valid for σ_{High} .
- σ_0 obtained from σ_{High} is ~ 110 MeV/c.

- GH formulation is valid only for heavy PLFs.
- σ_0 is slightly larger than that for Ar-beam.

Reduced width : σ_0

- Target dependence

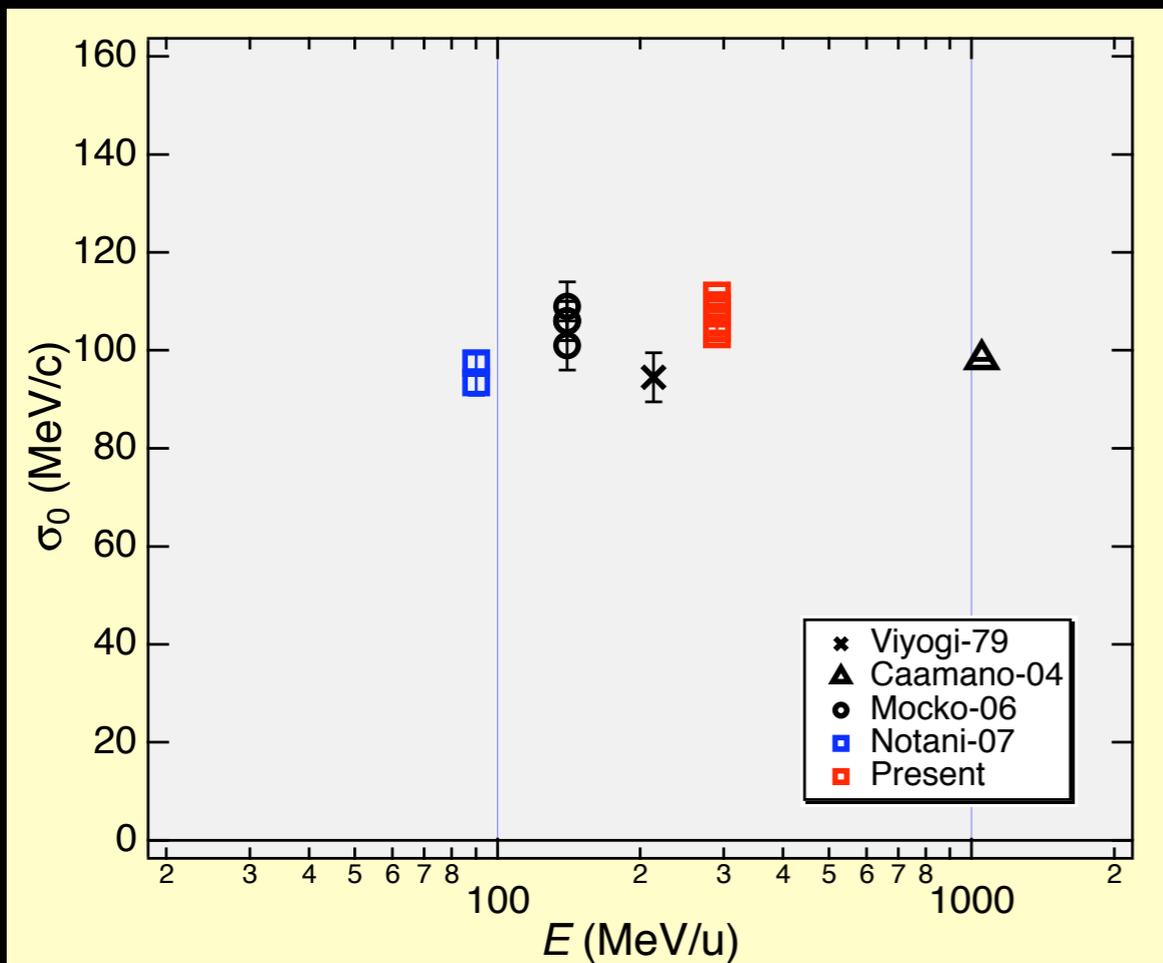


- Small target dependence
- $\sigma_0(\text{Kr})$ is larger than $\sigma_0(\text{Ar})$.

Reduced width : σ_0

- E dependence

Ar-beam

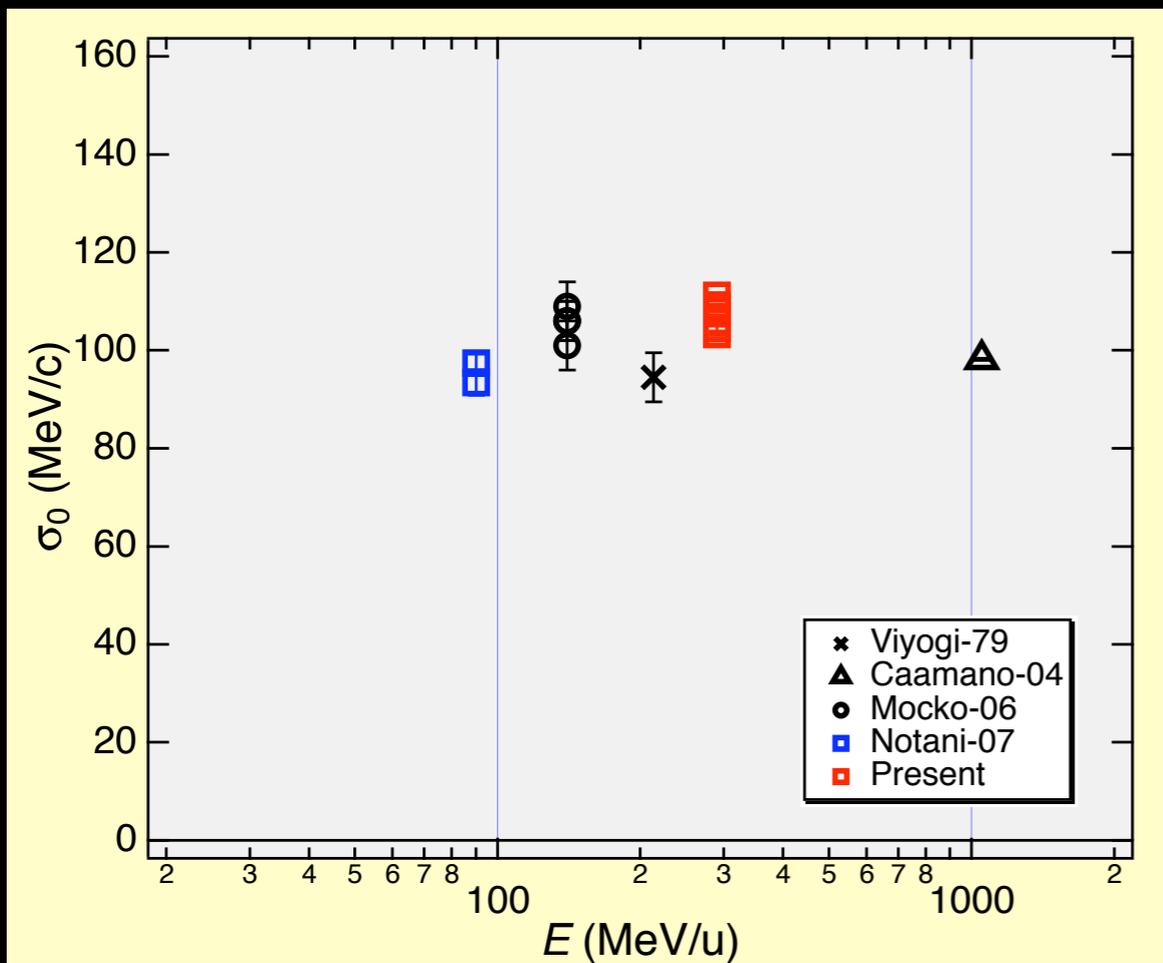


- σ_0 is constant at $E = 90 \sim 1000$ MeV/u.

Reduced width : σ_0

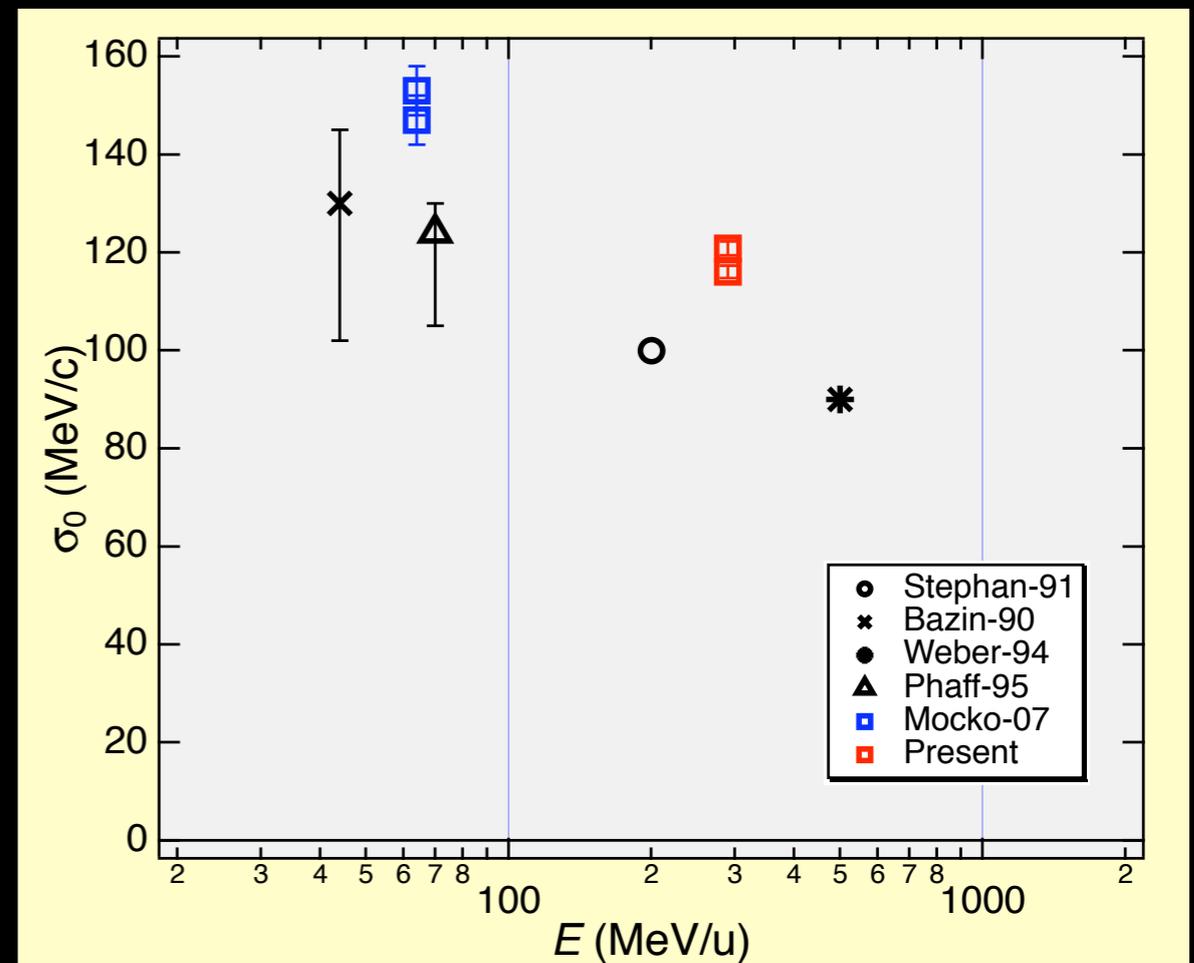
- E dependence

Ar-beam



- σ_0 is constant at $E = 90 \sim 1000$ MeV/u.

Kr-beam

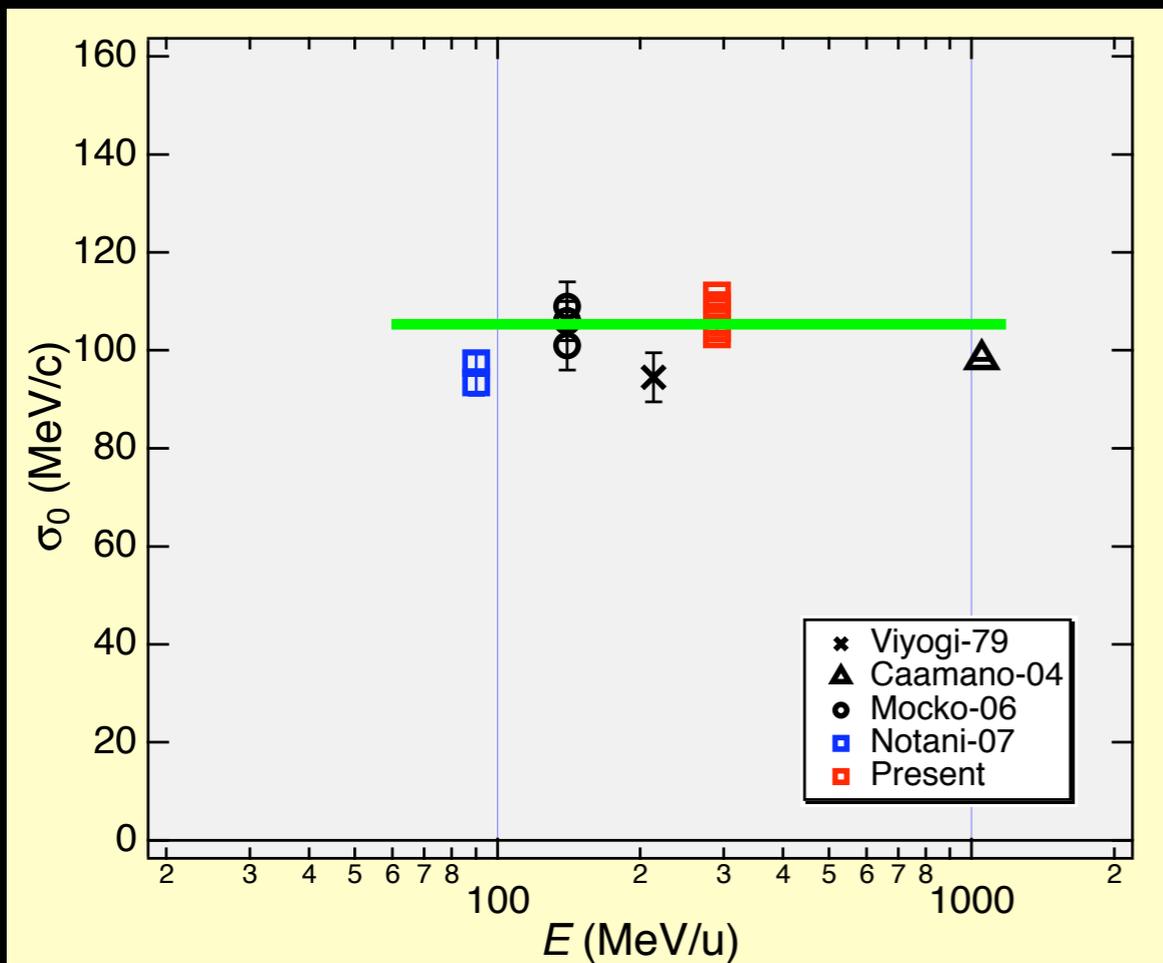


- σ_0 decreases at $E = 40 \sim 500$ MeV/u.
- Recent results are larger than previous ones.

Reduced width : σ_0

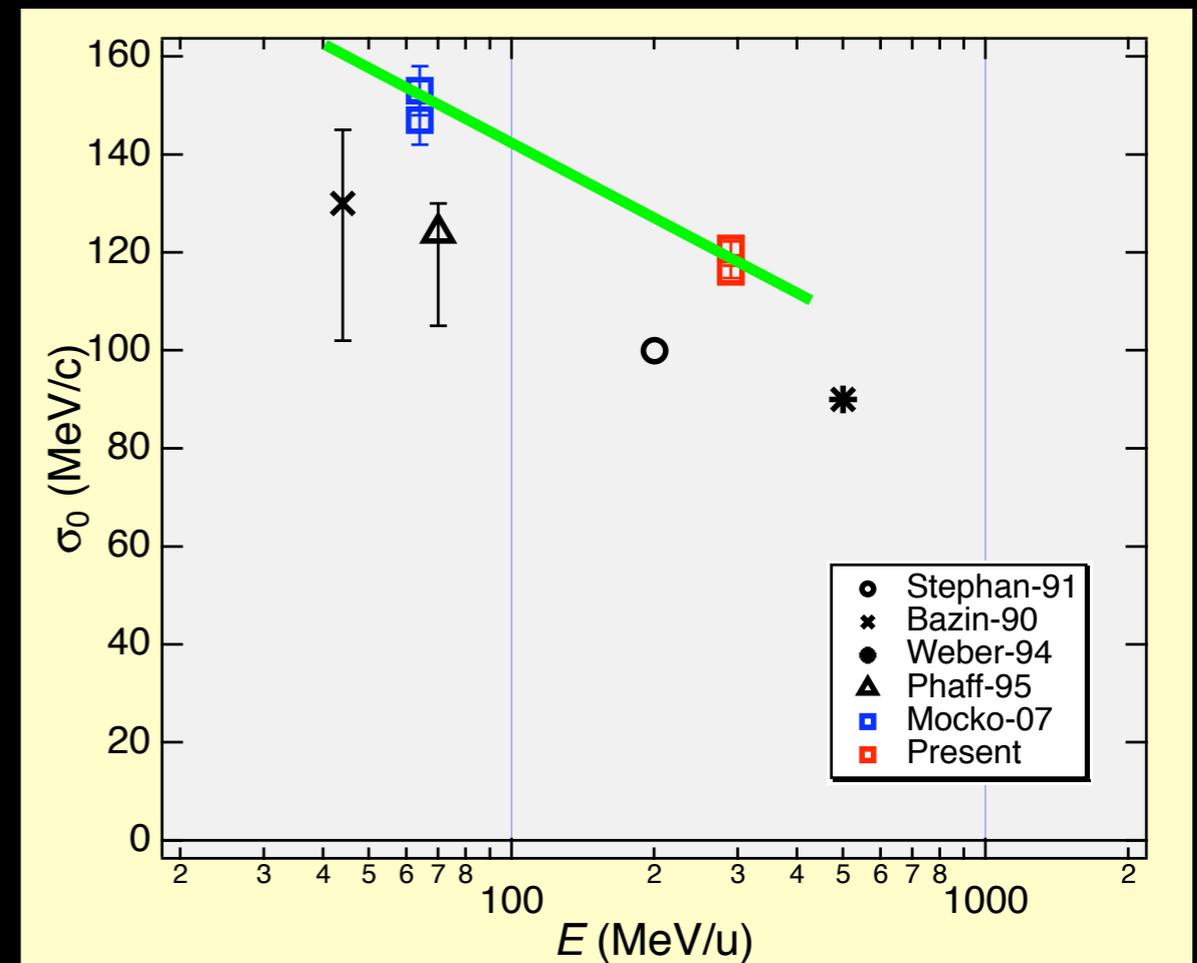
- E dependence

Ar-beam



- σ_0 is constant at $E = 90 \sim 1000$ MeV/u.

Kr-beam



- σ_0 decreases at $E = 40 \sim 500$ MeV/u.
- Recent results are larger than previous ones.

Parametrization of σ_0

- Based on observed systematics

Formulation proposed by Tripathi

$$\sigma_{0,\text{exp.}} = \left(1 + \frac{E_C}{4T_{\text{lab.}}}\right) \left(70 + \frac{2}{3} A_P\right) \text{ MeV/c}$$

$$E_C = \frac{1.44 Z_P Z_T}{r_P + r_T}, \quad r_1 = \sqrt{\frac{5}{3}} (r_1)_{\text{rms}}$$

$T_{\text{lab.}}$: Beam E in MeV/u

Tripathi et al., Phys. Rev. C 49 (1994) 2237.

$^{12}\text{C}, ^{16}\text{O}$	(1, 2 GeV/u)	: Greiner	@1975
^{139}La	(1.2 GeV/u)	: Brady	@1988
^{40}Ar	(213 MeV/u)	: Viyogi	@1979
^{197}Au	(1 GeV/u)	: Dreute	@1991

Parametrization of σ_0

- Based on observed systematics

Formulation proposed by Tripathi

$$\sigma_{0,\text{exp.}} = \left(1 + \frac{E_C}{4T_{\text{lab.}}}\right) \left(70 + \frac{2}{3} A_P\right) \text{ MeV/c}$$

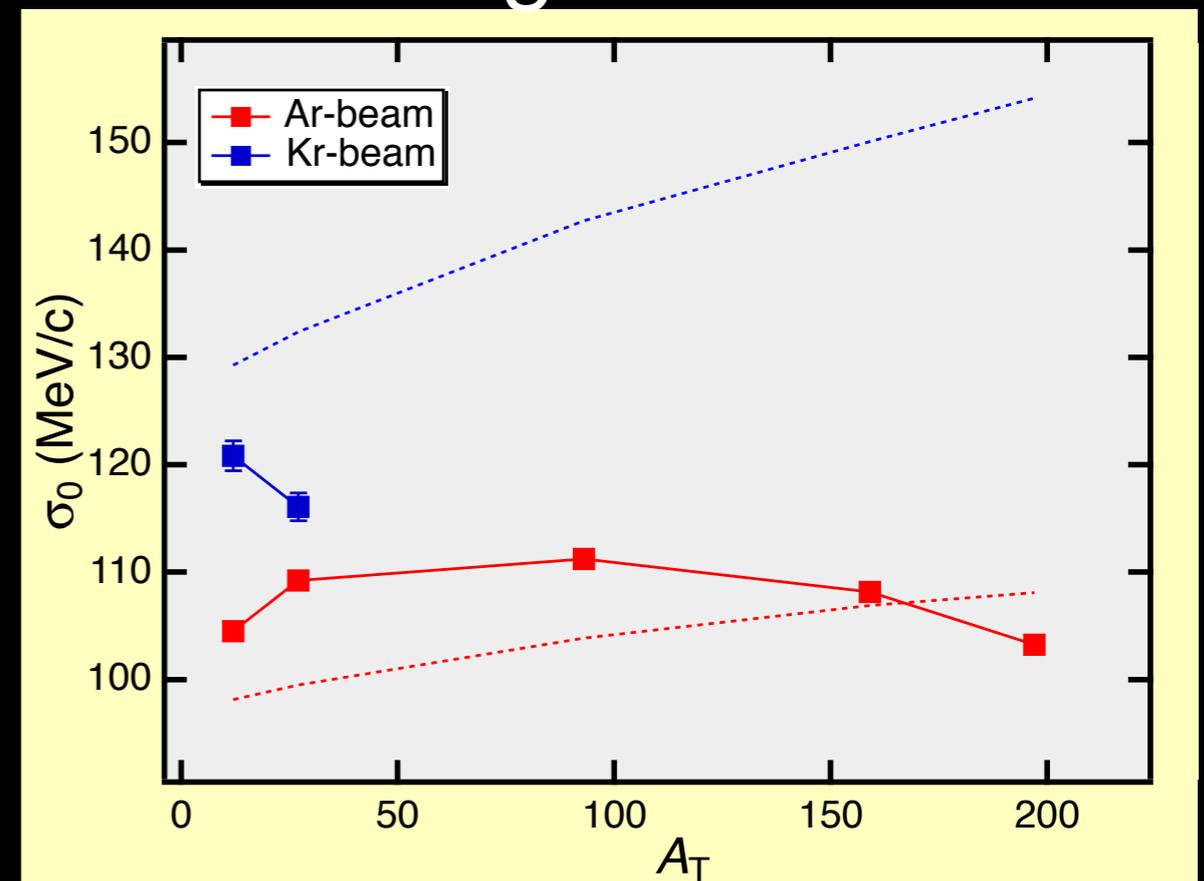
$$E_C = \frac{1.44 Z_P Z_T}{r_P + r_T}, \quad r_i = \sqrt{\frac{5}{3}} (r_i)_{\text{rms}}$$

$T_{\text{lab.}}$: Beam E in MeV/u

Tripathi et al., Phys. Rev. C 49 (1994) 2237.

$^{12}\text{C}, ^{16}\text{O}$	(1, 2 GeV/u)	: Greiner	@1975
^{139}La	(1.2 GeV/u)	: Brady	@1988
^{40}Ar	(213 MeV/u)	: Viyogi	@1979
^{197}Au	(1 GeV/u)	: Dreute	@1991

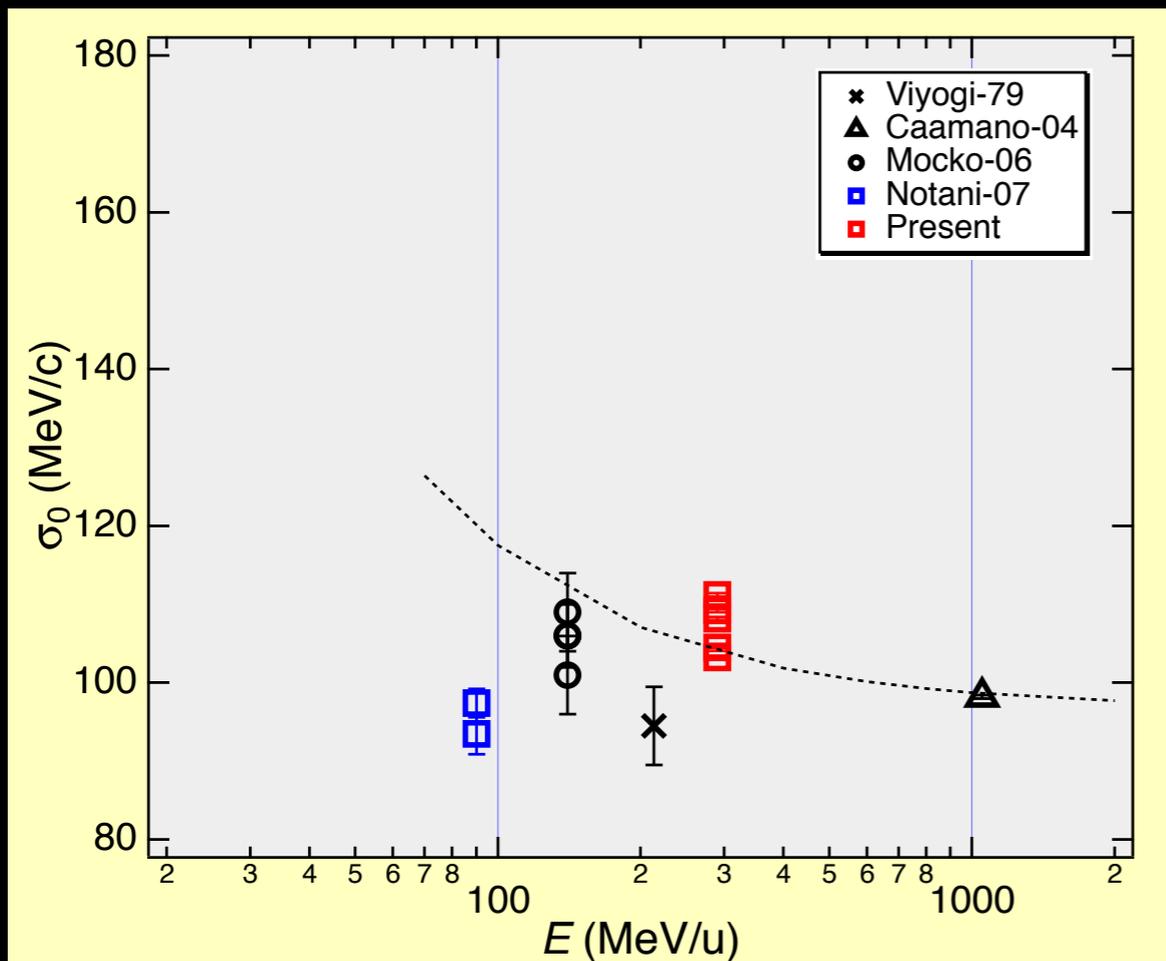
• Target mass



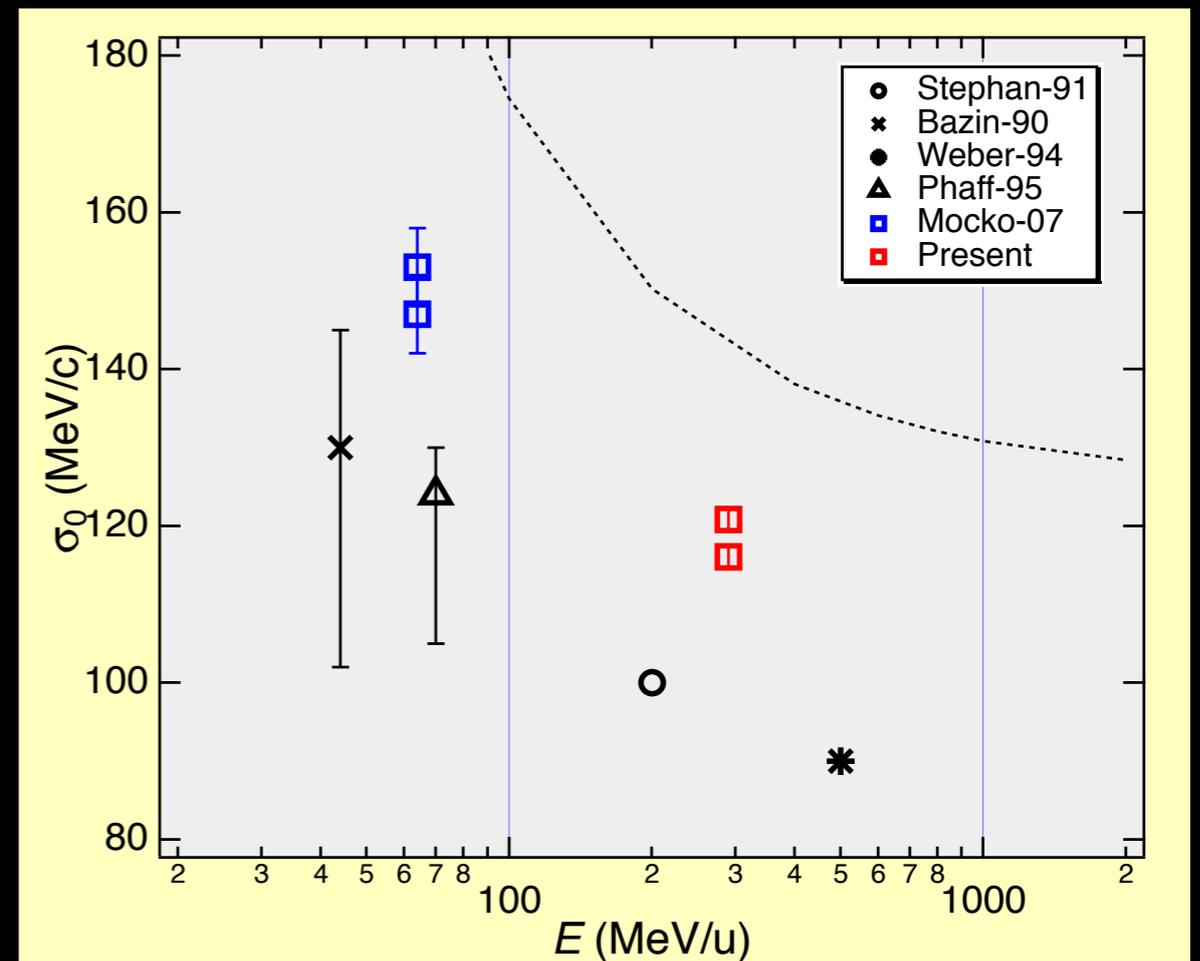
Parametrization of σ_0

- Energy dependence

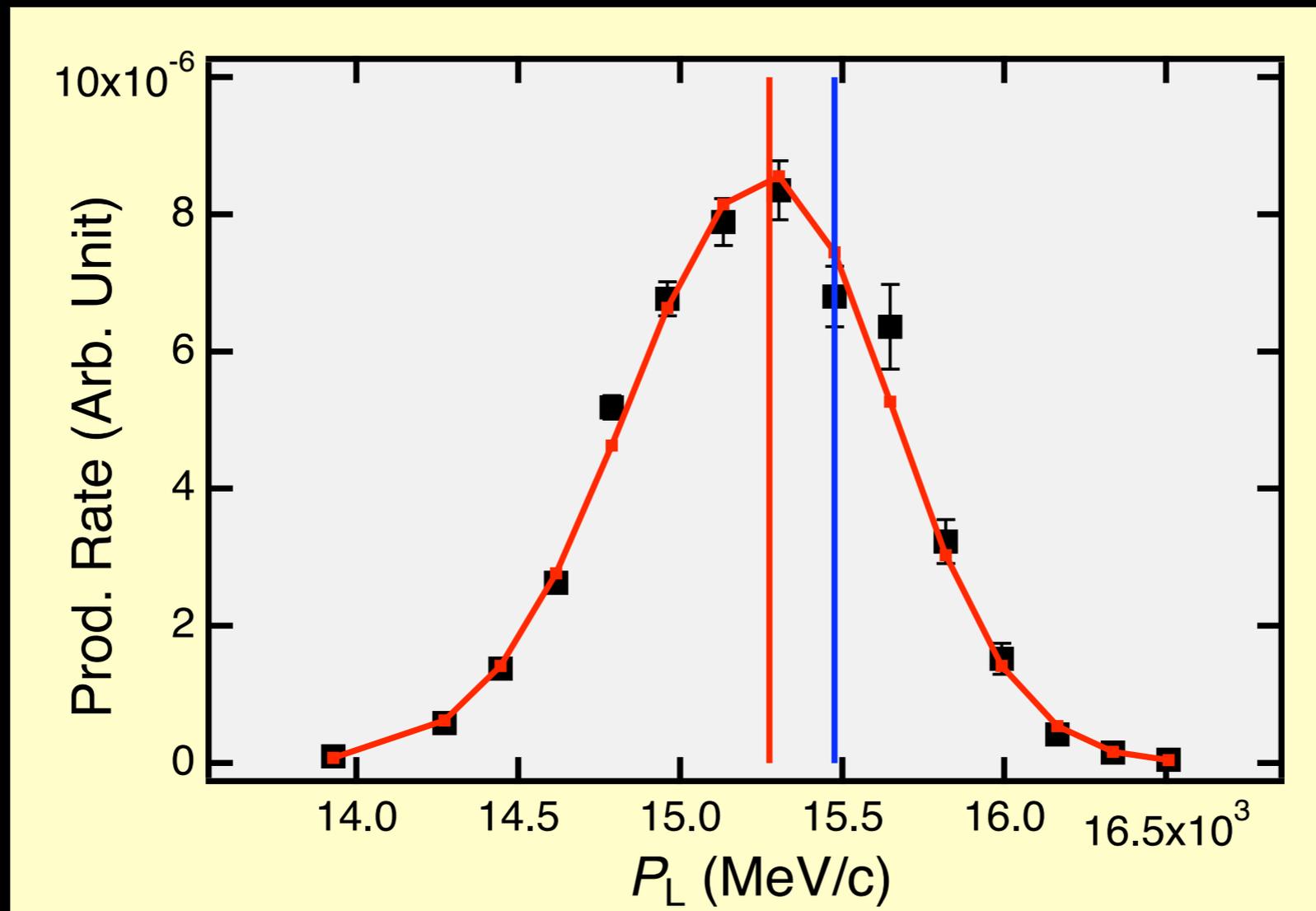
•Ar



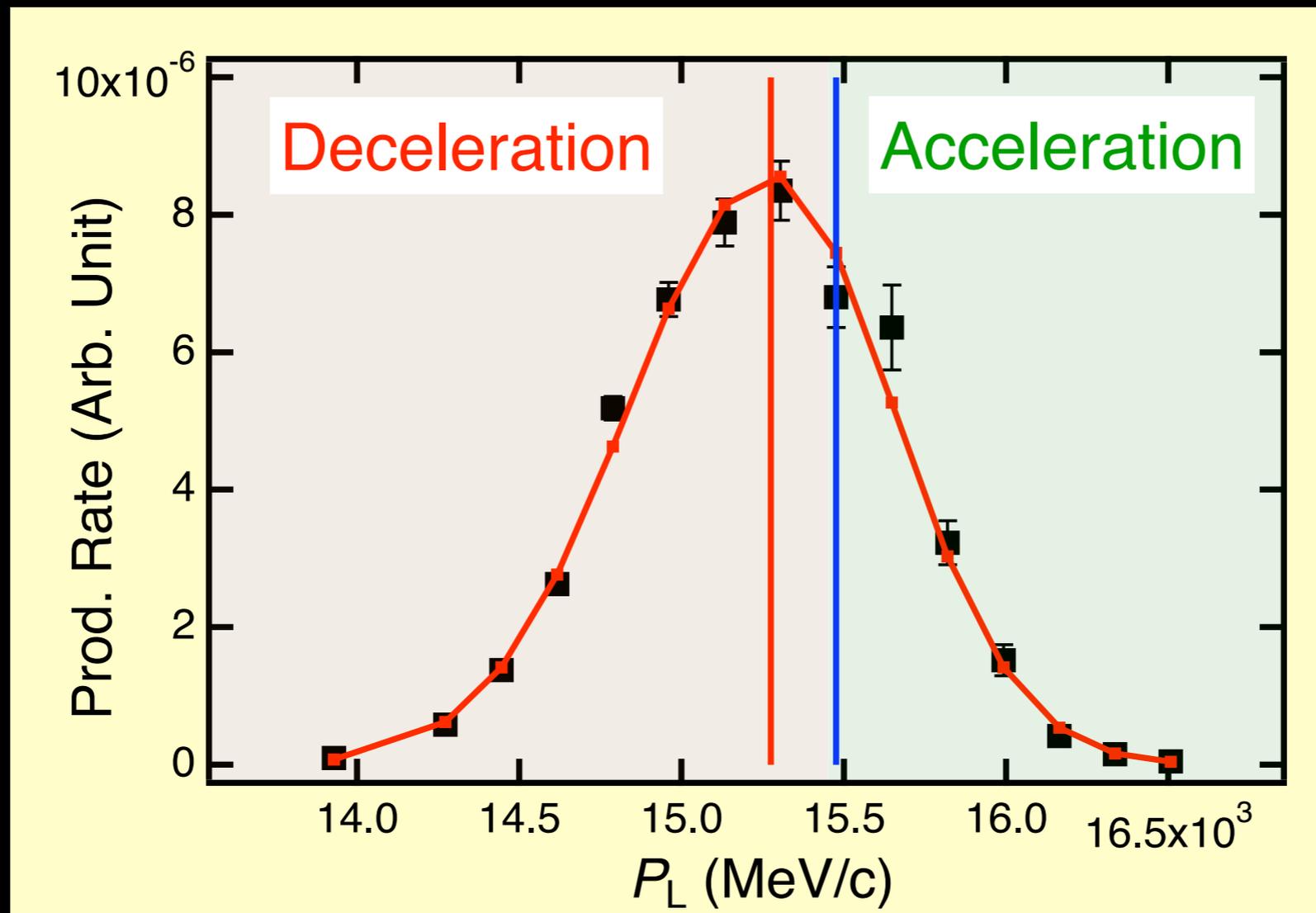
•Kr



Velocity shift

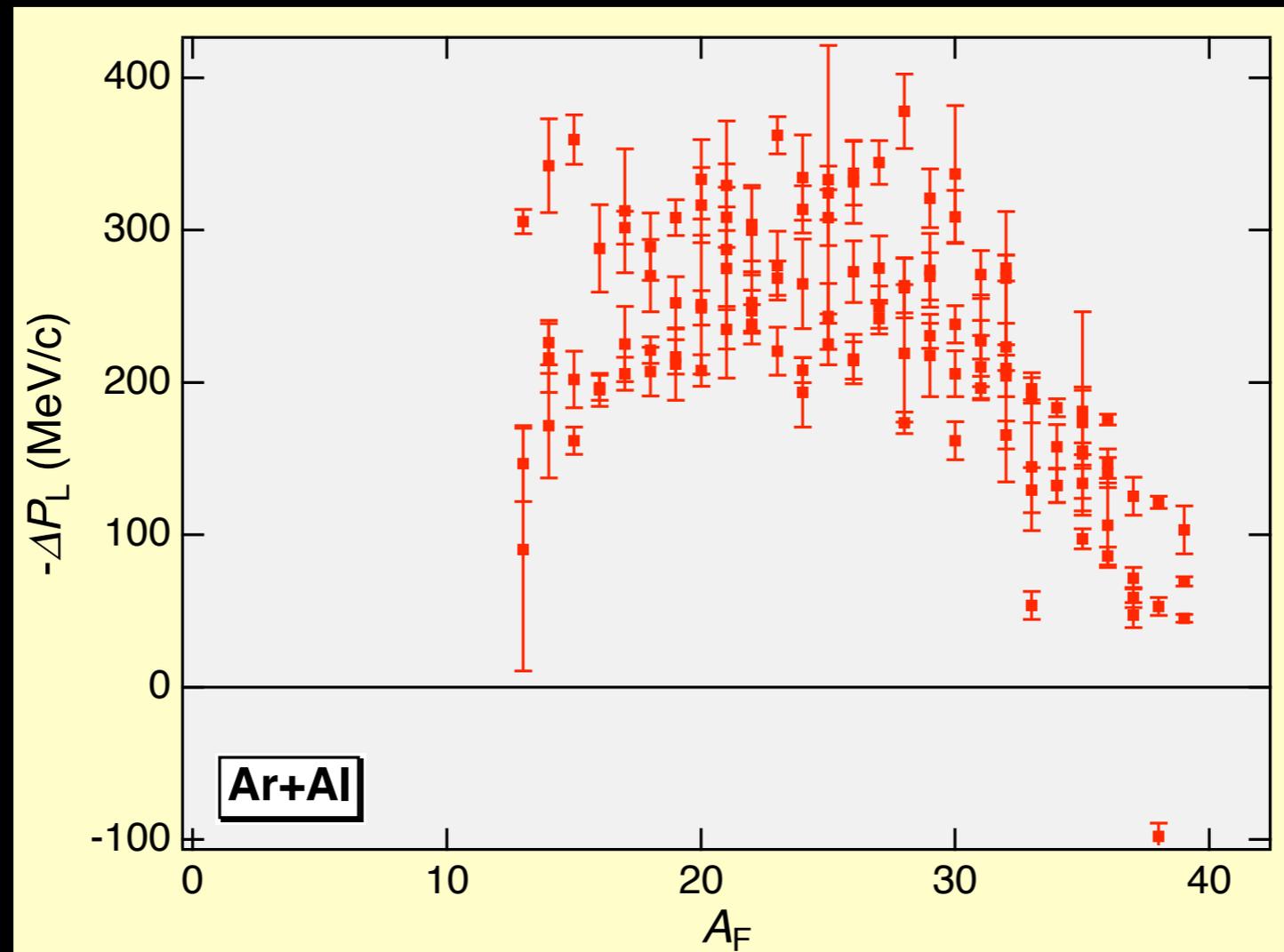


Velocity shift



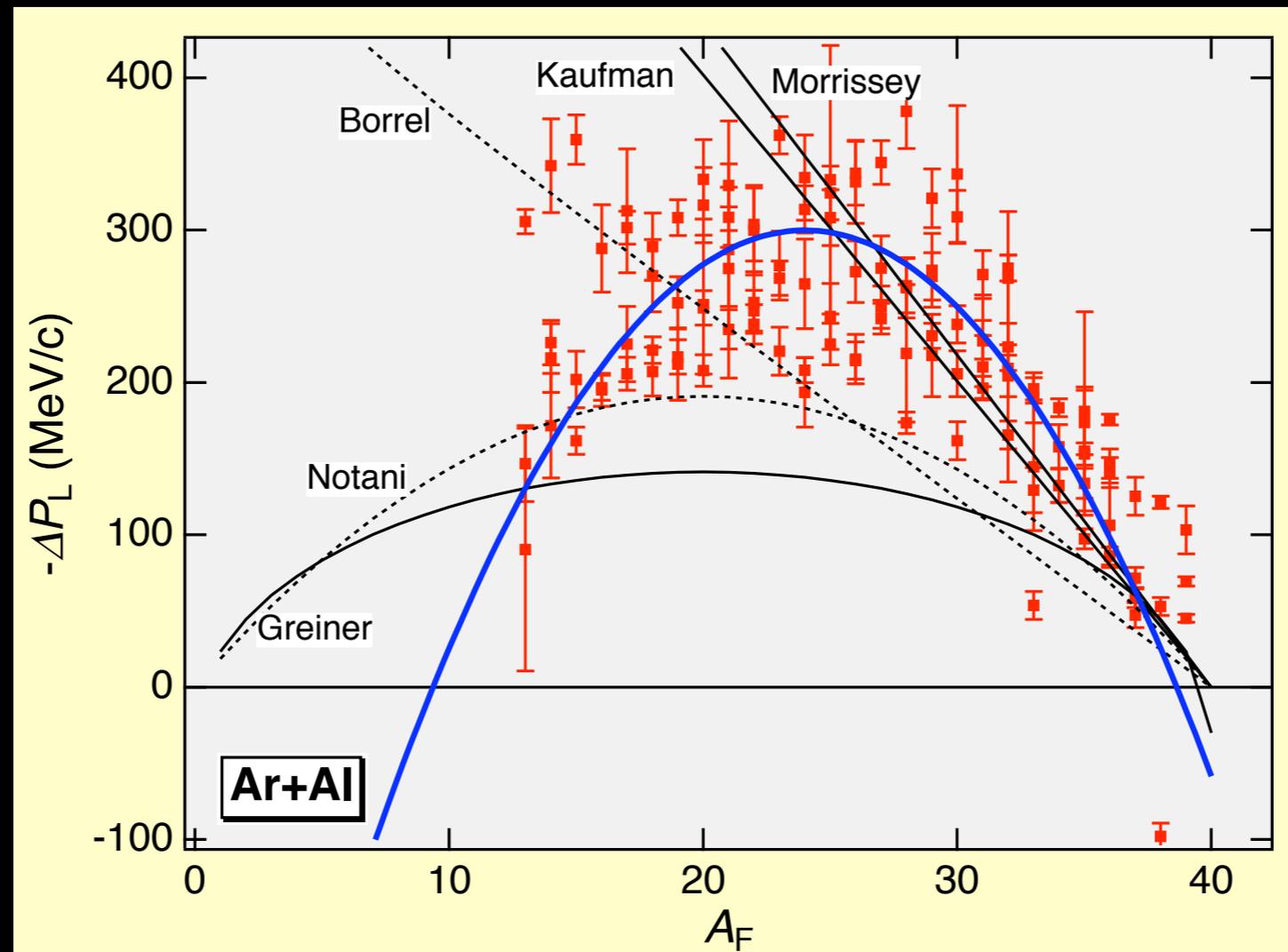
Velocity shift

- In case of Ar-beam



Velocity shift

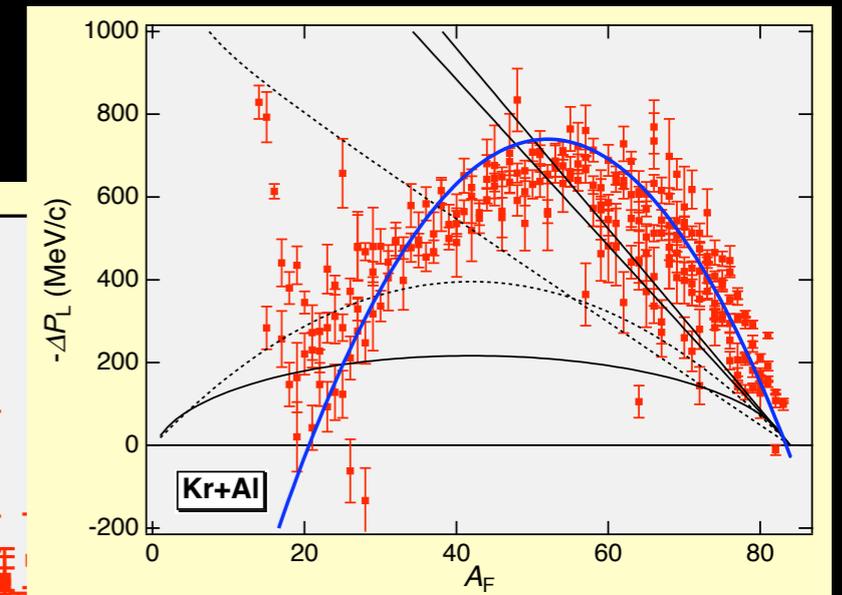
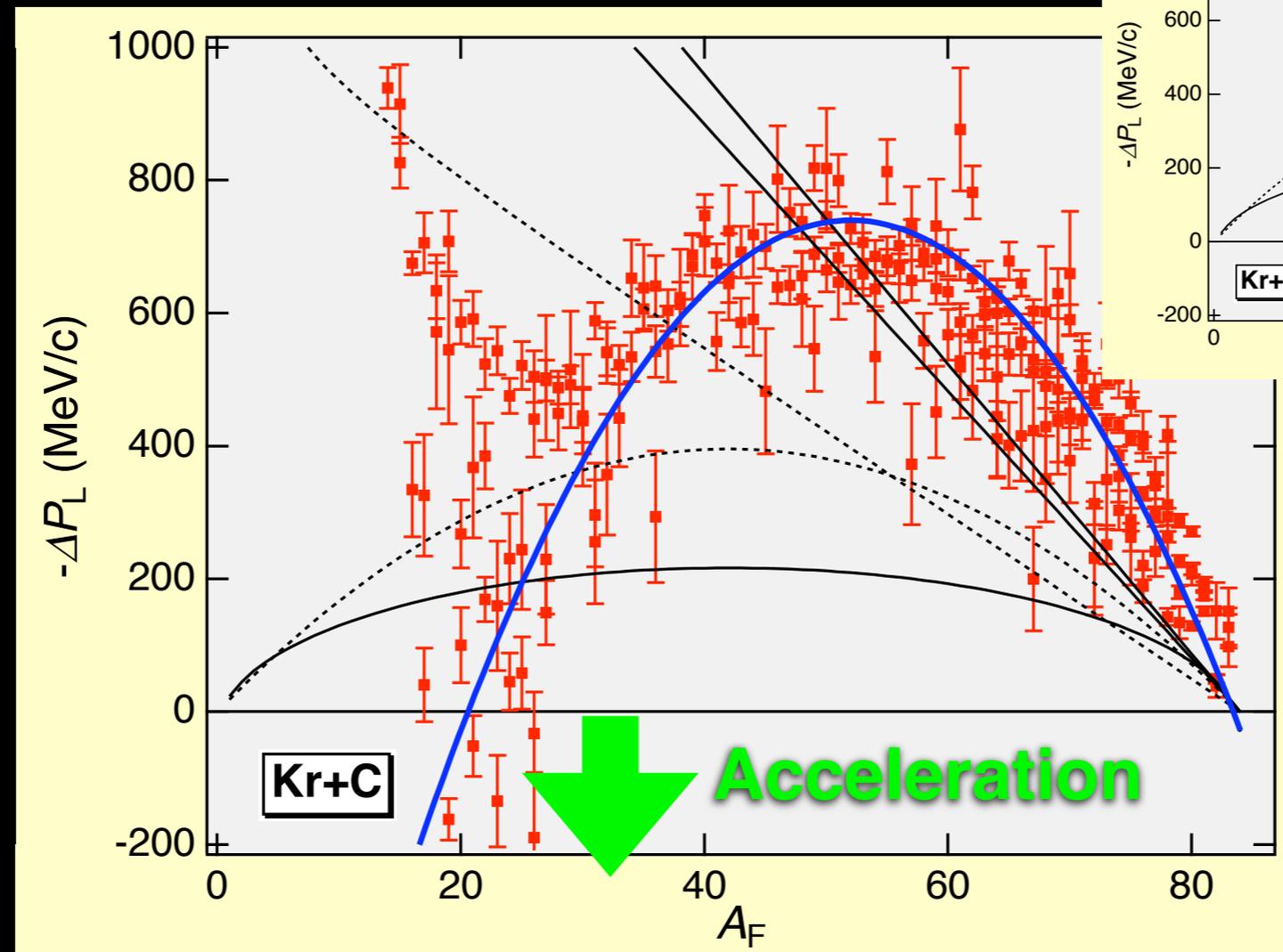
- In case of Ar-beam



- $-\Delta P_L$ distribution shows parabolic shape and become its maximum 300 MeV/c at $A_F \sim 25$.
- Morrissey/Kaufman formulation is probable for heavier PLFs.

Velocity shift

- Kr-beam

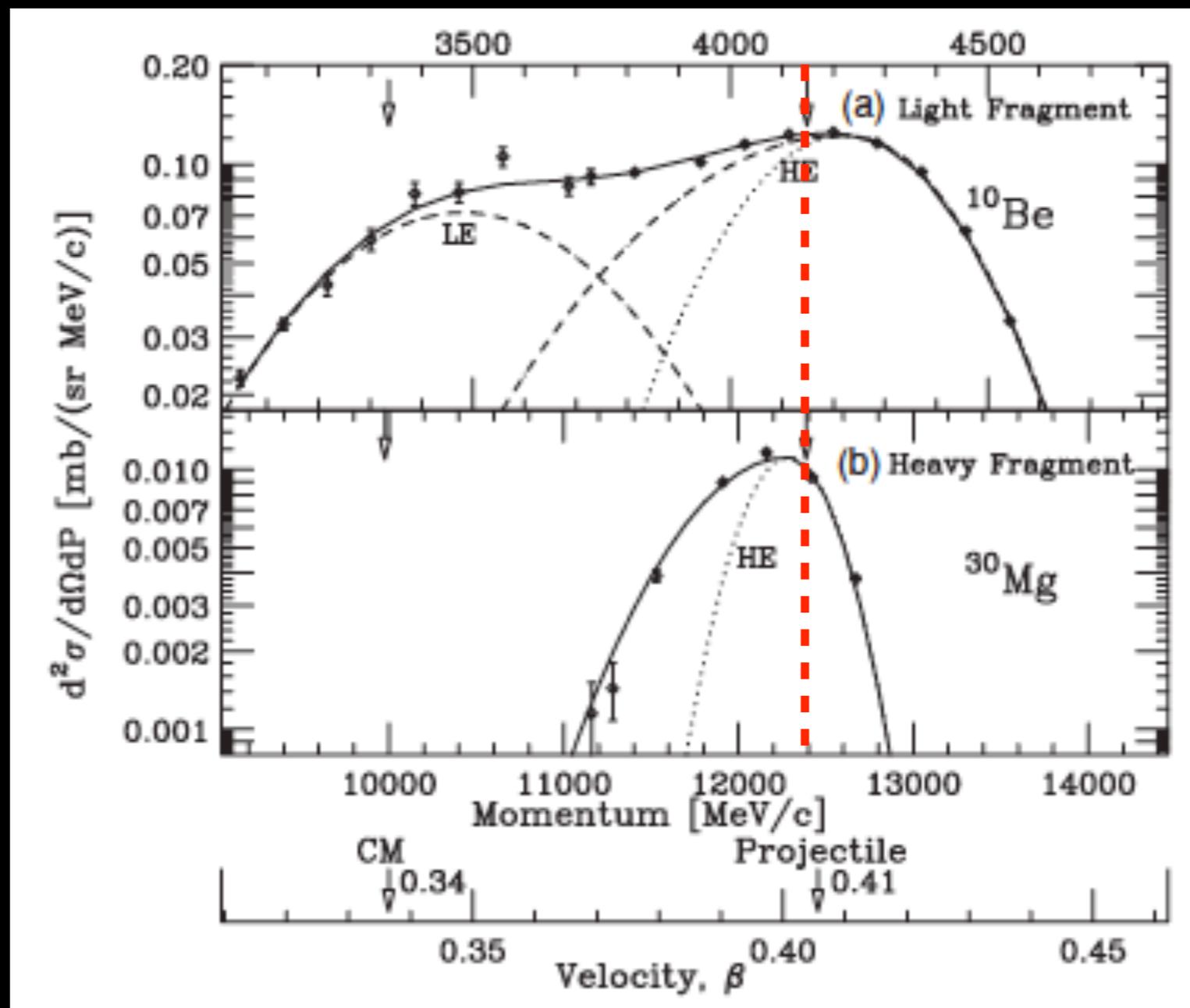


- $-\Delta P_L$ distribution shows parabolic shape and become its maximum 700 MeV/c at $A_F \sim 50$.
- Morrissey/Kaufman formulation is probable for heavier PLFs.

Acceleration effect

- at $E = 90$ MeV/u

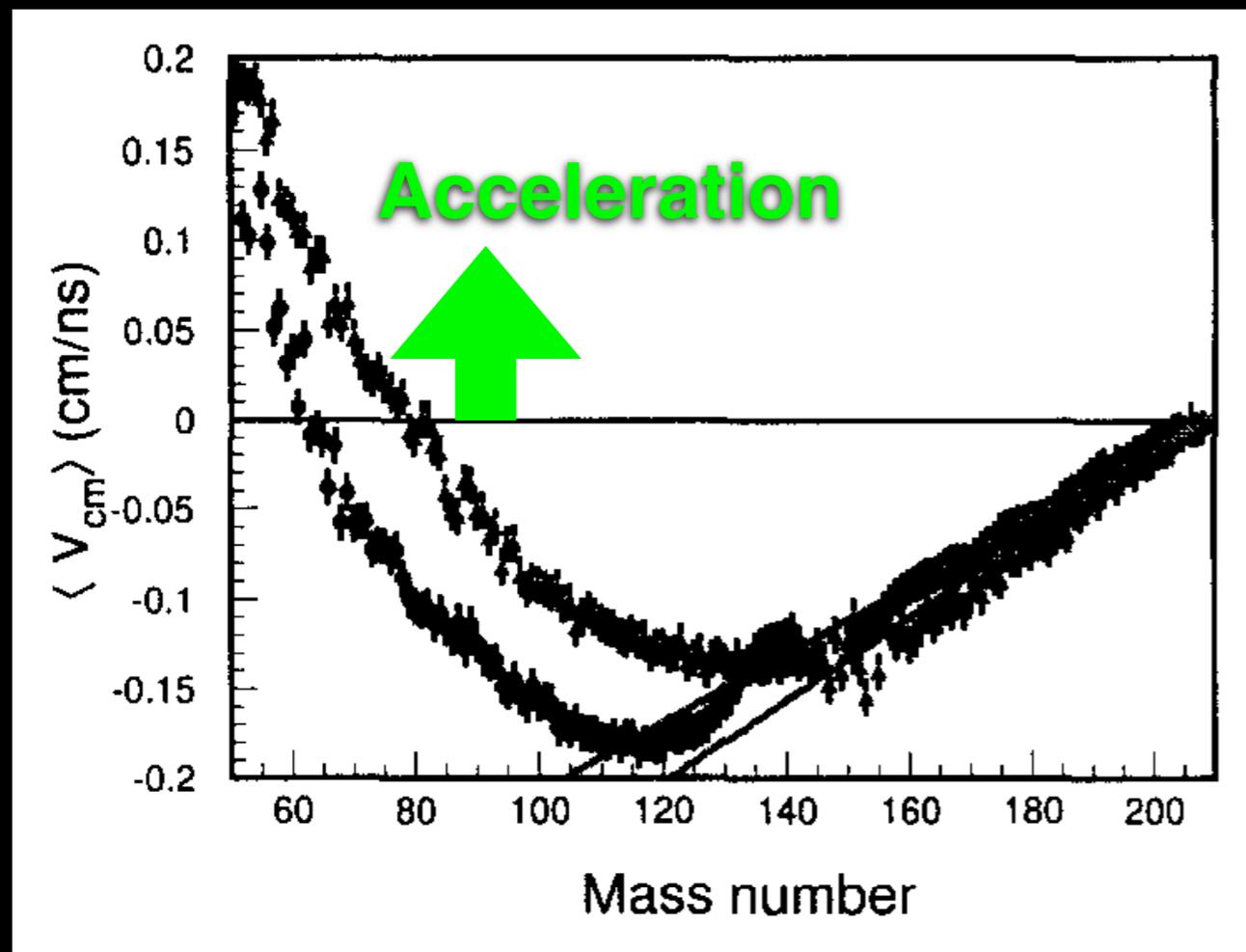
- $^{40}\text{Ar} + ^9\text{Be} \rightarrow ^9\text{Be}$



Acceleration effect

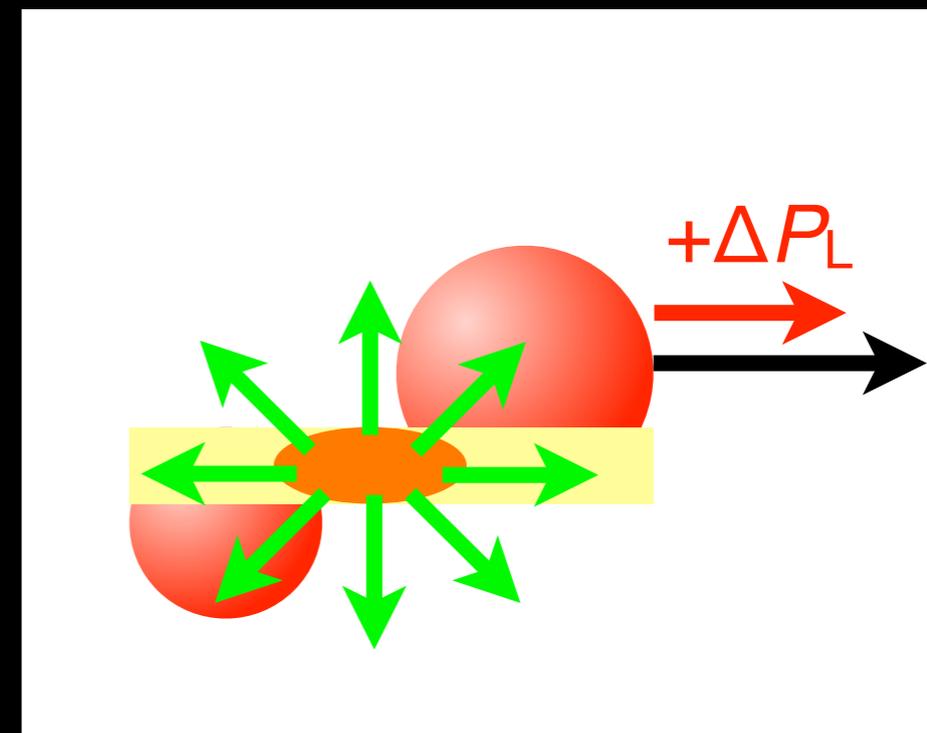
- Tool to investigate EOS

^{208}Pb (0.5, 1.0 GeV/u) + Ti



J. Benlliure et al., NP A 734 (2004) 609.

Participant blast pushes spectator.

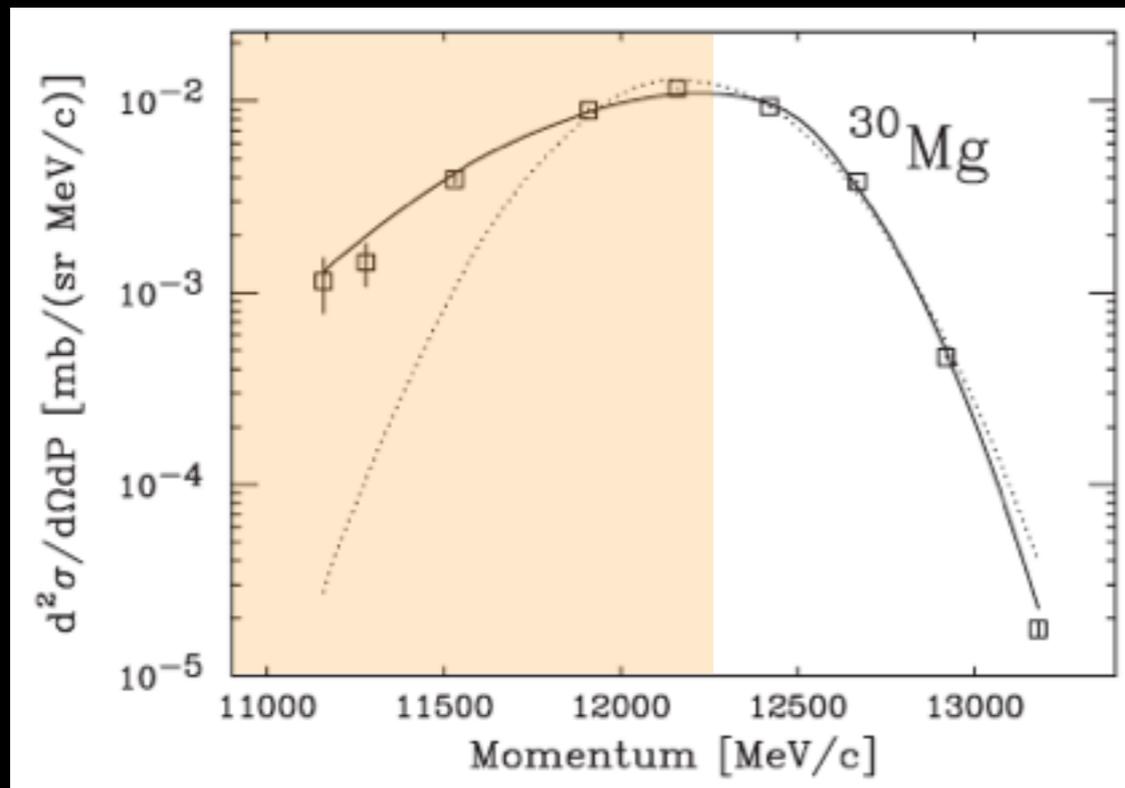


L. Shi et al., PR C 64 (2001) 034601.

P_T distribution

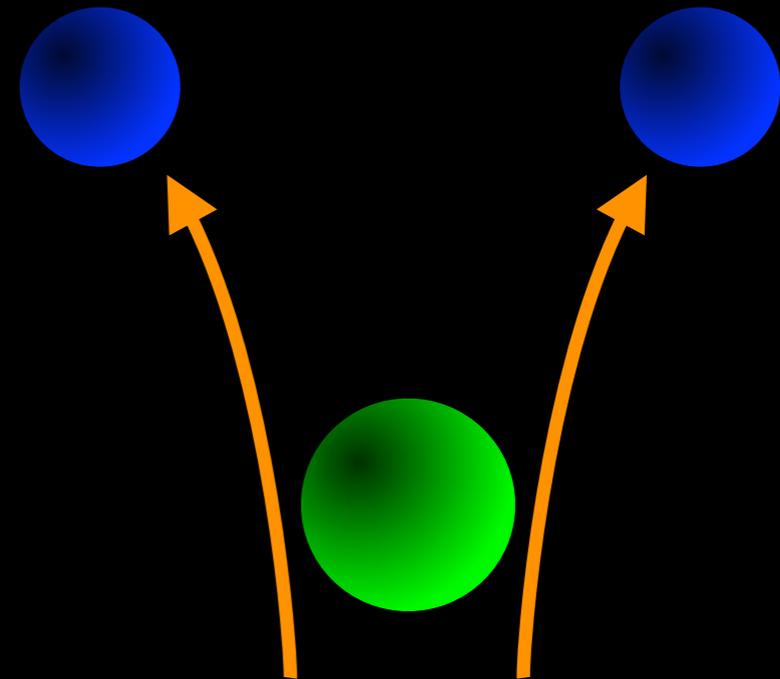
P_T distribution

1) Contamination of another process



Dispersion would depend on P_L .

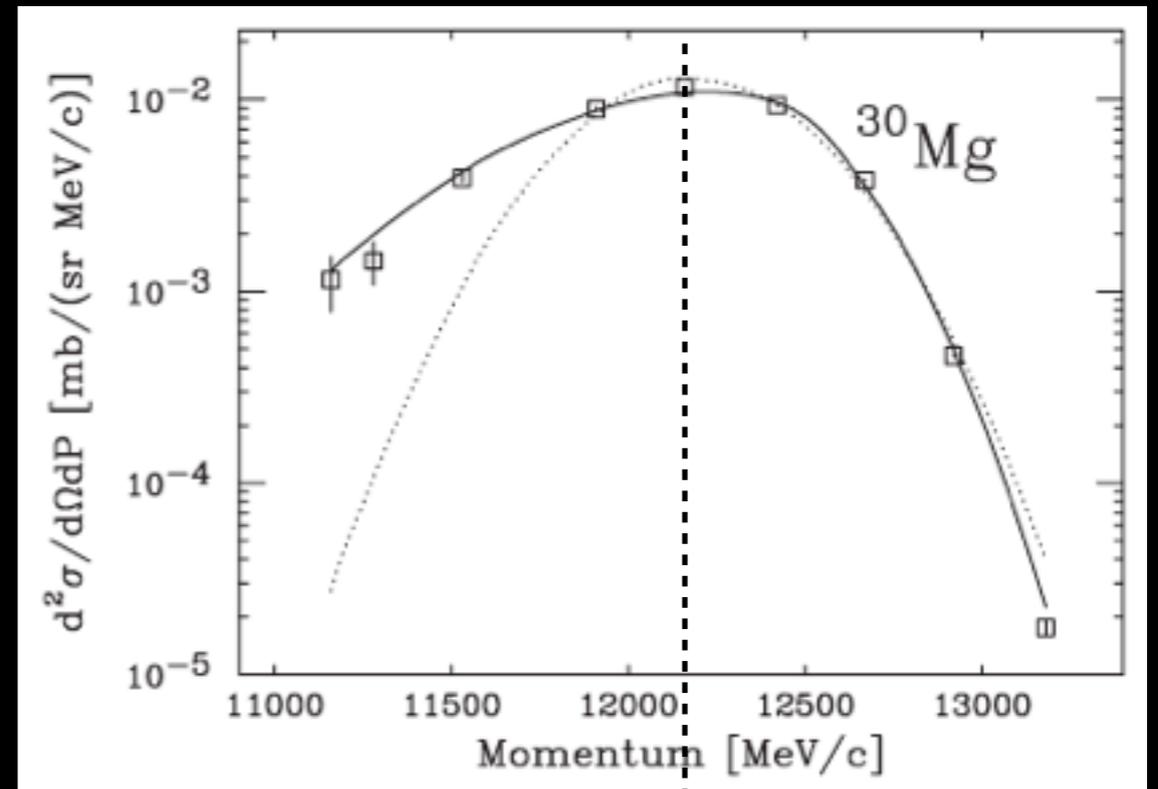
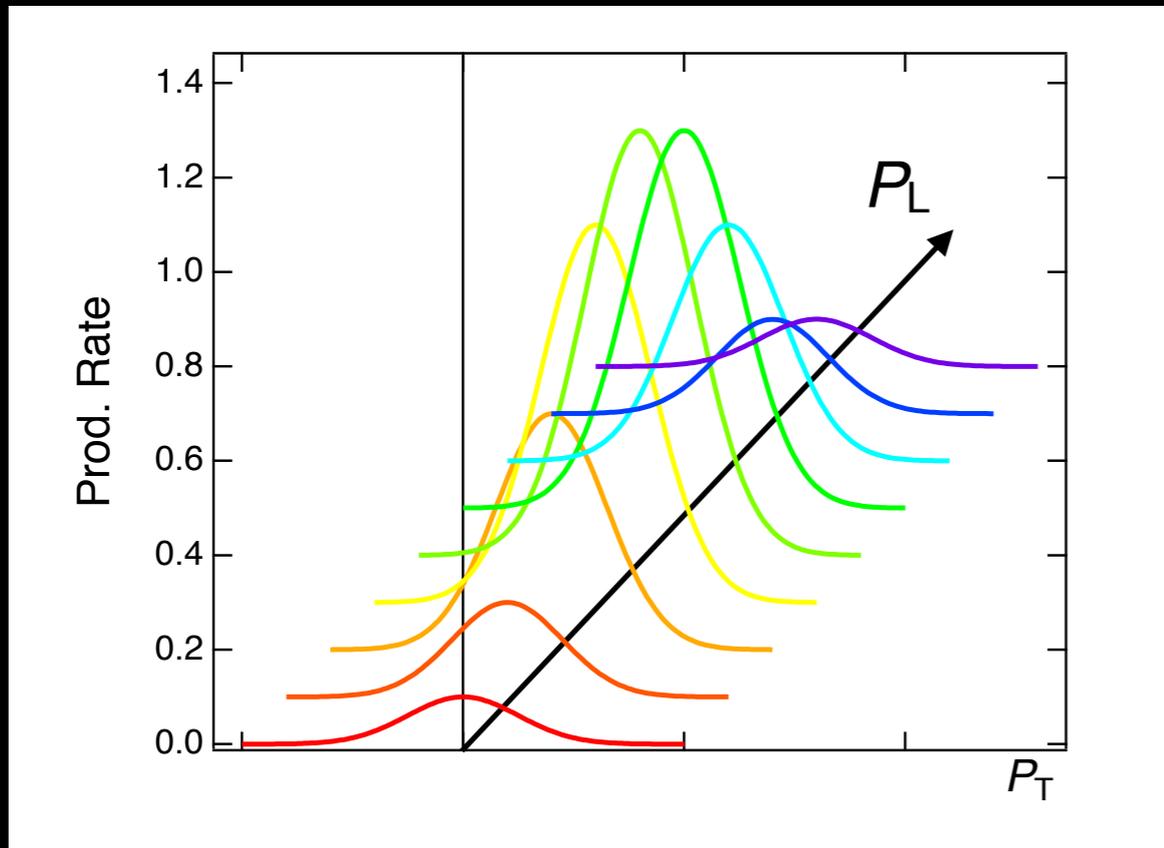
2) Orbital deflection with heavy target



Off-centered P_T dist.

Meas. of P_T distribution

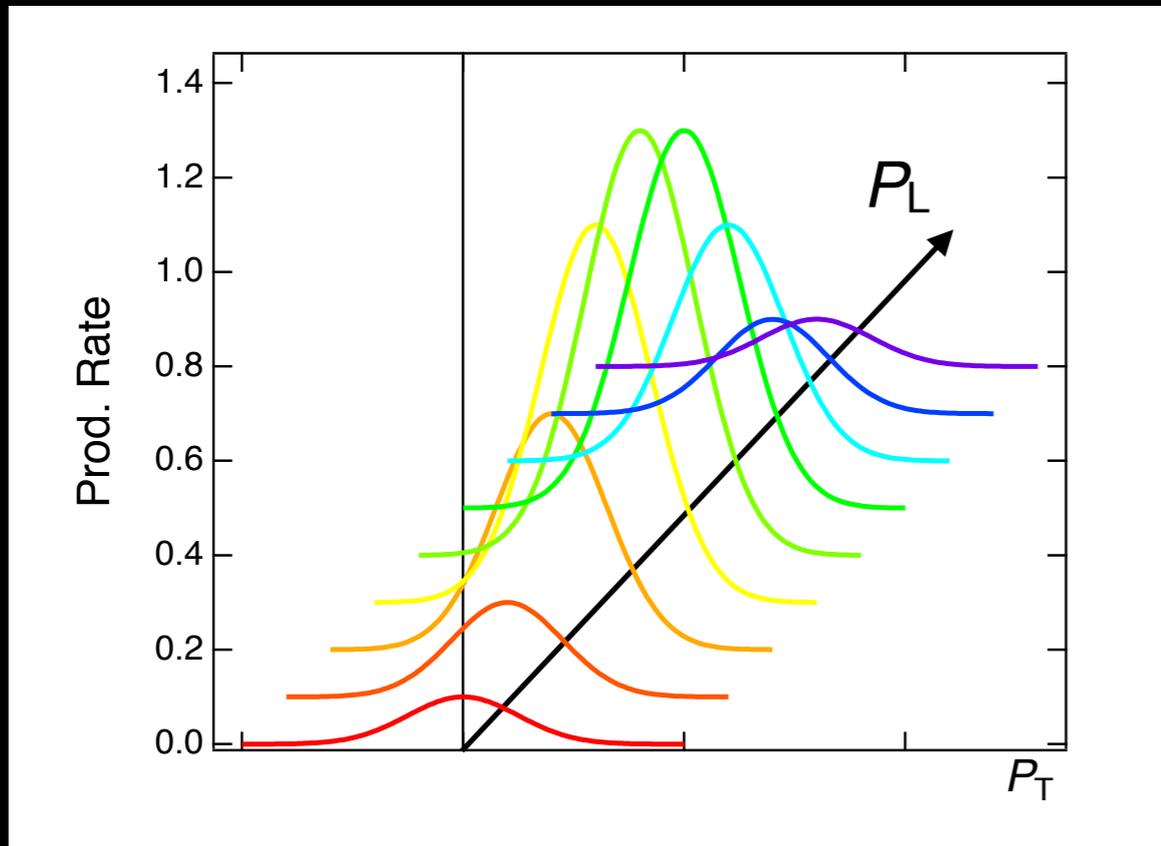
- as a function of P_L



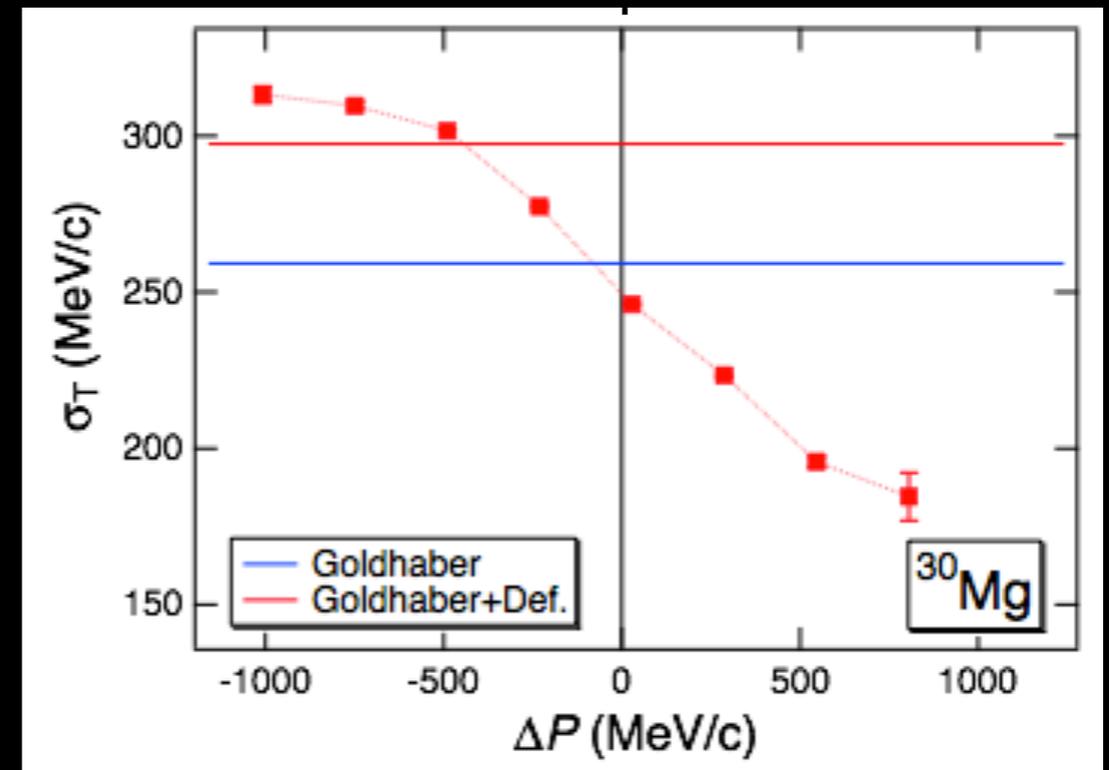
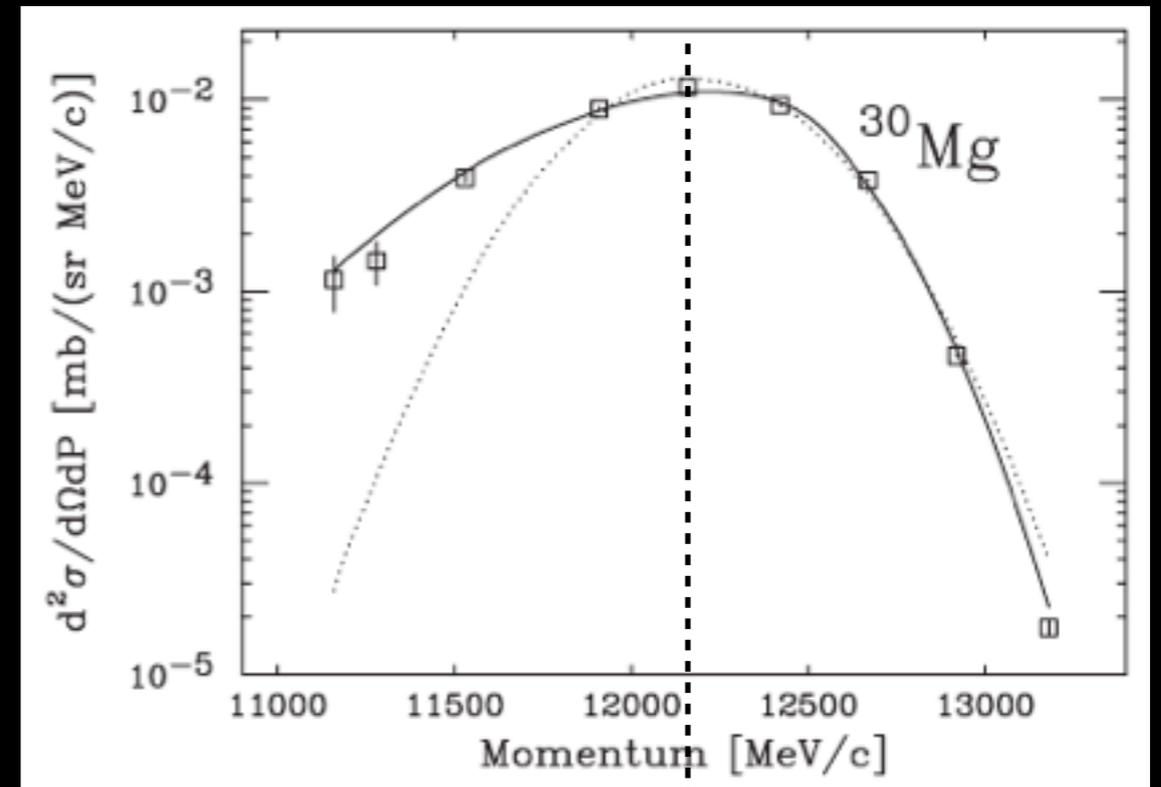
Dispersion (σ_T) observed at each P_L .

Meas. of P_T distribution

- as a function of P_L



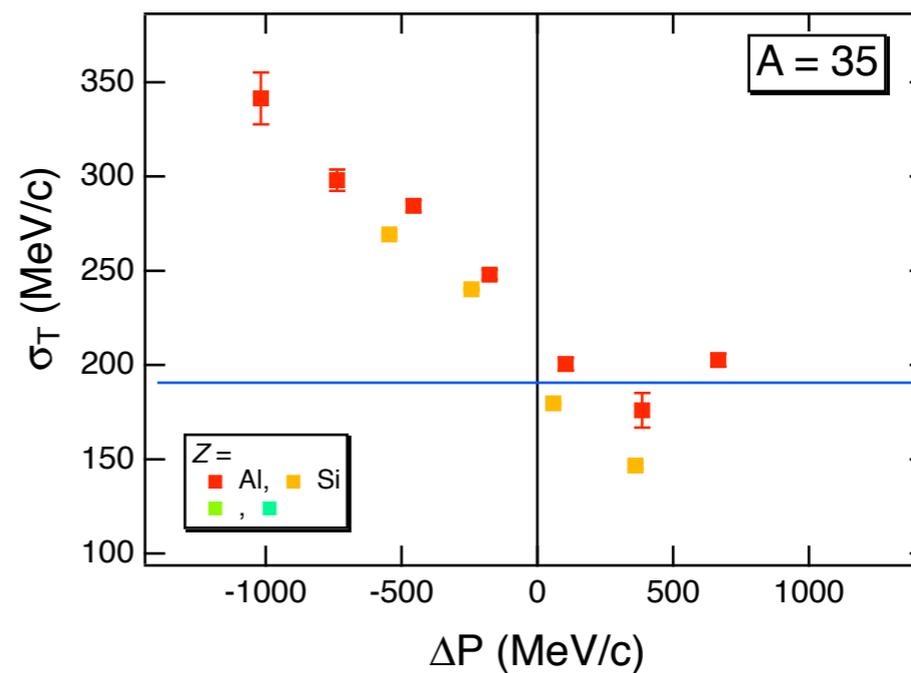
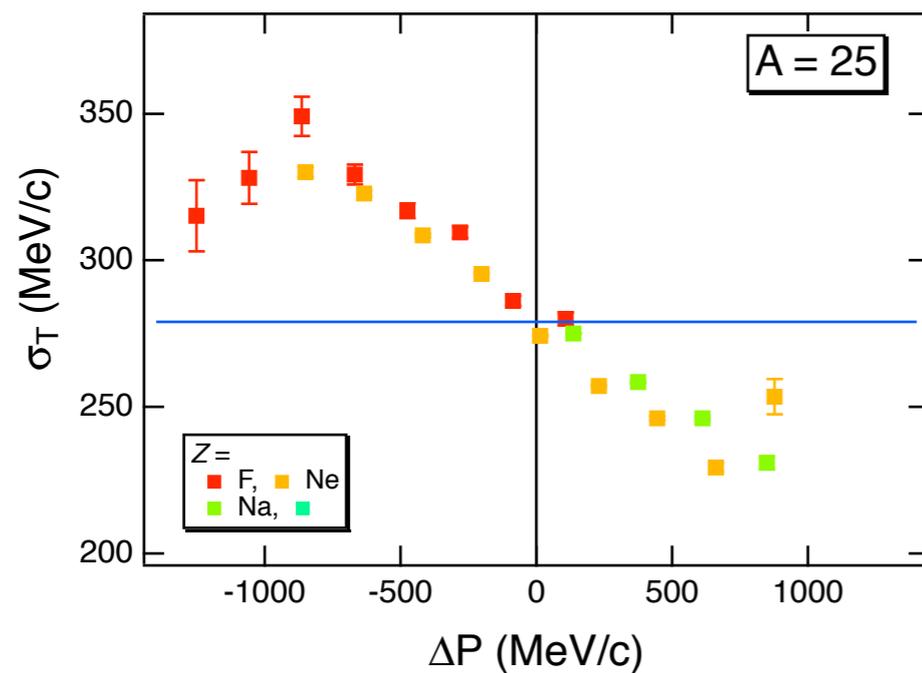
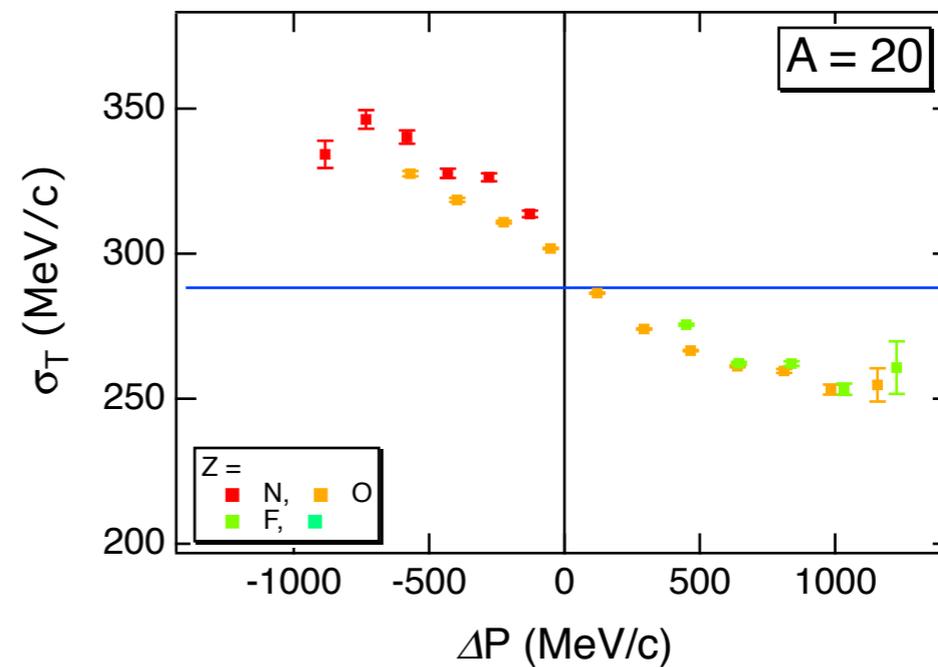
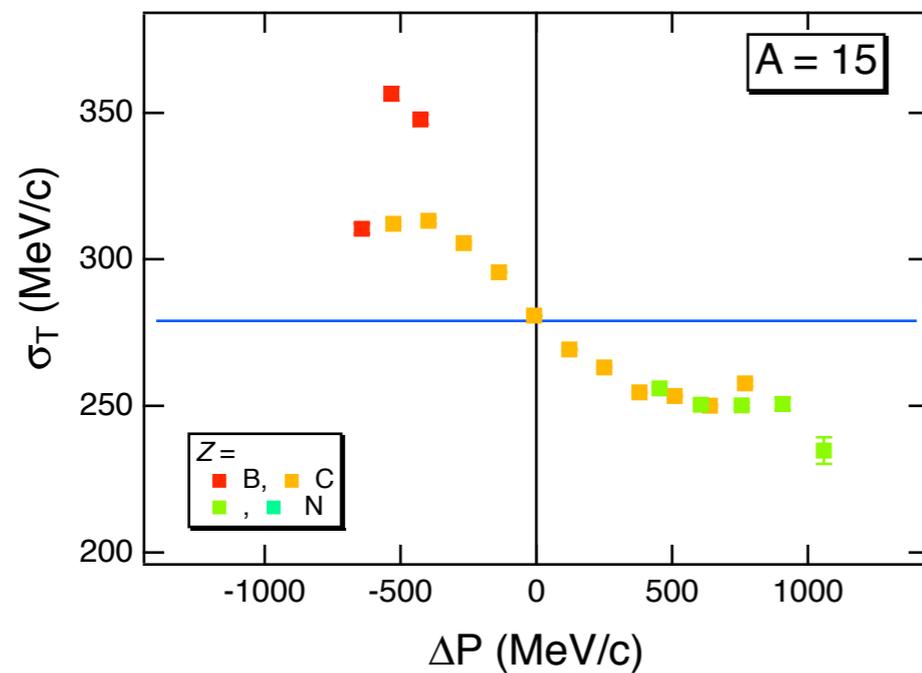
Dispersion (σ_T) observed at each P_L .



Correlation between σ_T and P_L

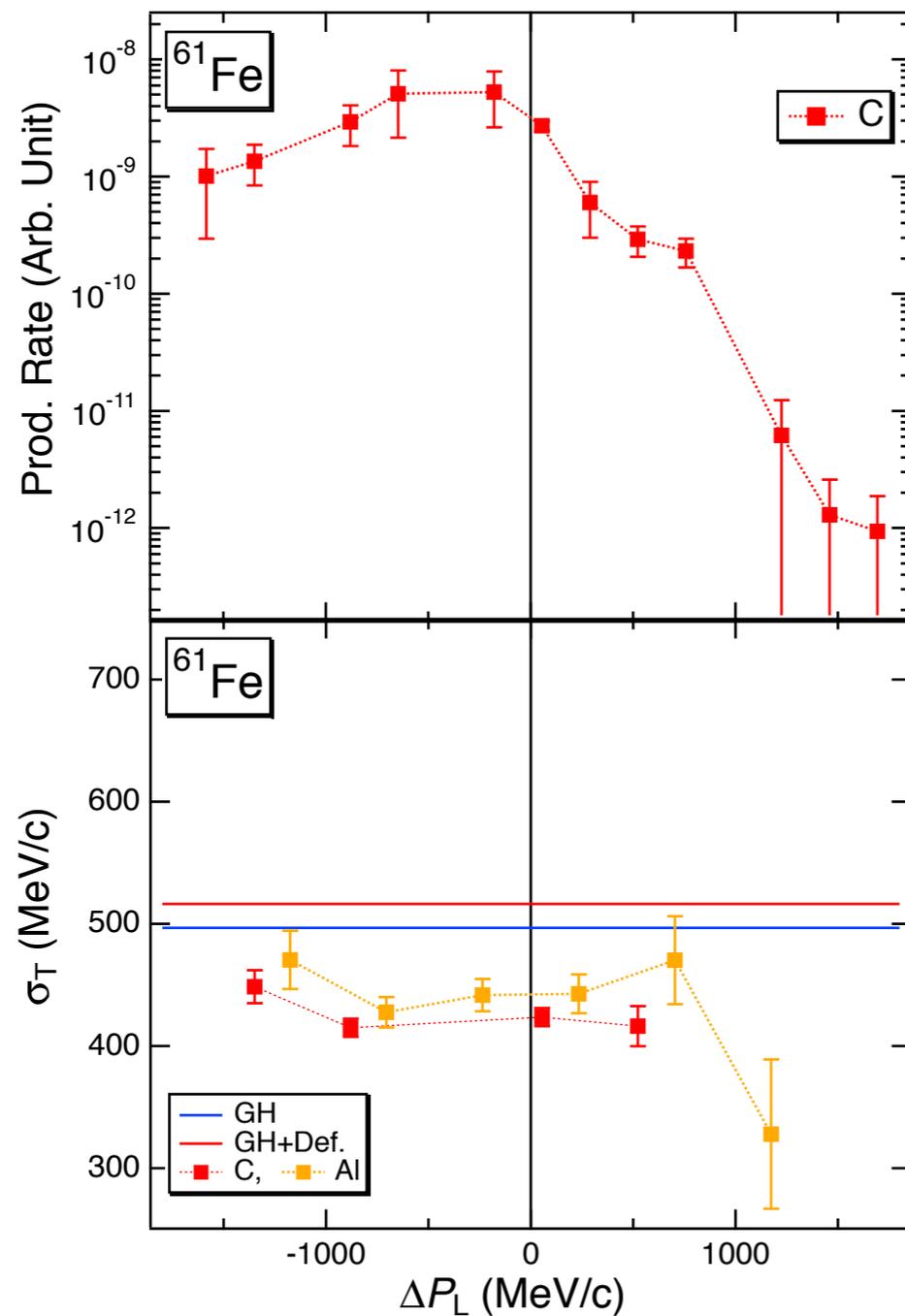
- $^{40}\text{Ar}+^9\text{Be}@95\text{ MeV/u}$

σ_T decrease monotonously.



Correlation between σ_T and P_L

- $^{84}\text{Kr}+^{12}\text{C}@290\text{ MeV/u}$

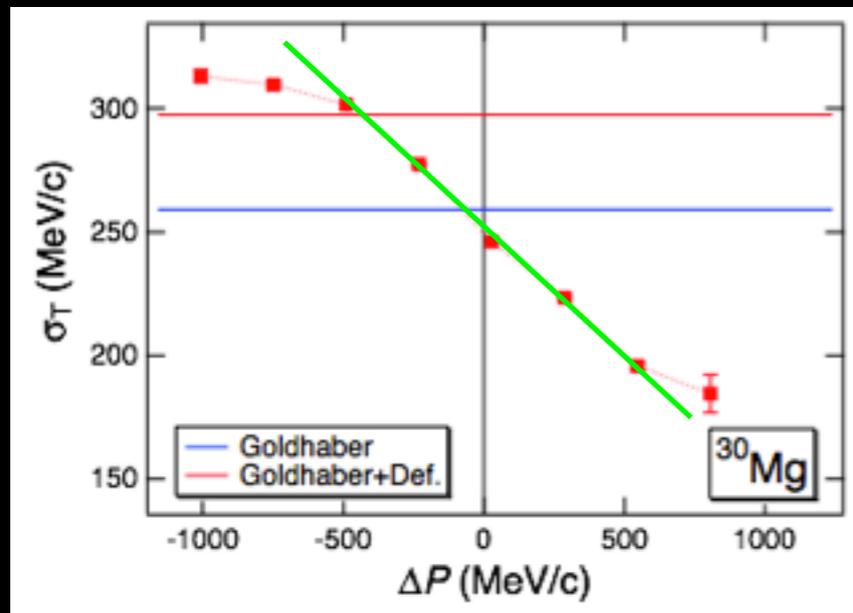


1. $\sigma_T \sim \text{const.}$

2. $\sigma_T < \sigma_L$

Correlation between σ_T and P_L

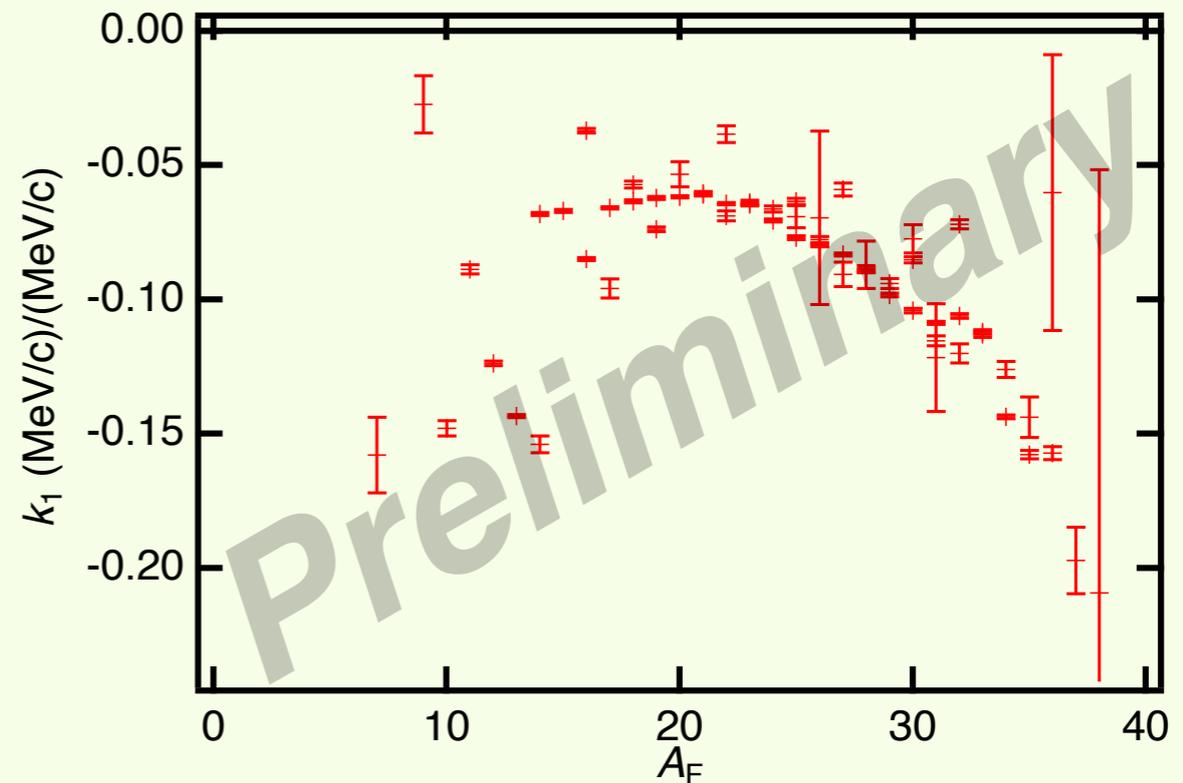
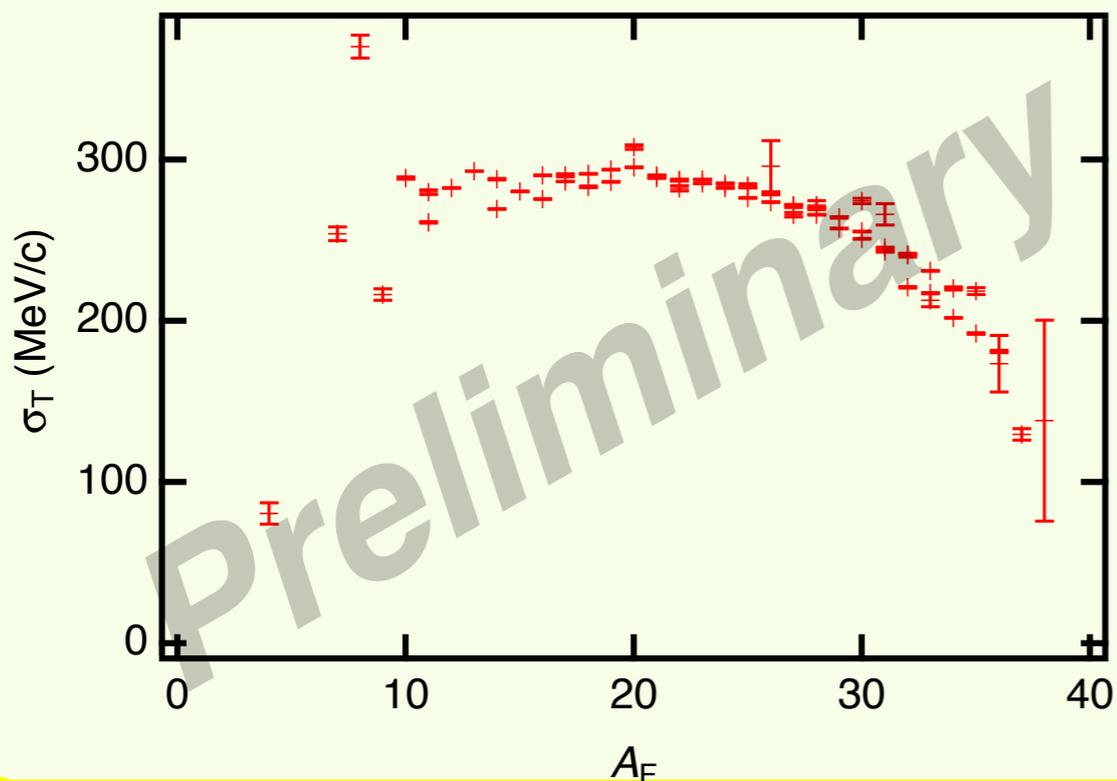
- Analysis by linear function



σ_T decrease monotonously.

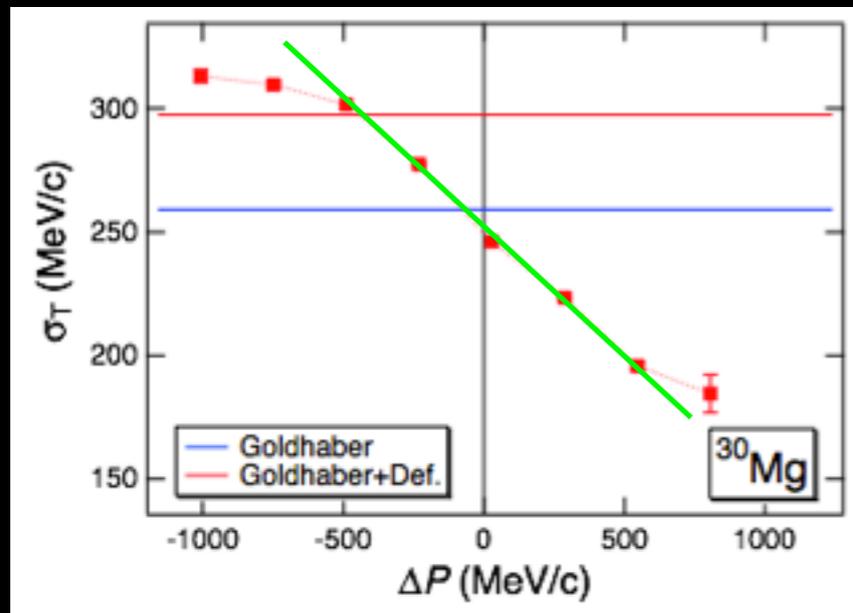
Fitting function :

$$\sigma_T = k_0 + k_1 \Delta P$$



Correlation between σ_T and P_L

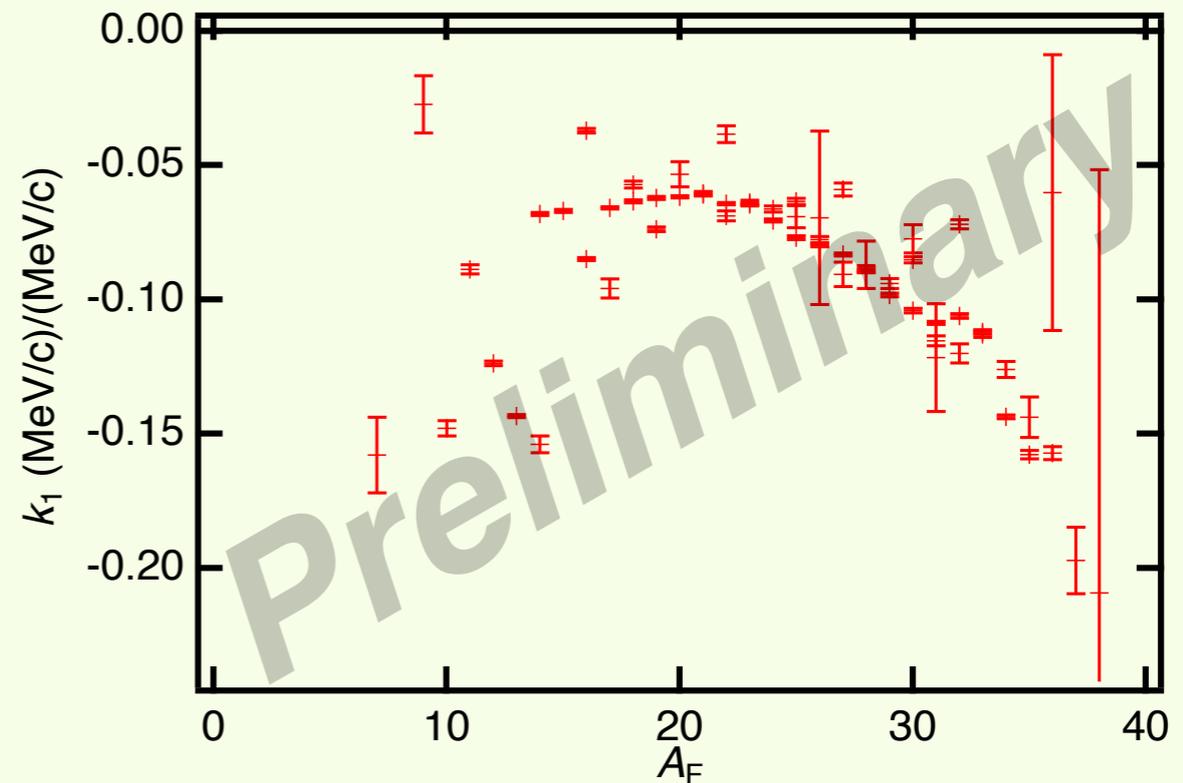
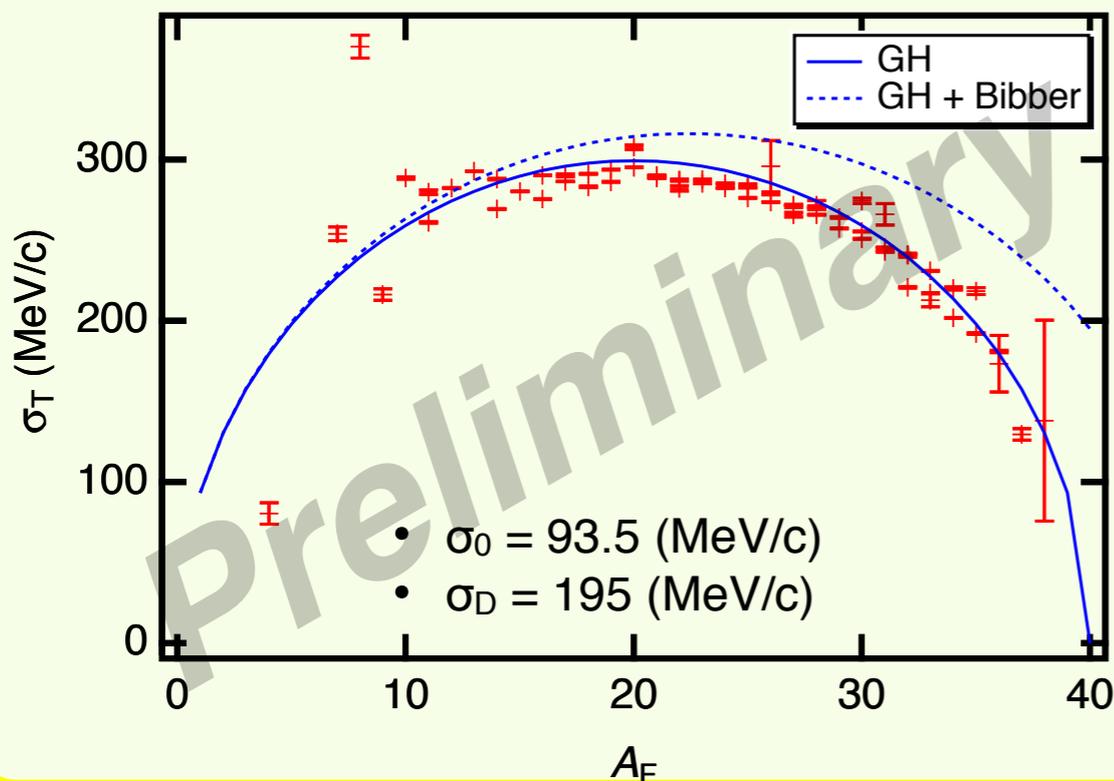
- Analysis by linear function



σ_T decrease monotonously.

Fitting function :

$$\sigma_T = k_0 + k_1 \Delta P$$

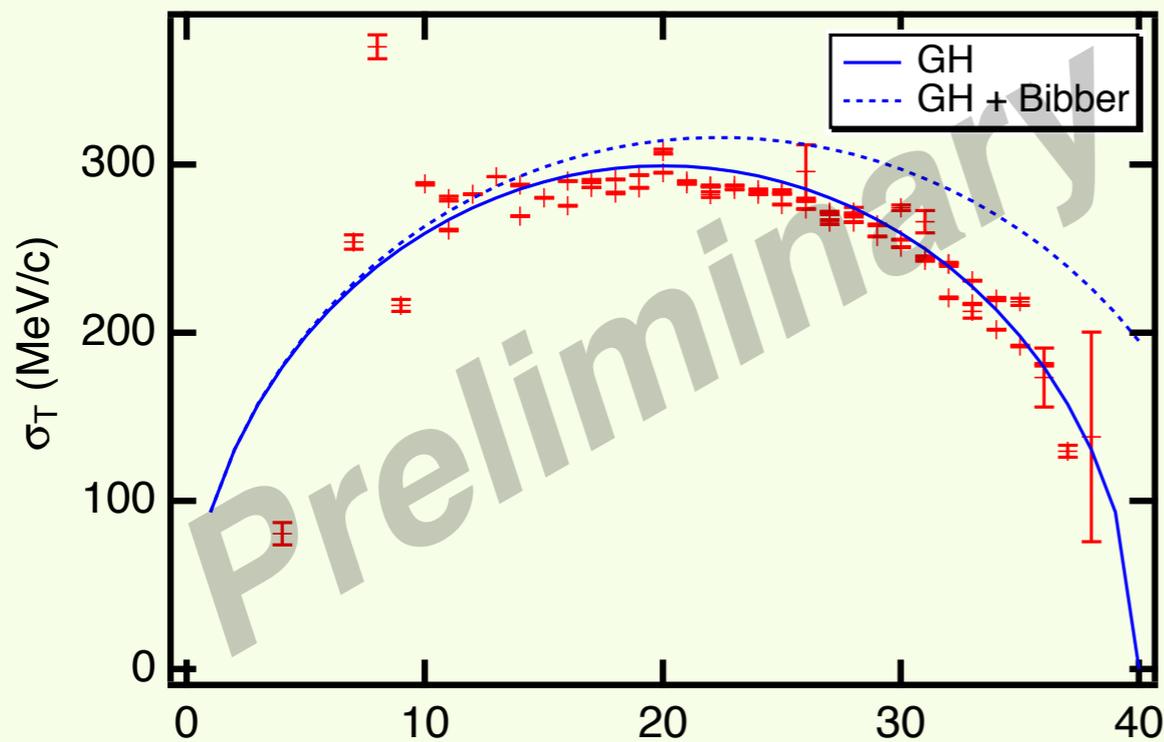


Dispersion of P_T at P_0

- ^{40}Ar beam

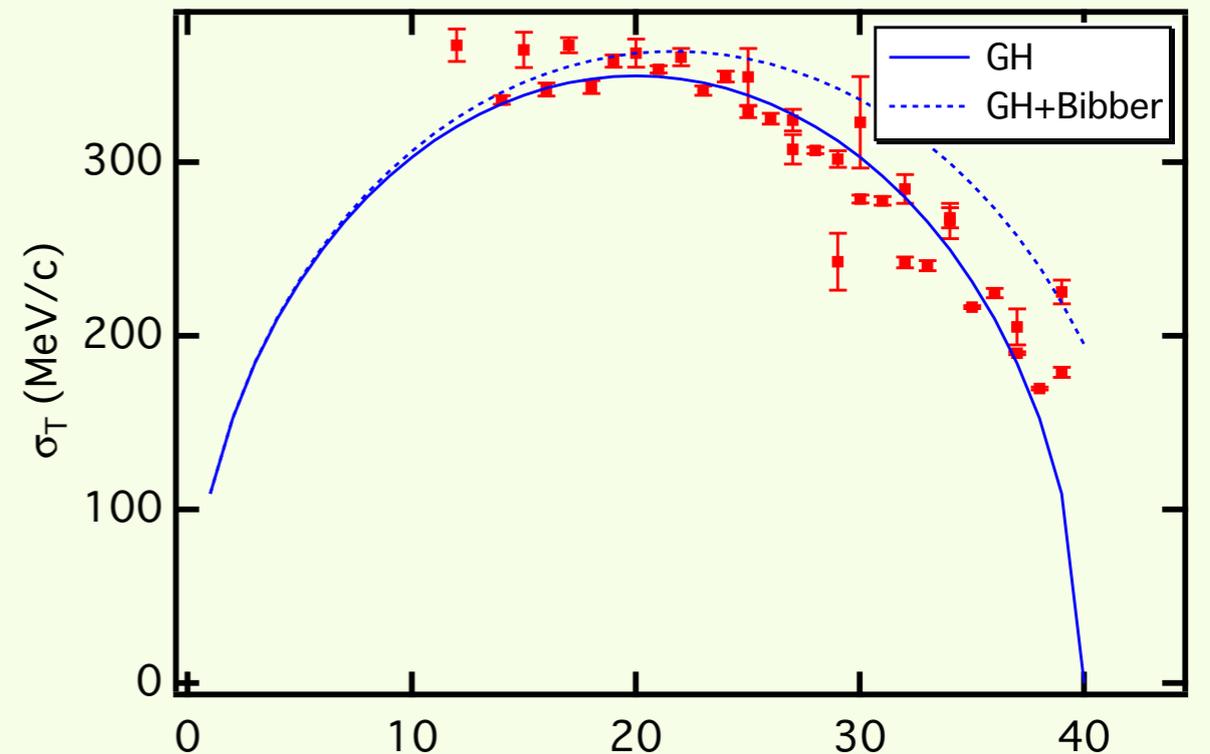
• $^{40}\text{Ar}+^9\text{Be}@95\text{ MeV/u}$

• $^{40}\text{Ar}+^{27}\text{Al}@290\text{ MeV/u}$



A_F

- $\sigma_0 = 93.5$ (MeV/c)
- $\sigma_D = 195$ (MeV/c)



A_F

- $\sigma_0 = 109.3$ (MeV/c)
- $\sigma_D = 195$ (MeV/c)

In case of Ar beam with light targets,

1) P_T distribution is well reproduced only by GH formulation.

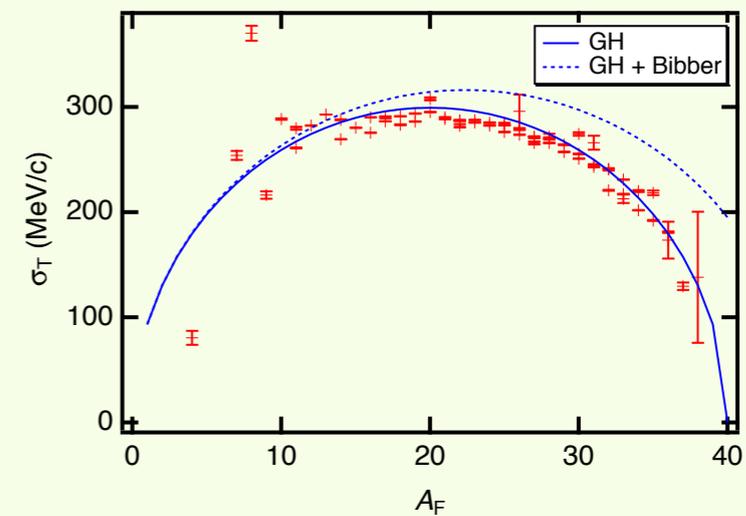
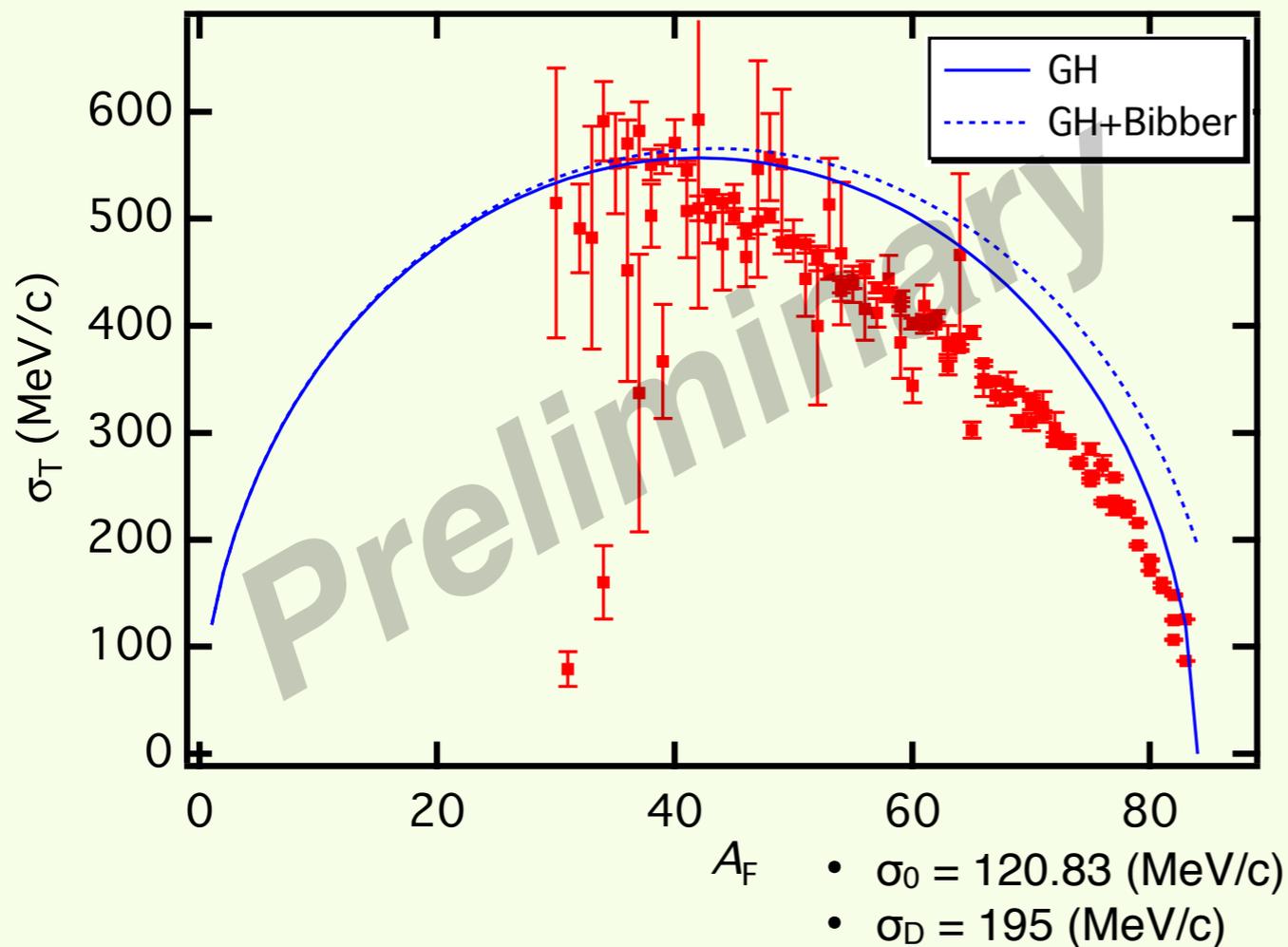
2) $\sigma_T \sim \sigma_{\text{High}}$

Dispersion of P_T at P_0

- ^{84}Kr beam

• $^{84}\text{Kr}+^{12}\text{C}@290\text{ MeV/u}$

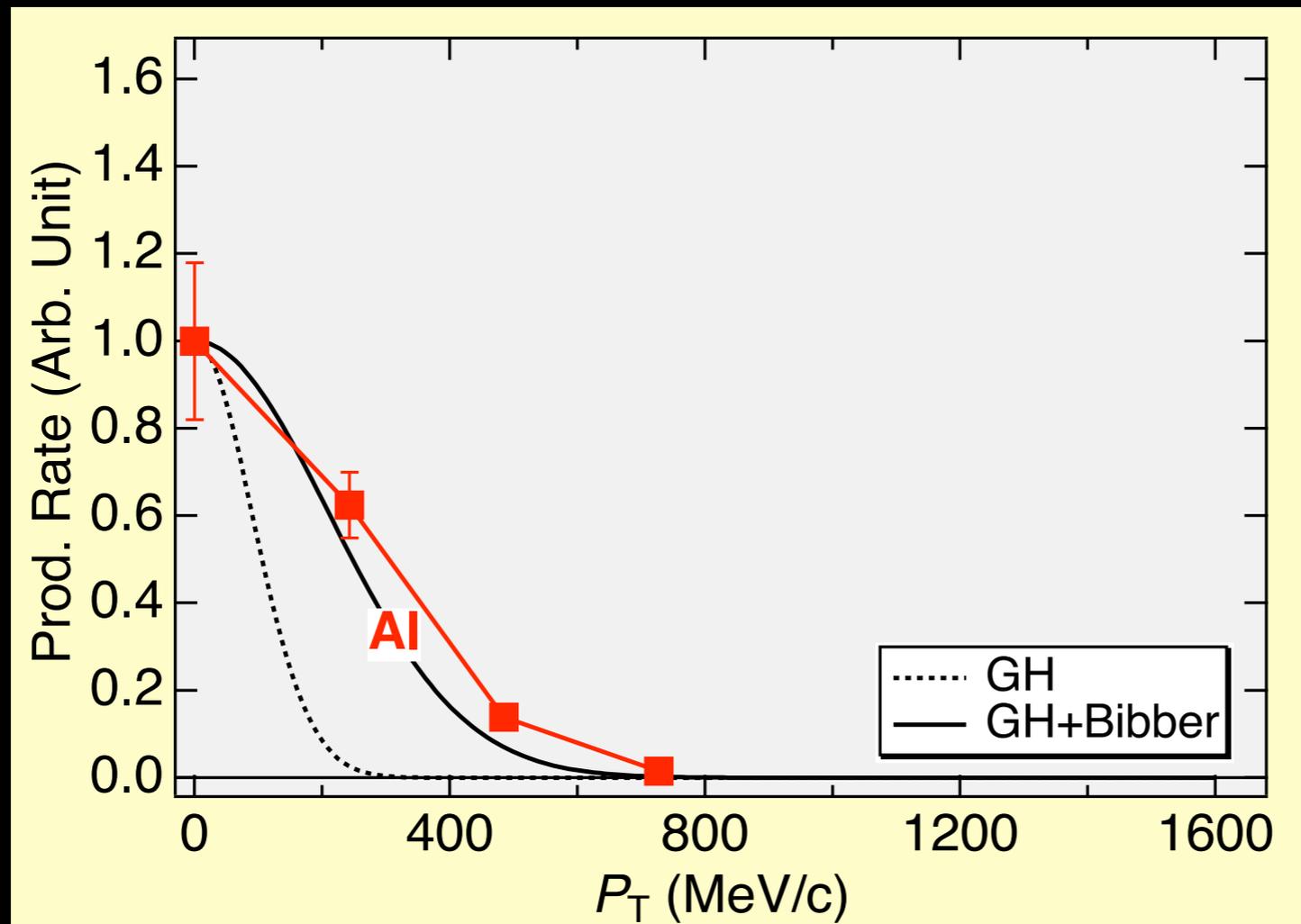
• $^{40}\text{Ar}+^{27}\text{Al}@290\text{ MeV/u}$



In case of Kr beam with light targets,
 P_T distribution is narrower than P_L distribution.

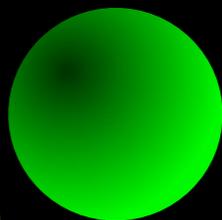
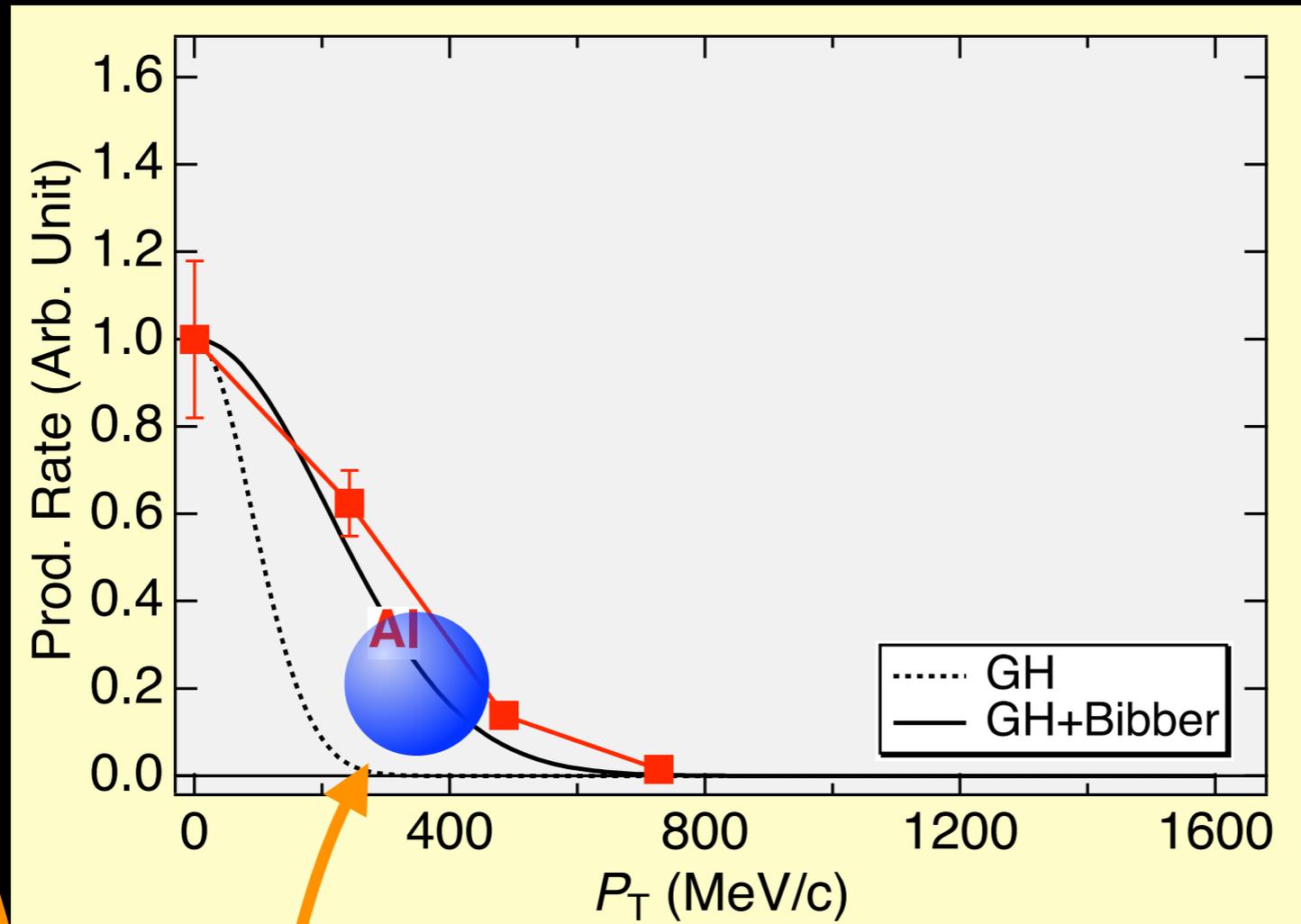
In case of heavier target

• $^{40}\text{Ar} + \text{Al, Nb, Tb, Au} \rightarrow ^{39}\text{Cl}$



In case of heavier target

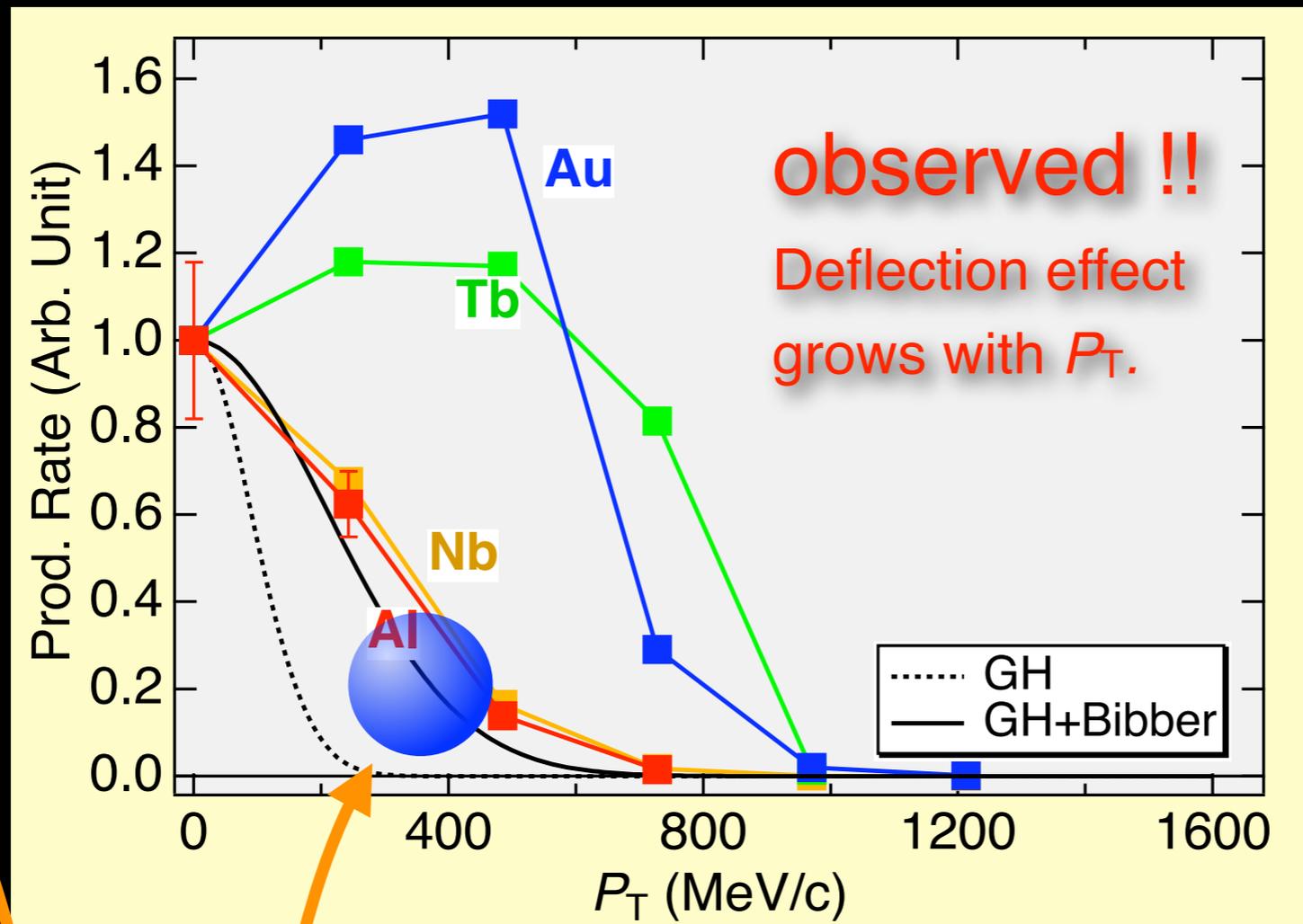
• $^{40}\text{Ar} + \text{Al, Nb, Tb, Au} \rightarrow ^{39}\text{Cl}$



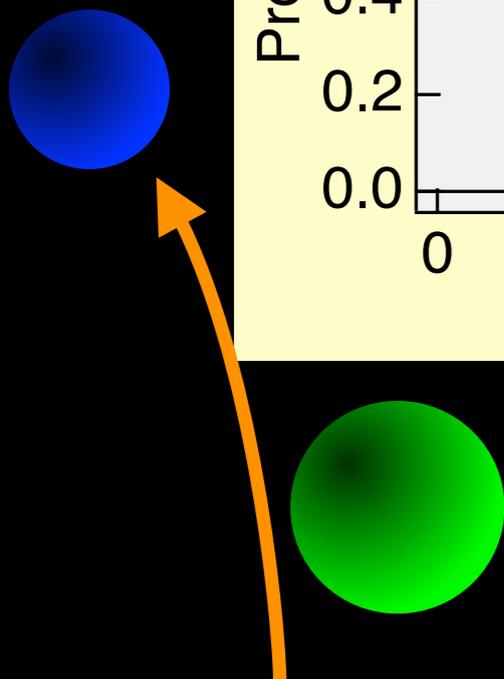
• With **heavy** target, **orbital-deflection** effect is expected.

In case of heavier target

• $^{40}\text{Ar} + \text{Al, Nb, Tb, Au} \rightarrow ^{39}\text{Cl}$



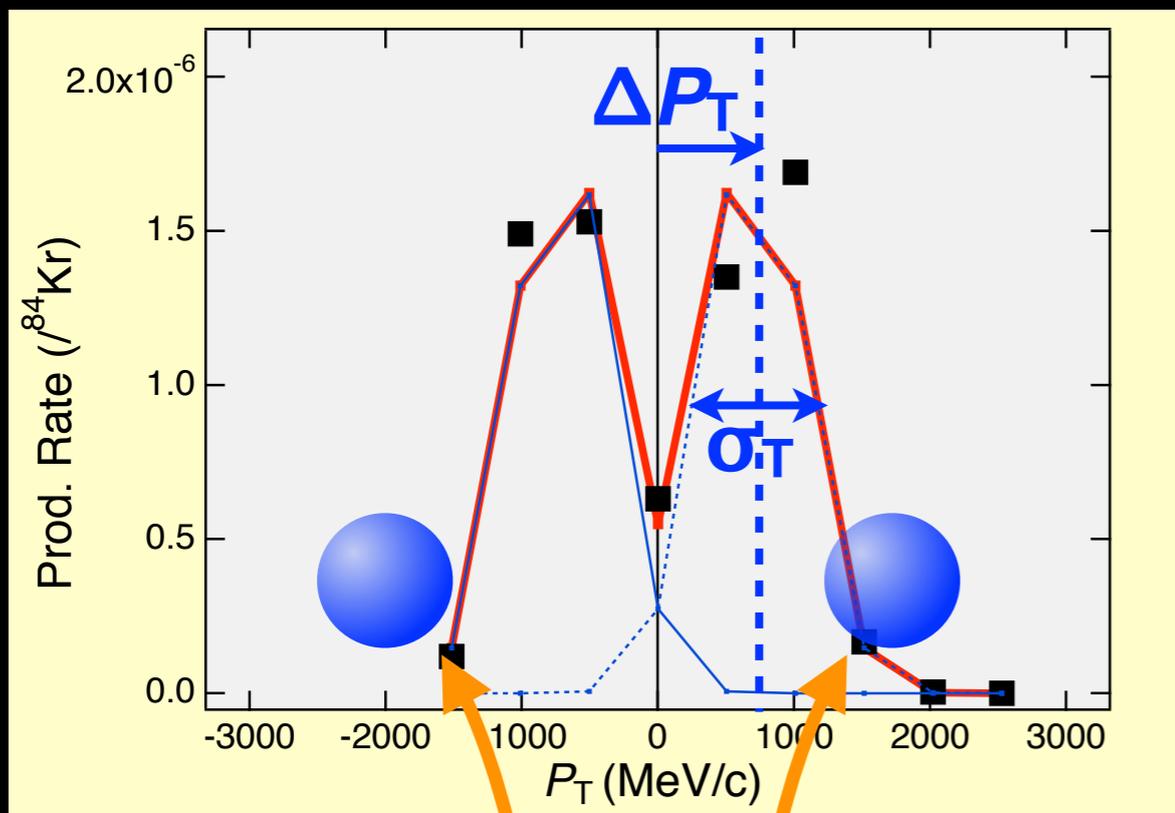
• With **heavy** target, **orbital-deflection** effect is expected.



Analysis of P_T distribution

- Evaluation of deflection effect

• $^{84}\text{Kr} + \text{Au} \rightarrow ^{83}\text{Br}$



Off-centered Gaussian functions

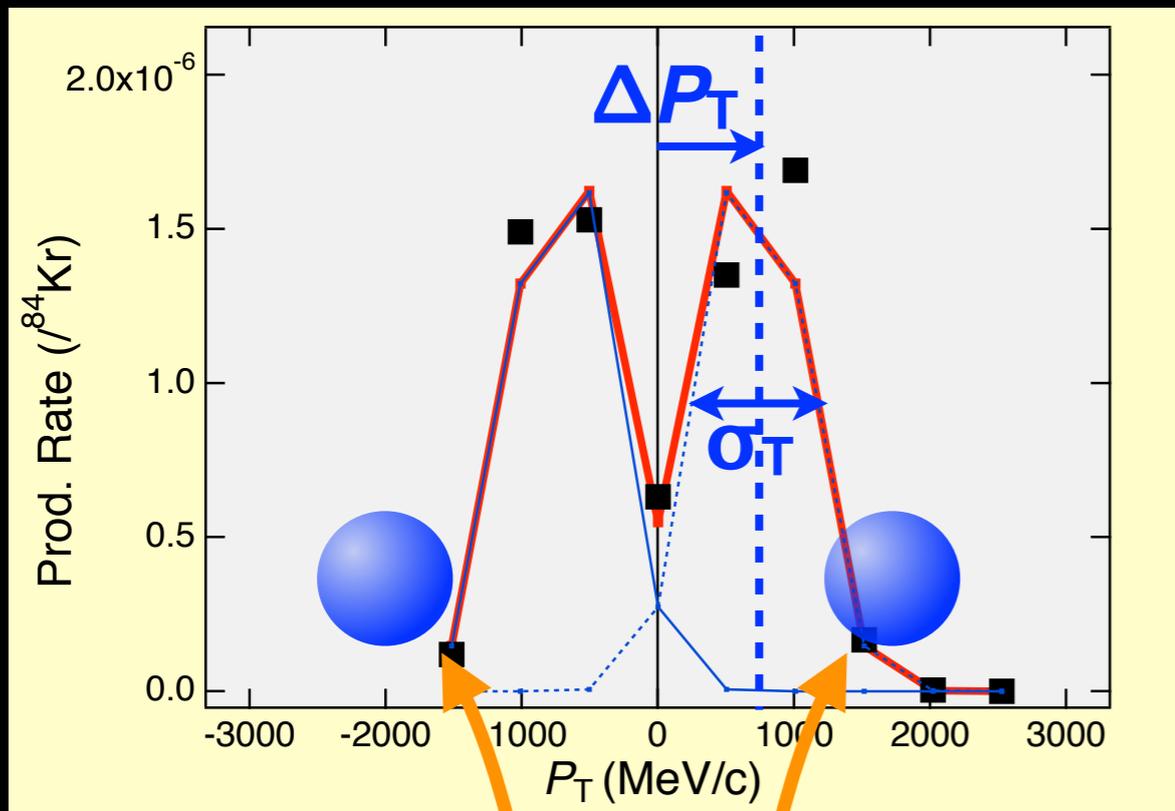
$$Y(P_T) = A \left\{ \exp\left(-\frac{(P_T - \Delta P_T)^2}{2\sigma(P_T)^2}\right) + \exp\left(-\frac{(P_T + \Delta P_T)^2}{2\sigma(P_T)^2}\right) \right\}$$

Let $\sigma(P_T) = \sigma_{\text{GH}}$, then
fitting to provide $A, \Delta(P_T)$.

Analysis of P_T distribution

- Evaluation of deflection effect

• $^{84}\text{Kr} + \text{Au} \rightarrow ^{83}\text{Br}$



Off-centered Gaussian functions

$$Y(P_T) = A \left\{ \exp\left(-\frac{(P_T - \Delta P_T)^2}{2\sigma(P_T)^2}\right) + \exp\left(-\frac{(P_T + \Delta P_T)^2}{2\sigma(P_T)^2}\right) \right\}$$

Let $\sigma(P_T) = \sigma_{GH}$, then
fitting to provide $A, \Delta(P_T)$.

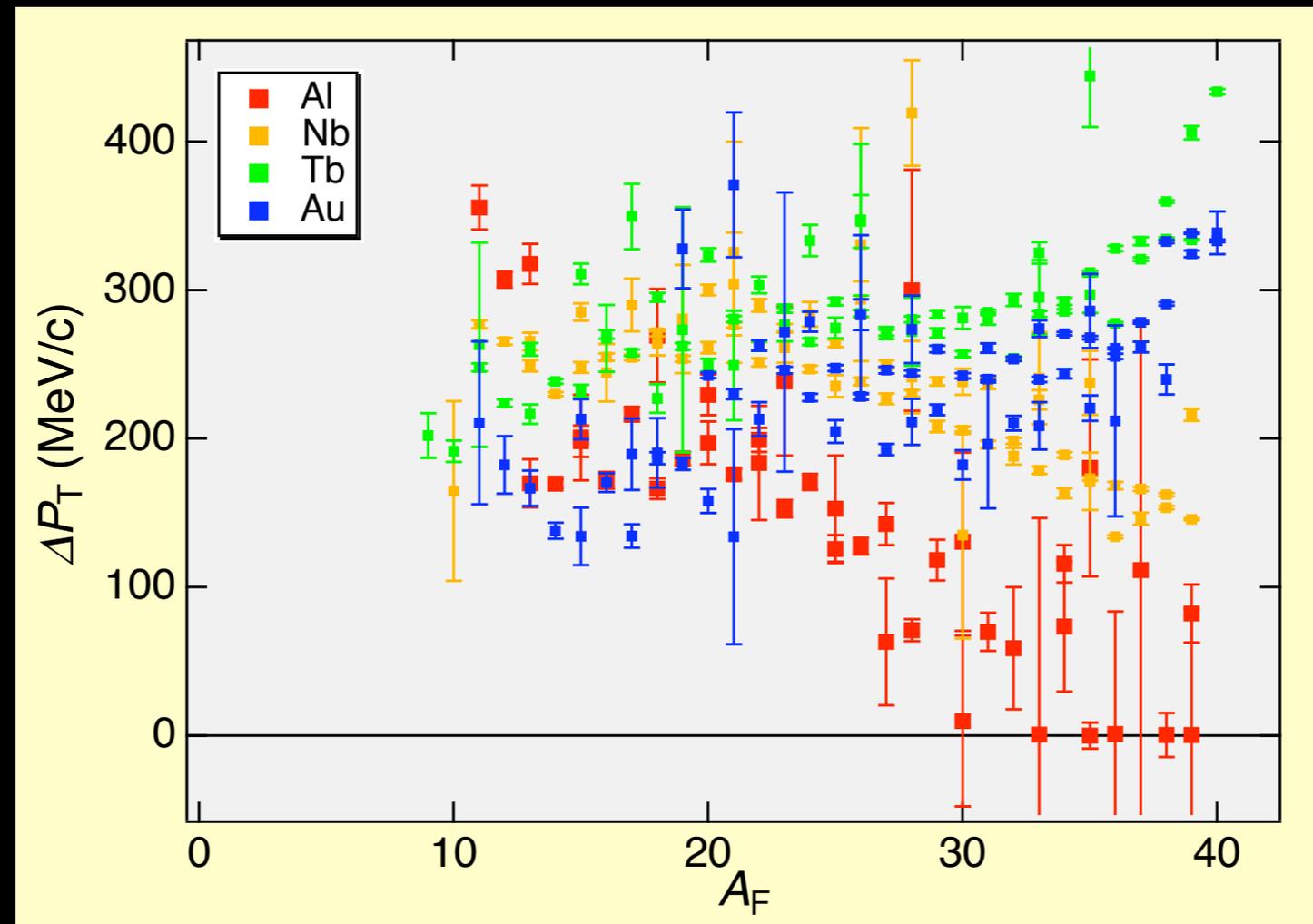
$\Delta\theta = 11.2$ mrad

Grazing angle : 14 mrad

Orbital-deflection effect

- Target dependence with Ar-beam

• $^{40}\text{Ar}+^A_Z$

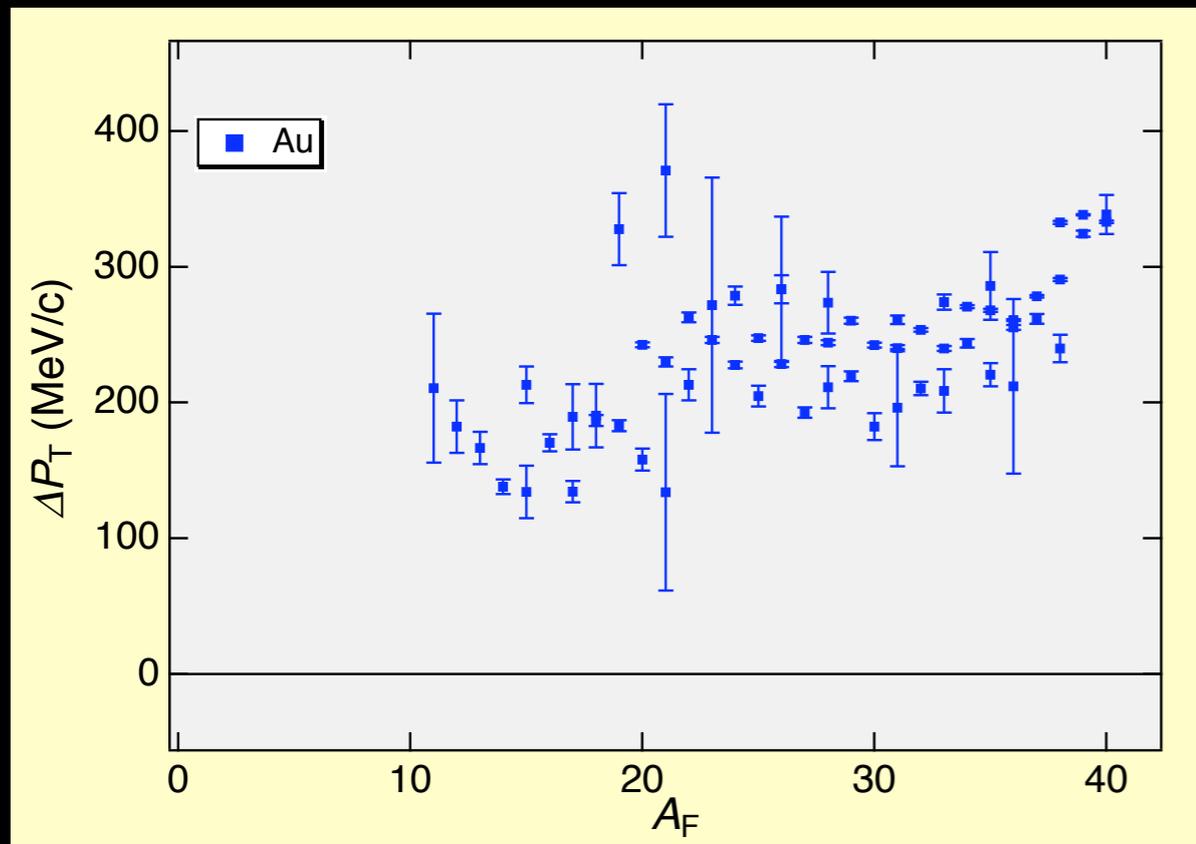


- The orbital-deflection effect grows with target mass.
- The target effect is remarkable for PLFs with $A_T > 20$.

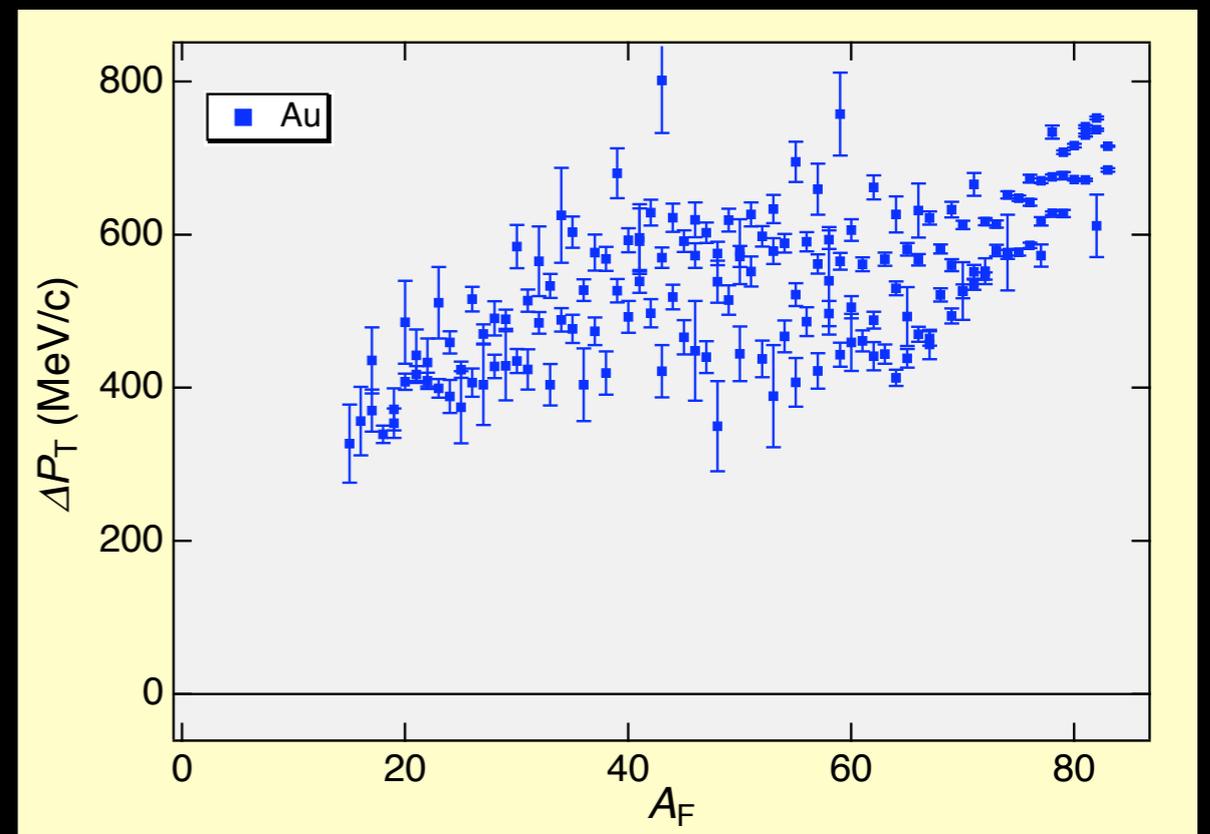
Orbital-deflection effect

- Ar, Kr + Au

• $^{40}\text{Ar} + ^{197}\text{Au}$



• $^{84}\text{Kr} + ^{197}\text{Au}$

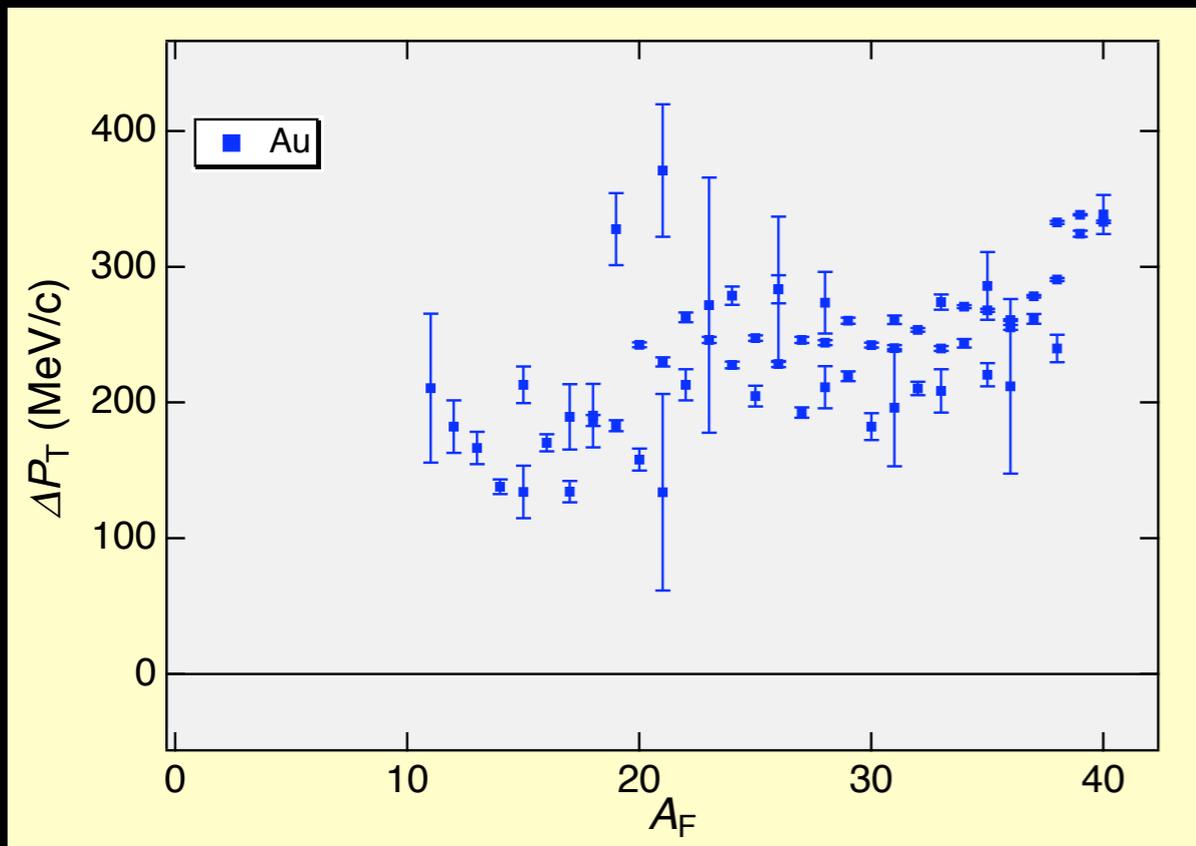


- The orbital-deflection effect is similar for Ar- and Kr-beam.
- The large fluctuation is found at $A_T = 30 \sim 60$.

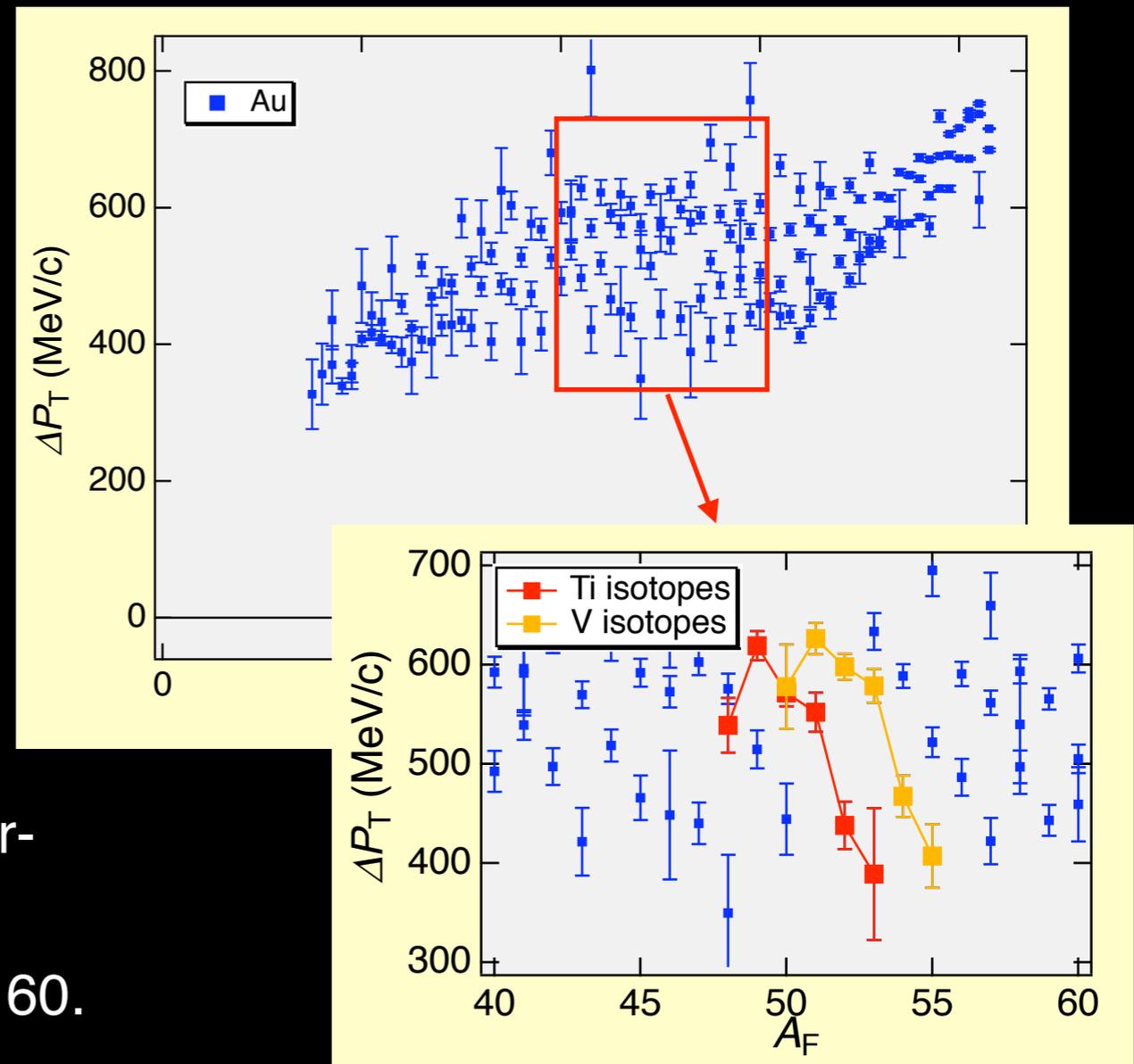
Orbital-deflection effect

- Ar, Kr + Au

• $^{40}\text{Ar} + ^{197}\text{Au}$



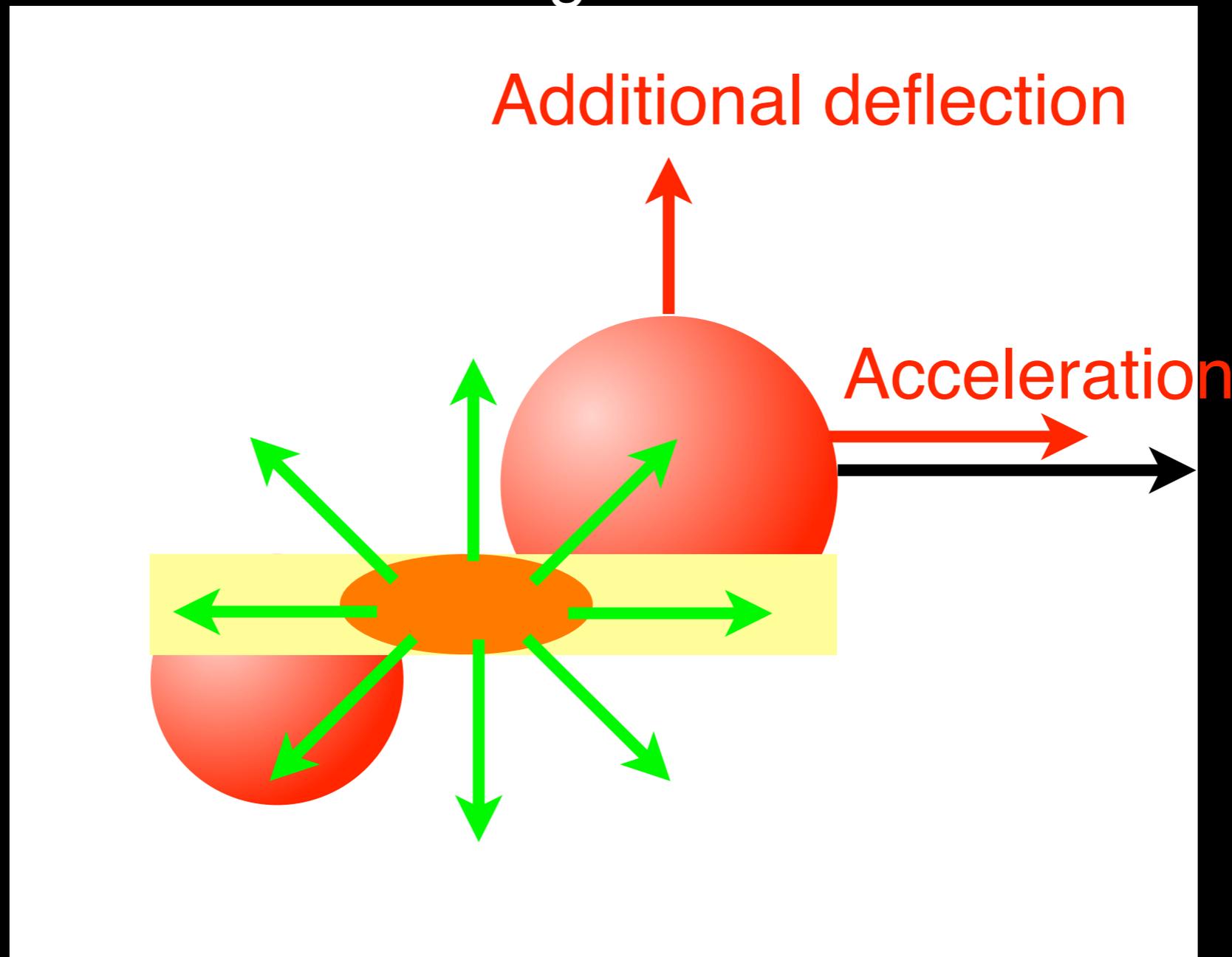
• $^{84}\text{Kr} + ^{197}\text{Au}$



- The orbital-deflection effect is similar for Ar- and Kr-beam.
- The large fluctuation is found at $A_T = 30 \sim 60$.
- The fluctuation comes from isotopic drift.

Participant blast effect in P_T dist.?

For light/intermediate fragments



$\sigma_{\text{Prod.}}$ of fragment

How to obtain σ_{Prod}

- Consideration of ang. acpt.

 - Prod. rate at 0 deg. in **limited ang. acpt.**

 - Integration assuming **reliable P_T distributions**

How to obtain σ_{Prod}

- Consideration of ang. acpt.

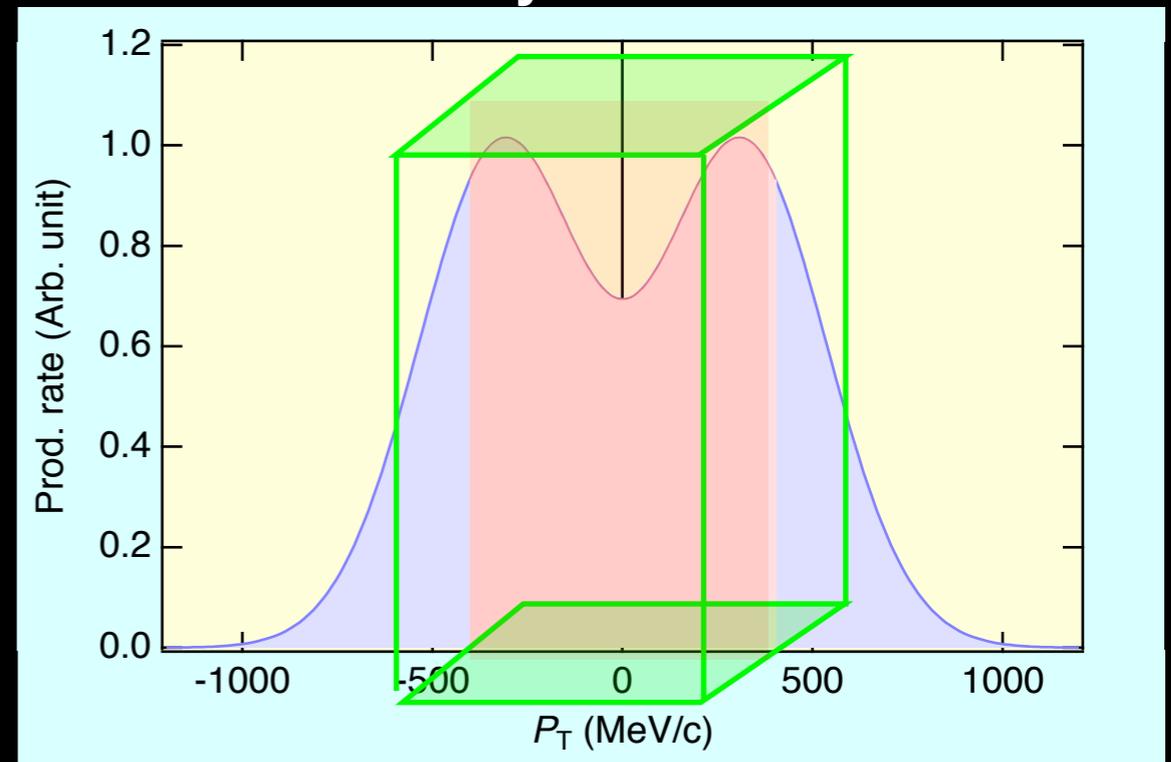
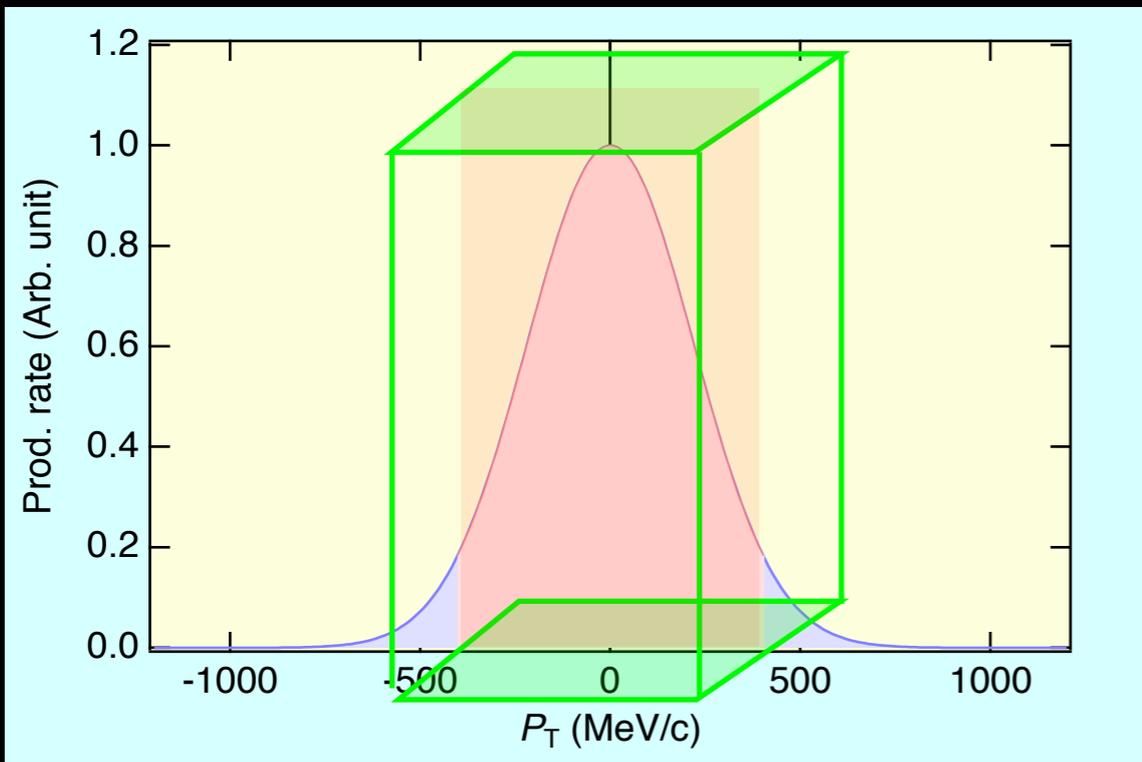
Prod. rate at 0 deg. in **limited ang. acpt.**

→ Integration assuming **reliable P_T distributions**

Ex. $^{40}\text{Ar} + ^{197}\text{Au} \rightarrow ^{39}\text{Cl}$

If GH + Bibber is assumed,

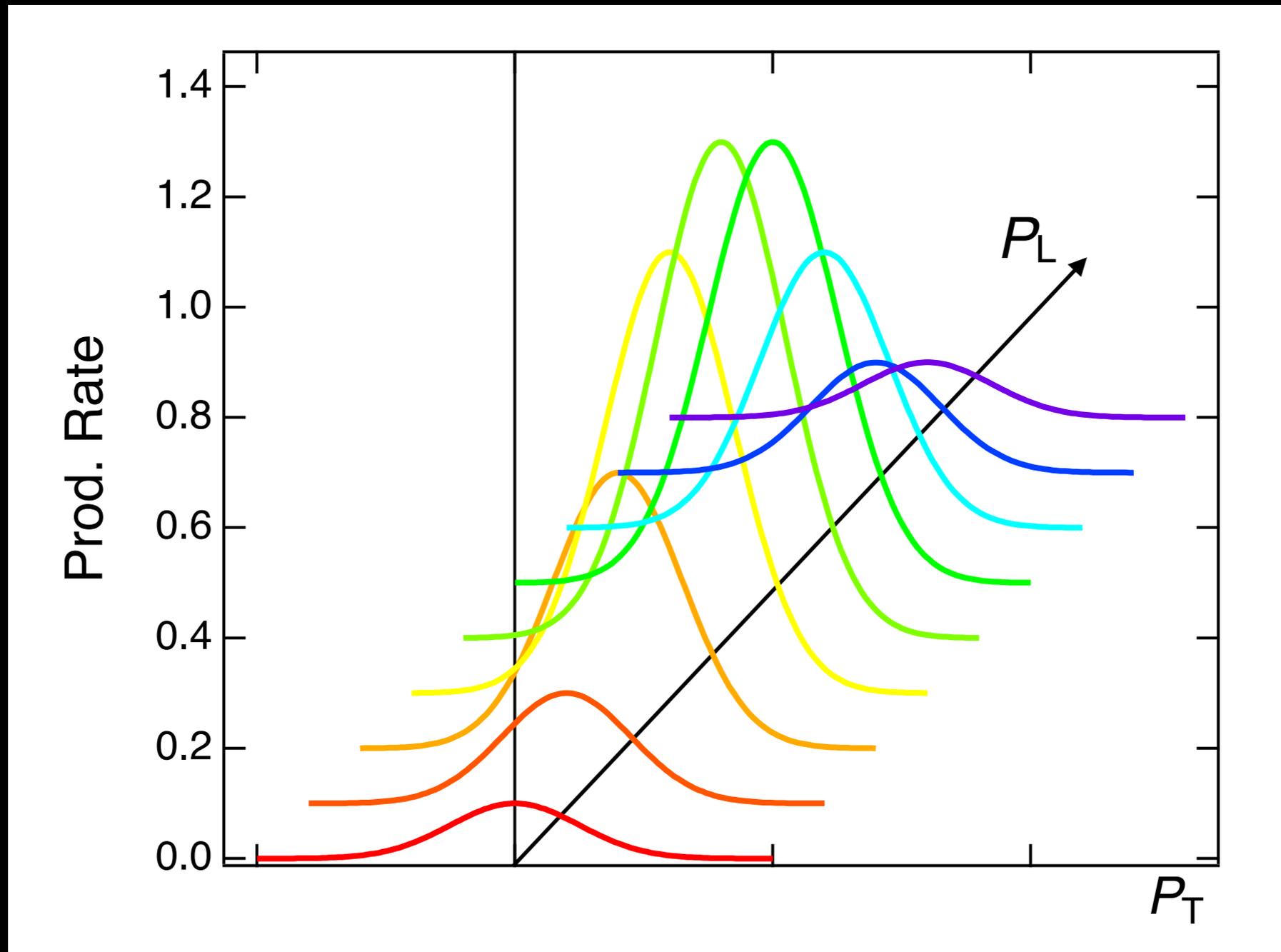
Actually...



Spuriously underestimated σ_{Prod}
would be provided.

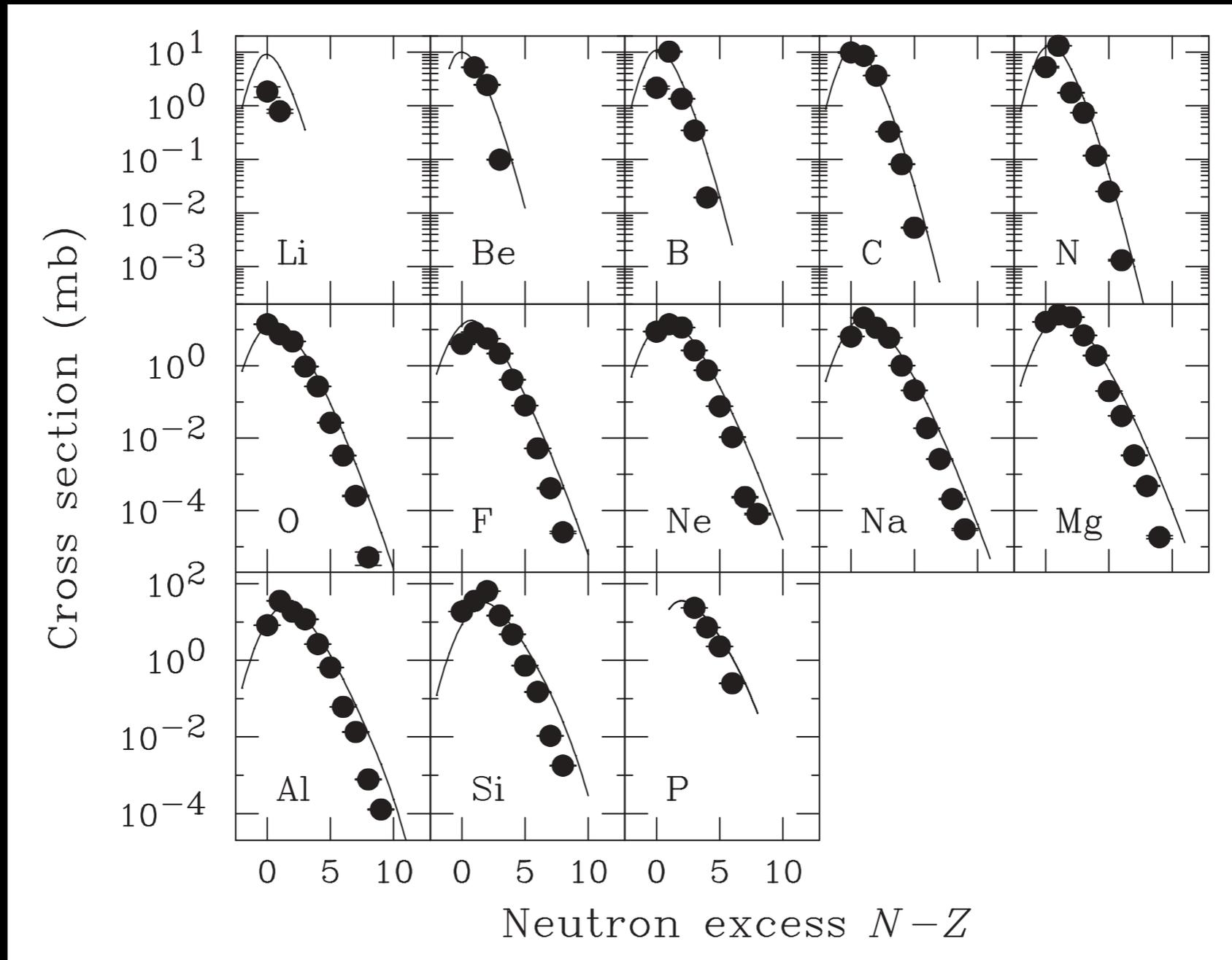
How to obtain σ_{Prod}

- Integration along P_L



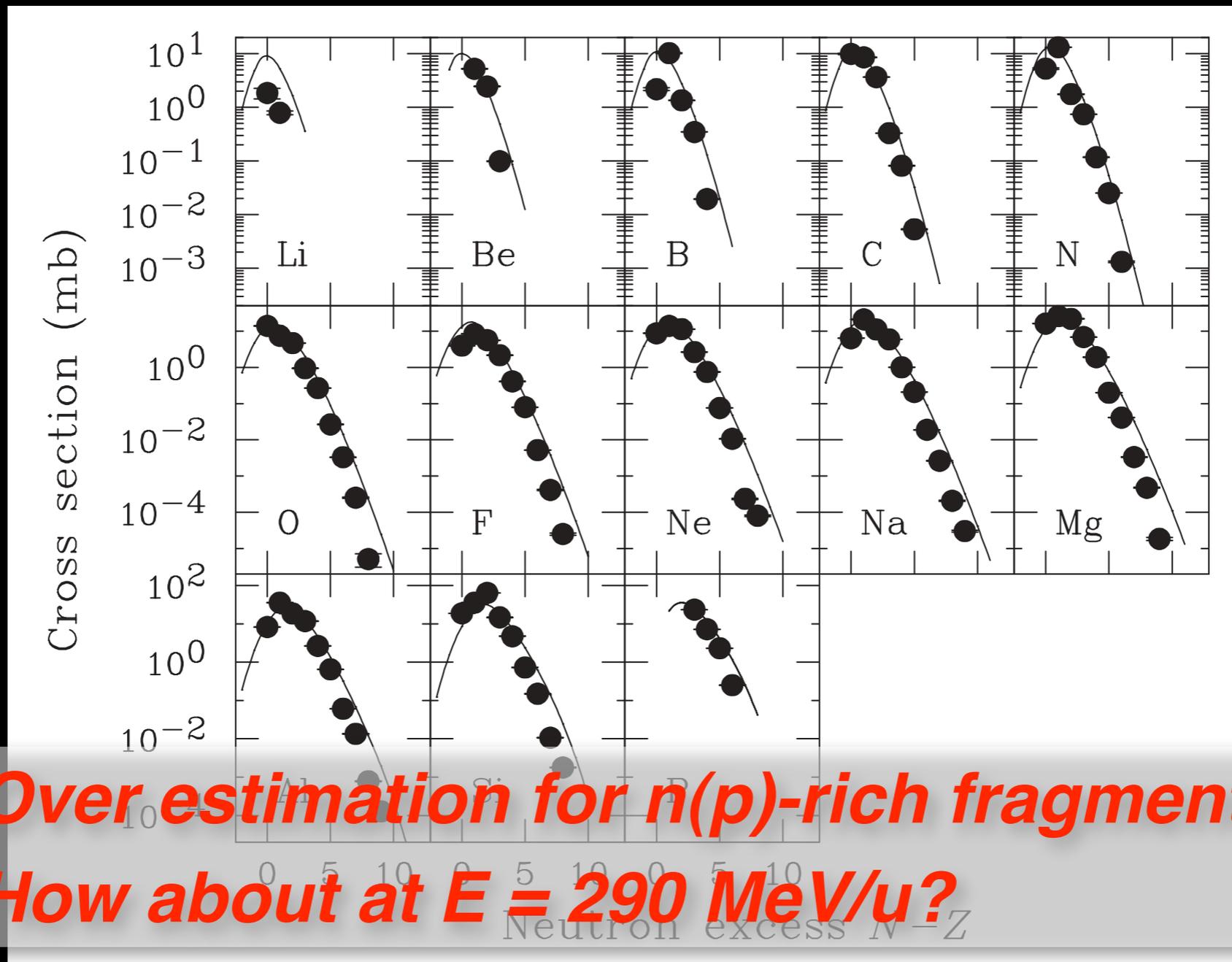
$\sigma_{\text{Prod.}}$ at $E = 90 \text{ MeV/u}$

- $^{40}\text{Ar} + ^9\text{Be}$



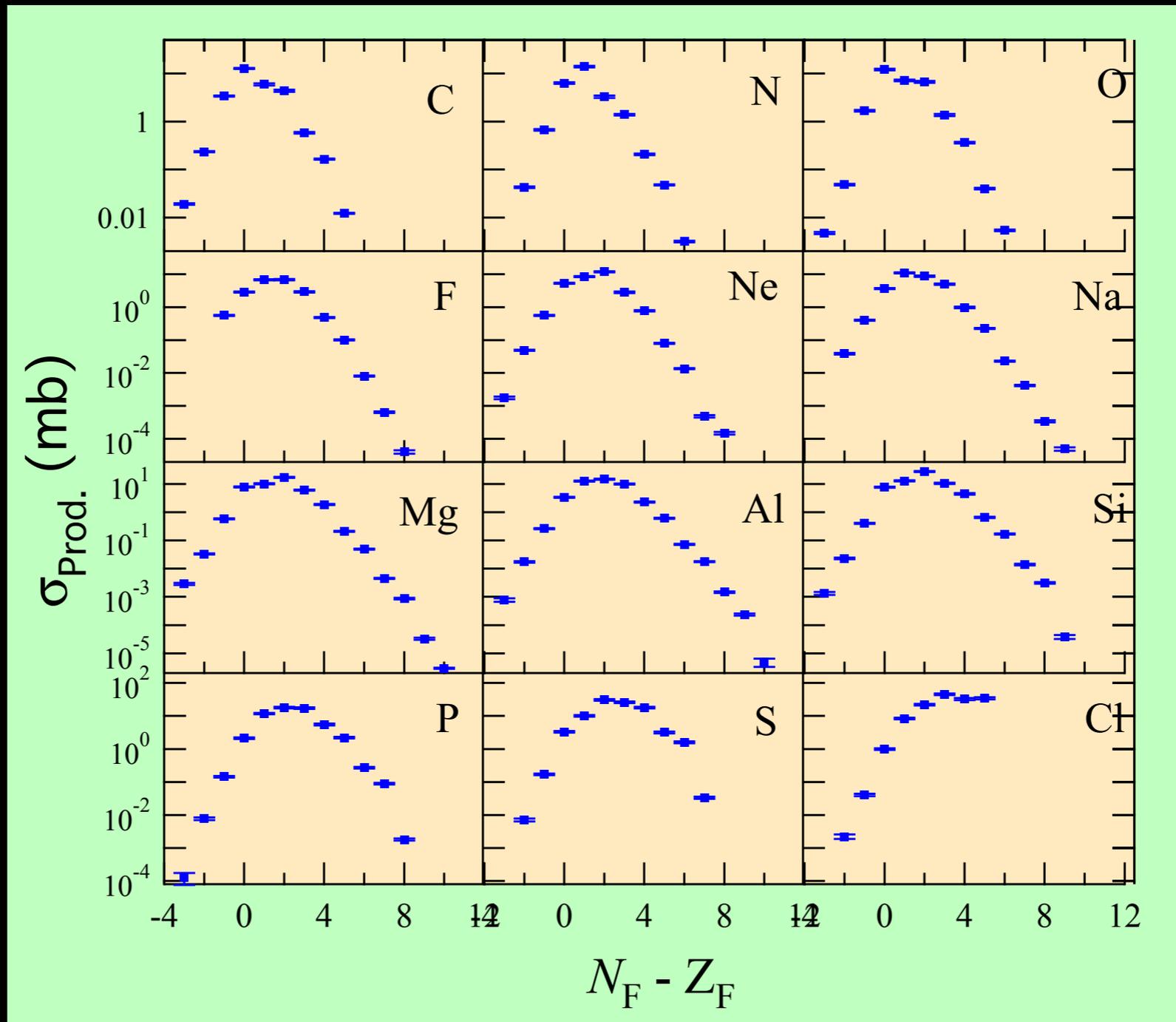
$\sigma_{\text{Prod.}}$ at $E = 90 \text{ MeV/u}$

- $^{40}\text{Ar} + ^9\text{Be}$



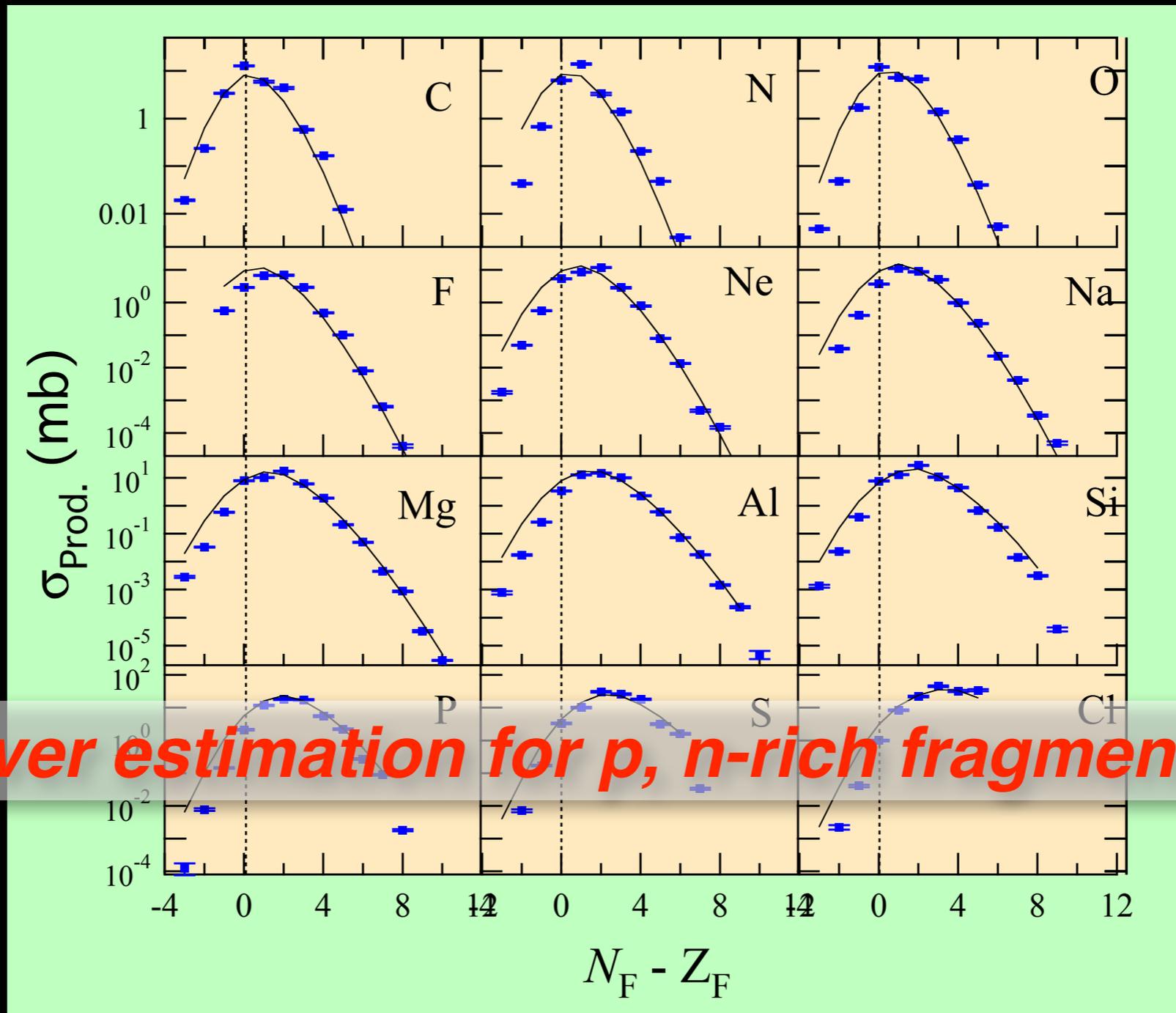
$\sigma_{\text{Prod.}}$ at $E = 290 \text{ MeV/u}$

- ^{40}Ar (290 MeV/u) + ^{12}C



$\sigma_{\text{Prod.}}$ at $E = 290 \text{ MeV/u}$

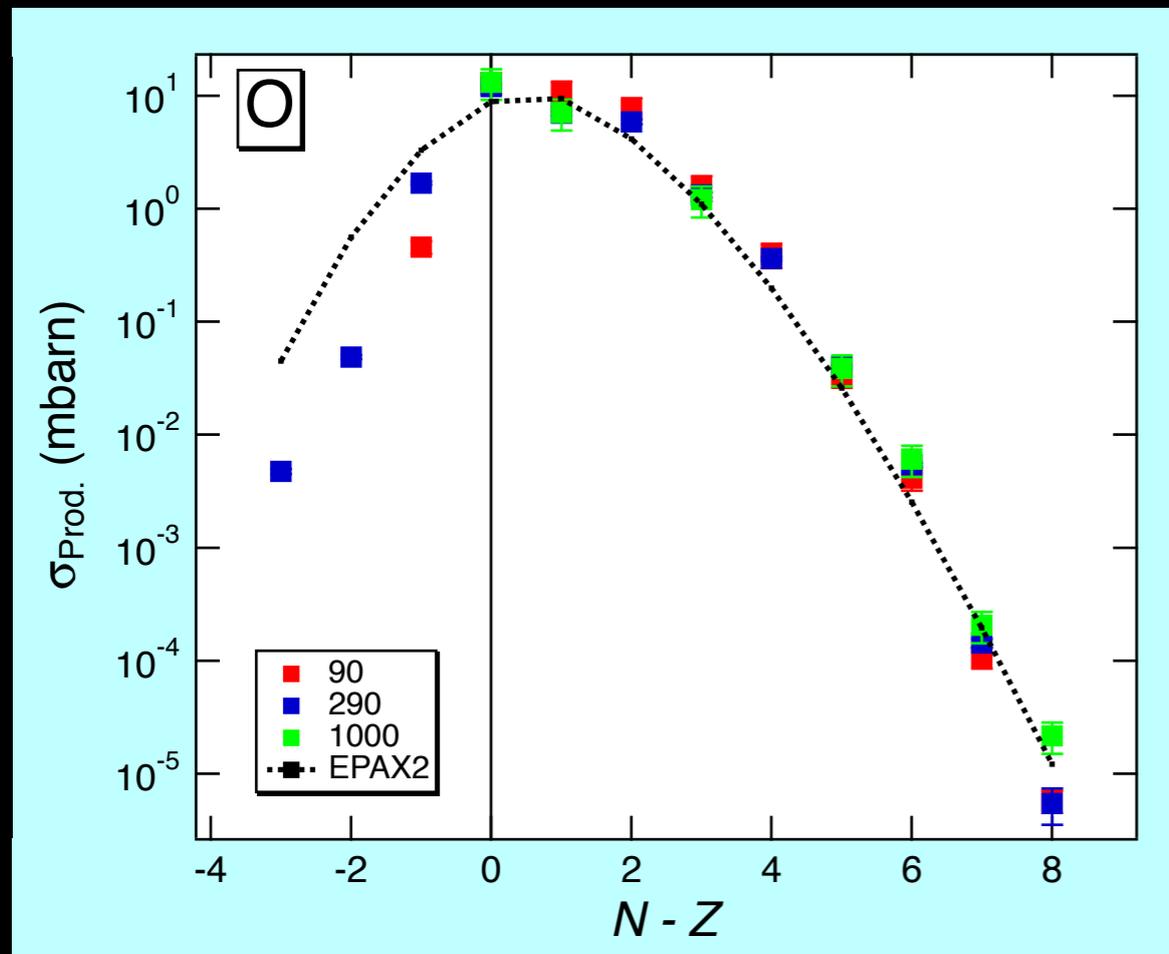
- ^{40}Ar (290 MeV/u) + ^{12}C



Energy dependence

- ^{40}Ar (290 MeV/u) + ^9Be , ^{12}C

Normalized by EPAX2



90 MeV/u : *M. Notani et al.*, PRC 76 (2007) 044605.

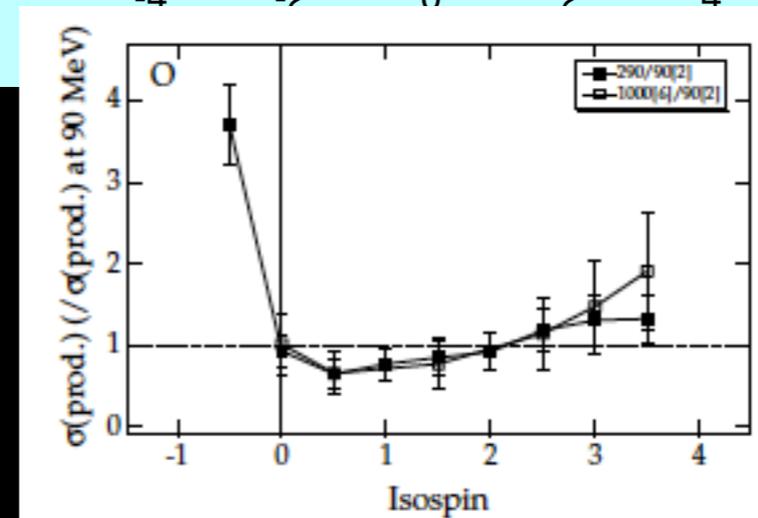
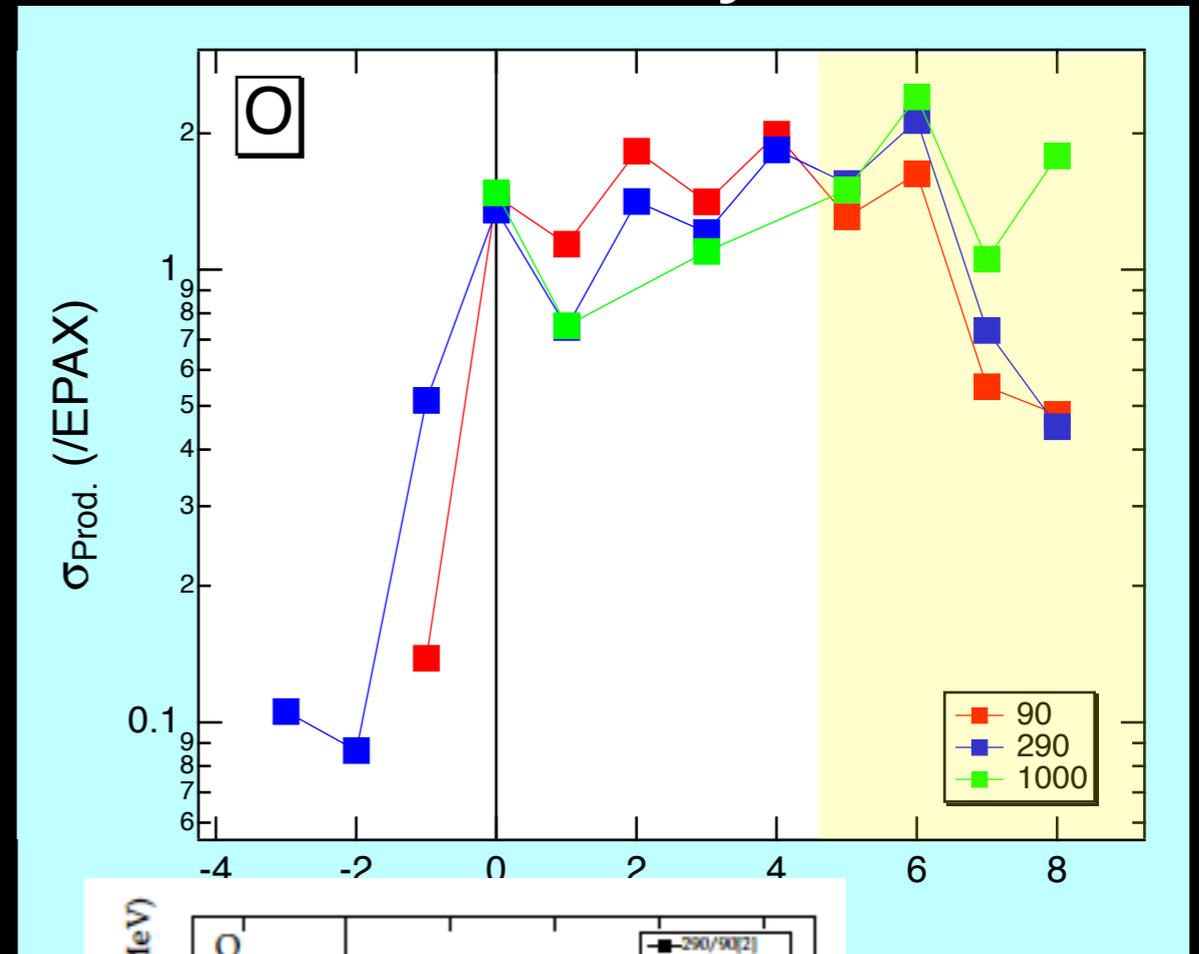
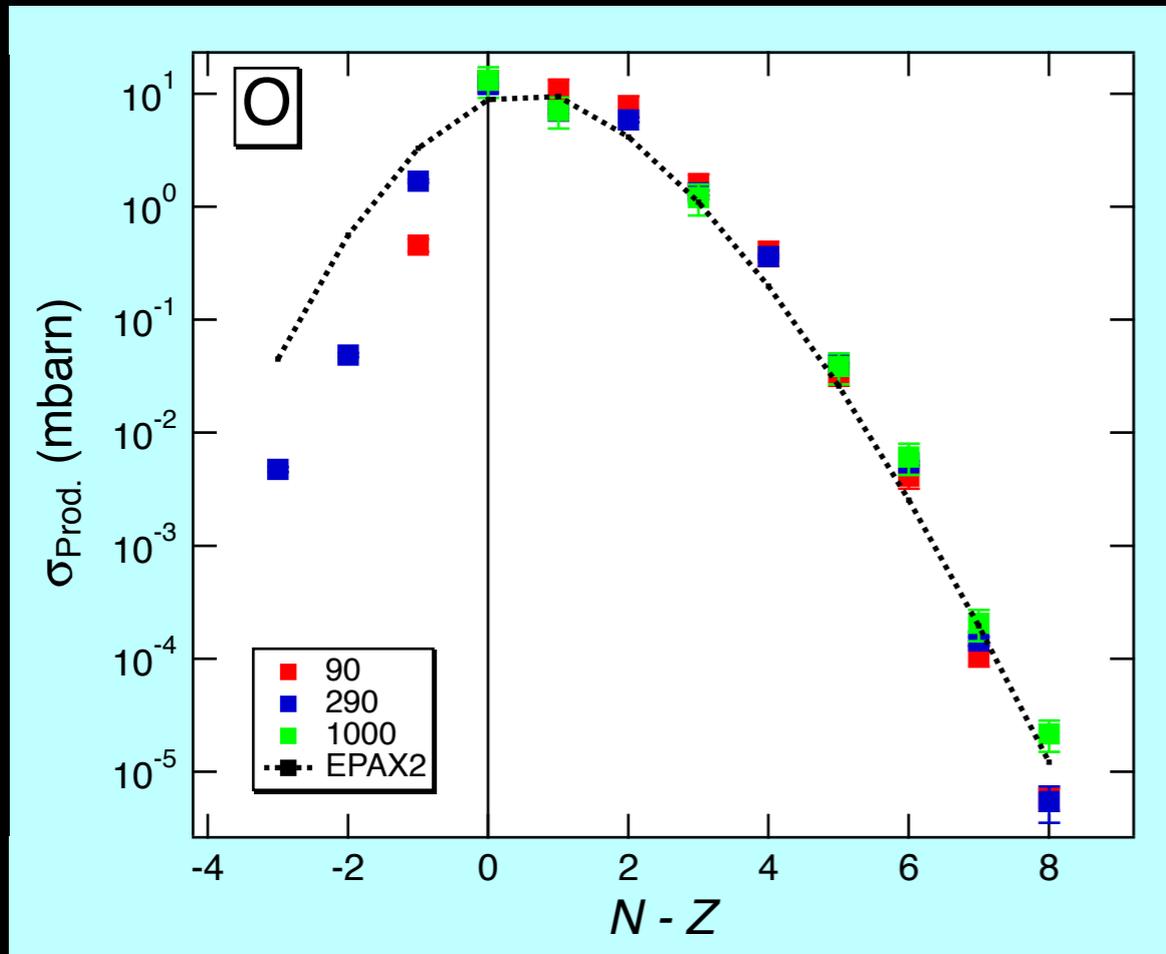
290 MeV/u : Our results

1000 MeV/u : *A. Ozawa et al.*, NP A 673 (2000) 375.

Energy dependence

- ^{40}Ar (290 MeV/u) + ^9Be , ^{12}C

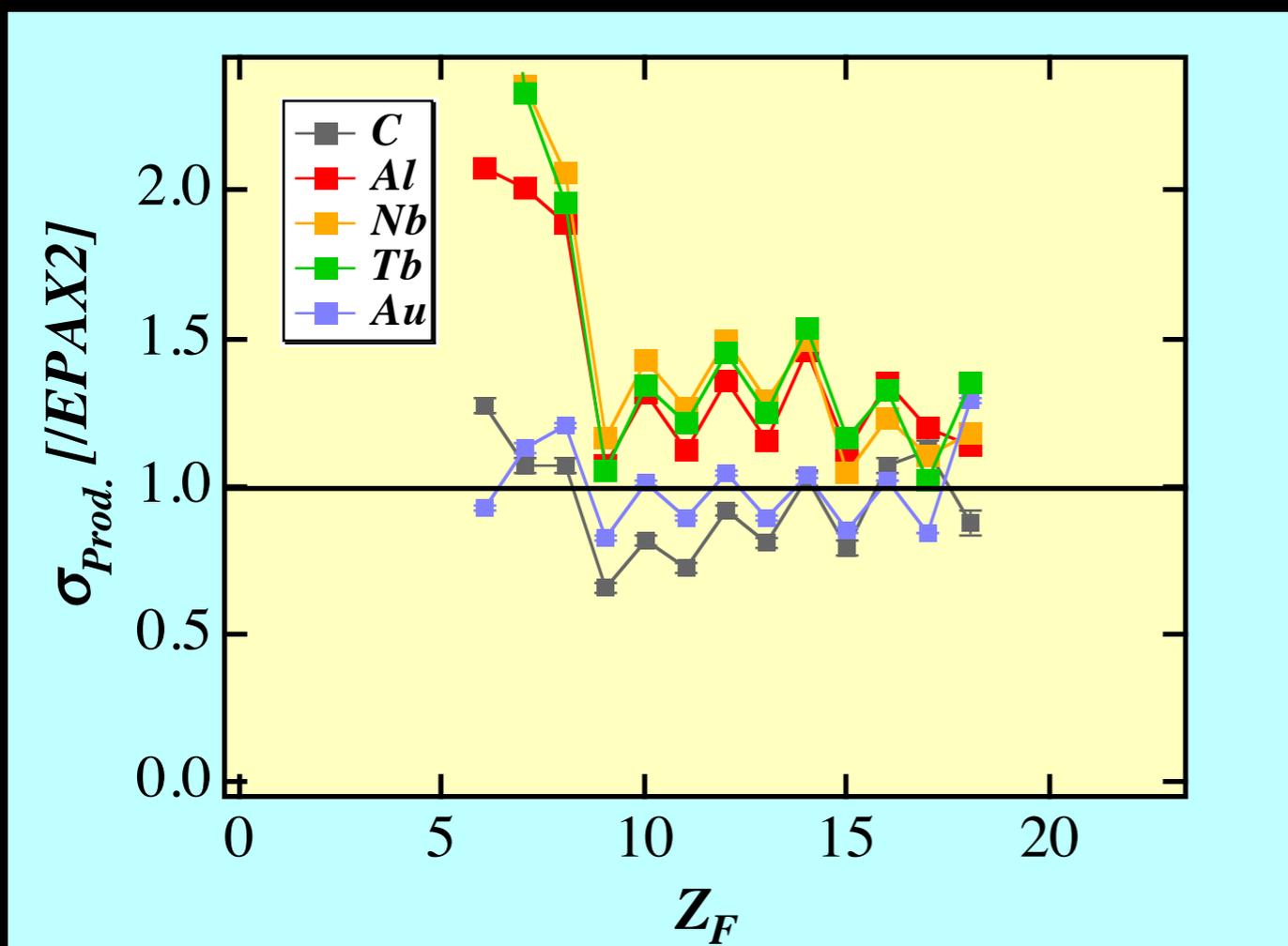
Normalized by EPAX2



90 MeV/u : *M. Notani et al.*, PRC 76 (2007) 044605.
 290 MeV/u : Our results
 1000 MeV/u : *A. Ozawa et al.*, NP A 673 (2000) 375.

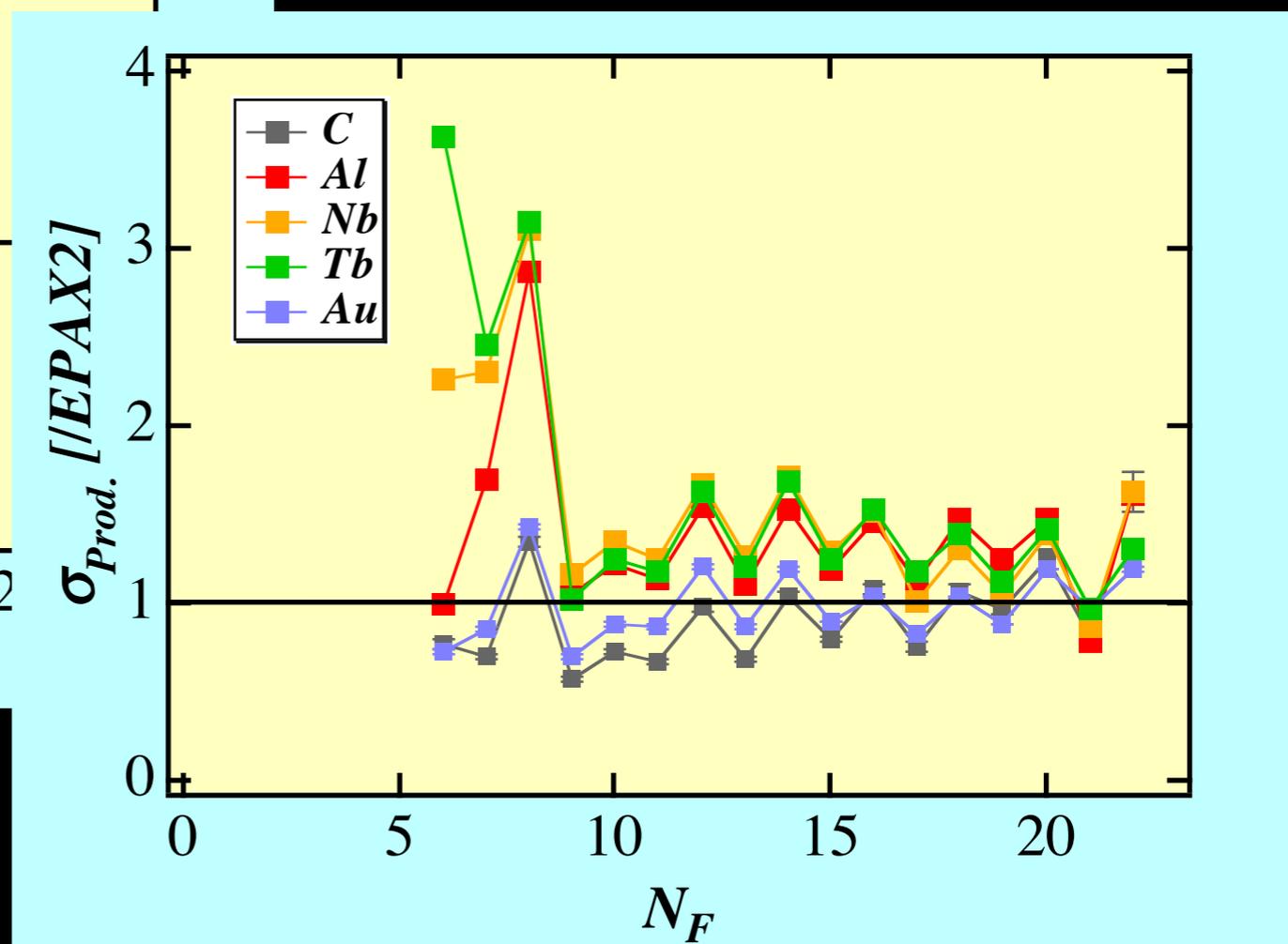
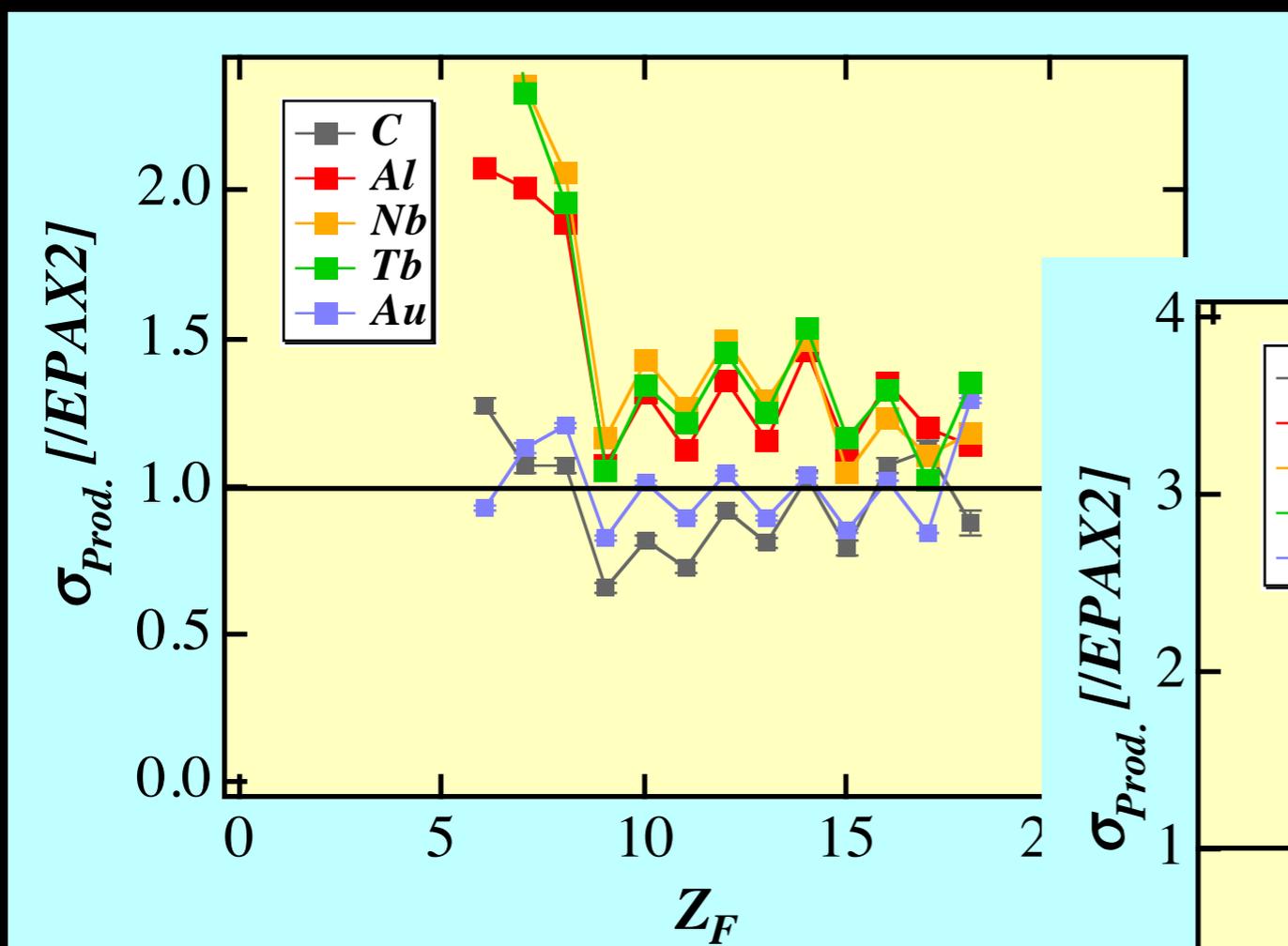
Contribution of nucl. structure

- Paring, Shell effect



Contribution of nucl. structure

- Paring, Shell effect



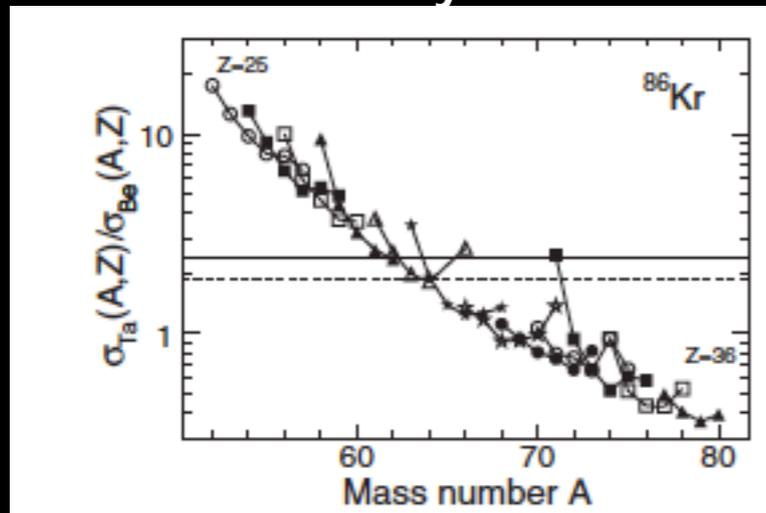
$\sigma_{\text{Prod.}}$ with Kr-beam

Measured and analysis in progress

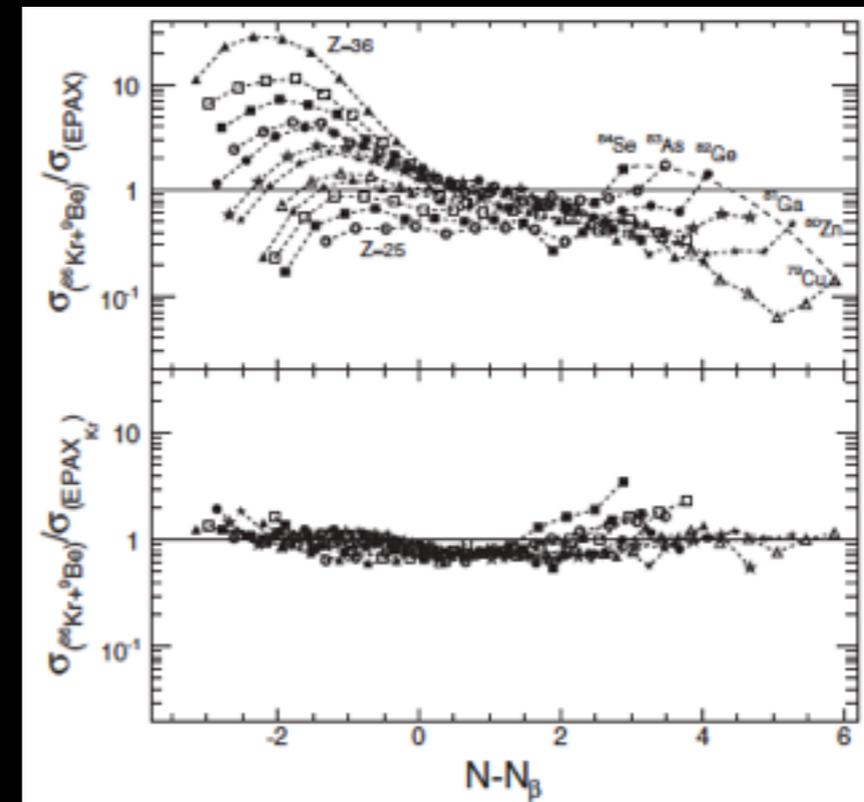
Modification of EPAX

- ^{86}Kr (64 MeV/u) + ^9Be , ^{181}Ta *M. Mocho et al., PRC 76 (2007) 014609.*

Mass yield



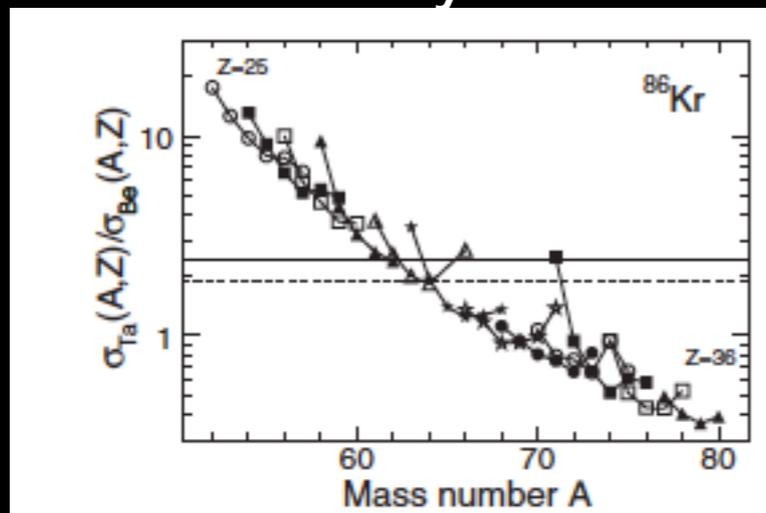
Optimization of EPAX



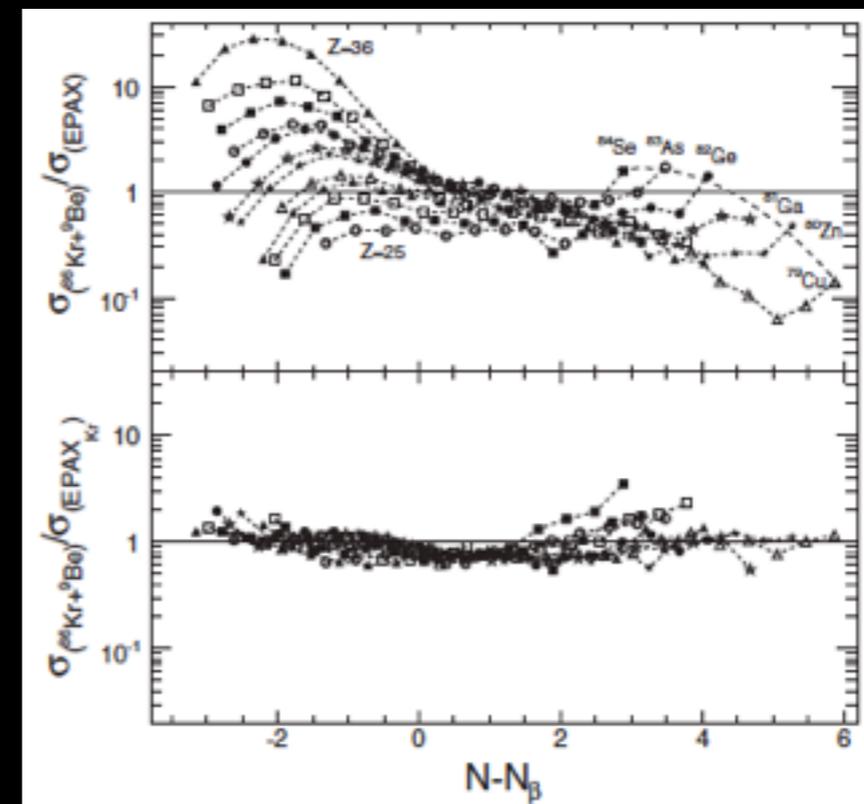
Modification of EPAX

- ^{86}Kr (64 MeV/u) + ^9Be , ^{181}Ta *M. Mocho et al., PRC 76 (2007) 014609.*

Mass yield



Optimization of EPAX



P_{T} distribution is assumed to be a simple Gaussian.

$$\sigma_{\perp}^2 = \sigma_0^2 \frac{A(A_P - A)}{A_P - 1} + \sigma_D^2 \frac{A(A - 1)}{A_P(A_P - 1)}$$

If the orbital deflection is considered, ...

Conclusions

At $E = 90, 290 \text{ MeV/u}$

- P_L distribution

Lower side : contribution of other reaction processes

Higher side: well reproduced by Goldhaber formulation.

- P_T distribution

@95 MeV/u : contribution of other reaction processes

@290 MeV/u

Light targets : No additional dispersion

Heavy targets: Orbital deflection effect

- Production cross sections

Contribution of nuclear structure

Careful consideration to P_T distribution

Development of formulation/HI transport code

Thanks to

RIKEN: r280n collaboration

*I. Tanihata, A. Ozawa, M. Notani, K. Yoshida,
K. Morimoto, T. Onishi, T. Yamaguchi, A. Yoshida,
Y.X. Watanabe, L. Zhong, and Y. Nojiri*

NIRS: P078, P178 Collaboration

M. Kanazawa, A. Kitagawa, S. Sato, and M. Suda